

1.  ${}^7\text{Li}+{}^{208}\text{Pb}$  within a two-body cluster model. We wish to study the reaction  ${}^7\text{Li}+{}^{208}\text{Pb}$  at  $E_{\text{lab}}=33$  MeV within the coupled-channels method, using a cluster model of the  ${}^7\text{Li}$  nucleus. We will consider only the bound state of this nucleus ( $3/2^-$ ) and the first excited state ( $E_x = 0.477$  MeV;  $1/2^-$ ). These states will be described assuming a  $\alpha+t$  cluster model. The nuclear part of the interaction between the clusters is parametrized in terms of a Gaussian potential with  $V_0 = -87.77$  MeV and  $R_0 = 2.52$  fm (absolute radius) and a spin-orbit part, also of Gaussian shape, with parameters  $V_{so} = 3.8$  MeV and  $R_{so}=2.52$  fm. The  $\alpha+{}^{208}\text{Pb}$  and  $t+{}^{208}\text{Pb}$  interactions are described in terms of standard (volume) Woods-Saxon forms, with the following parameters ( $R_x = r_x A_t^{1/3}$ ):

System	$V_0$ (MeV)	$r_0$ (fm)	$a_0$ (fm)	$W_v$ (MeV)	$r_i$ (fm)	$a_i$ (fm)	$r_c$ (fm)
$\alpha+{}^{208}\text{Pb}$	35.0	1.547	0.570	9.0	1.547	0.57	1.547
$t+{}^{208}\text{Pb}$	161.24	1.20	0.720	18.06	1.40	0.84	1.30

### Questions:

- (a) Calculate the elastic and inelastic scattering angular distributions. Check the convergence of the calculation with respect the the maximum integration radius (`rmatch`) and the maximum total angular momentum (`jtnmax`).
  - (b) Compare the *converged* calculation with the elastic and inelastic data reported in the work of Rusek *et al*, Nuclear Physics A 614 (1997) 112.
  - (c) Reduce the maximum total angular momentum to `jtnmax=25` and recalculate the inelastic angular distribution. How would you interpret the observed oscillations?
  - (d) Using the information contained in the `fort.56` output file, plot the reaction and inelastic cross section as a function of the total angular momentum. Comment on the results in connection with the previous item.
2. *CDCC calculation for deuteron scattering*. Consider the reaction  $d+{}^{58}\text{Ni}$  at  $E_d = 80$  MeV, described in a three-body model ( $p+n+{}^{58}\text{Ni}$ ). The proton-neutron interaction is described with a simple Gaussian potential:  $V(r) = -72.15 \exp[-(r/1.484)^2]$  MeV.
    - (a) Find suitable potentials for the proton- ${}^{58}\text{Ni}$  and neutron- ${}^{58}\text{Ni}$  systems at the appropriate energy per nucleon (you may get them from <http://www-nds.iaea.org/RIPL-3/>).
    - (b) With the help of the CDC code, build the FRESKO input for this reaction. Consider only the partial waves  $\ell=0,2$  for the deuteron continuum, and set to zero the spin of the proton and the neutron. For each partial wave, truncate the continuum at a maximum energy of  $E_{rel}=20$  MeV and discretize it using initially 5 bins with the same width (in  $k$ ). Calculate the elastic scattering (relative to Rutherford) and the (angle-integrated) breakup differential cross section with respect to the excitation energy ( $d\sigma/dE_x$ ). For the latter, you may use the code SUMXEN installed in the TALENT server.

- (c) Increase progressively the maximum excitation energy and number of bins until you get converged (i.e. stable) results for both the elastic and  $d\sigma/dE_x$  breakup cross sections.
- (d) Compare with the elastic data for this reaction (available at the TALENT website).
- (e) Remove the continuum states, and perform a calculation including *only* the ground state of the deuteron. Compare the result with the data and the with full calculation.
- (f) Repeat the calculation using the DWBA approximation (`iter=1`, `iblock=0`) and compare with the result of the previous item. What can we conclude regarding the influence of multi-step processes in this reaction?
- (g) Perform a new calculation at  $E_d = 21$  MeV. Study the convergence with respect the the number of bins and the maximum excitation energy (for simplicity, use the same proton and neutron potentials as in the previous case).
- (h) Obtain the breakup energy distribution ( $d\sigma/dE_x$ ) and compare with the results at  $E_d=80$  MeV. Interpret the results.
- (i) At this energy, compare the full CC calculation with the DWBA solution. Interpret the results.