

Hands-on session on the phenomenological R-matrix method: excel program talent_rmatrix2013.xlsm

1. General remarks

- a. The program can fit elastic, inelastic or transfer cross sections.
- b. See additional help in the sheet "HELP".
- c. Data on energy levels can be found at the TUNL web page
<http://www.tunl.duke.edu/nuclldata/index.shtml>.

2. Inputs

- a. **Sheet "Main"**: the program is launched from this sheet.
- b. **Sheet "input"**: R-matrix parameters.
Each resonance is defined by at set 2 lines (must be repeated for each resonance).
line 1:
J= spin of the resonance (multiplied by 2 if half-integer)
nres: the number of resonances in the partial wave
ell=angular lomentum
l=channel spin (multiplied by 2 if half-integer)
line 2:
Energy, width (in MeV)
For inelastic scattering or transfer, line 1 is complemented by (ell, l) in the exit channel, and line 2 by the width in the exit channel.
- c. **Sheet with the data**: contains energy, cross section, and error in the 3 first columns.
Cells e1:h1 and e2 are used to specify the reaction. Other cells are not used by the program.

3. Use of the program

- a. Several data sets can be fitted simultaneously (e.g. different angles, or elastic and inelastic). The name of the data sheet(s) must be introduced in row 19 of sheet "Main").
- b. The parameters that you want to fit must be introduced in row 28. These parameters correspond to the cell of the sheet "input". **If no cell number is introduced, there is no fit. The program uses the parameters in sheet "input"**.
- c. Output: chi2, and parameters on row 33
cross sections, starting from row 36

Questions

1. $^{12}\text{C}+p$ elastic scattering

Experimental elastic cross sections for $^{12}\text{C}+p$ are given in sheets “c12p_146” and “c12p_89” for $\theta_{cm} = 146.9^\circ$ and $\theta_{cm} = 89.1^\circ$ (taken from H.O. Meyer et al., Z. Phys. A279 (1976) 41). They cover the energy range from 0 to 2 MeV, where 3 resonances (1/2+, 3/2-, 5/2+) are expected (see the ^{13}N spectrum, e.g. at <http://www.tunl.duke.edu/nuclldata/chain/13.shtml>)

- With $r_{max}=5$ fm, determine the properties (energy and proton width) of these 3 resonances by a fit of the data (use the experimental values as initial conditions).
- Check that the results (R-matrix parameters, cross sections) are nearly insensitive to the channel radius (reasonable variations).

2. $^6\text{He}(p,n)$ transfer

The analog of the ^7He ground state is a 3/2- resonance at $E_x=11.24$ MeV in ^7Li (see figure below). This resonance has been investigated by Rogachev et al. (Phys. Rev. Lett. 92 (2004) 232502) by the $^6\text{He}(p,n)^6\text{Li}$ reaction. The experimental data are given in sheet “he6pn”.

- Determine the c.m. energy in the entrance channel, and the angular momentum of the resonance.
- This resonance has an isospin $T=3/2$. Determine the possible ^6Li state(s) populated by the $^6\text{He}(p,n)^6\text{Li}$ reaction, and the c.m. energy in the exit channel.
- The total width of the resonance is $\Gamma = 260$ keV. This width is composed of a proton and of a neutron partial widths: $\Gamma = \Gamma_p + \Gamma_n$. From isospin selection rules one expects the ratio of the *reduced* widths: $\gamma_n^2/\gamma_p^2 = 2$.

By using sheet “Coulomb” to compute the penetration factors, determine the expected values for Γ_p and Γ_n .

- Enter these values in sheet “input”, and the appropriate masses and charges in sheet “Main” (check the option “Include inelastic or transfer channels”). Compare the R-matrix results with the data.
- The $^6\text{He}+p$ elastic scattering at these energies is unknown experimentally. A sheet with “arbitrary” data is provided by he6pp. Compute the predicted elastic cross section at 180 degrees.

Assume that the neutron width $\Gamma_n = 0$, and that the total width is given by the proton component: $\Gamma = \Gamma_p = 260$ keV. Compare the elastic cross section.

