



Isomers in the $f_{7/2}$ shell

Secrets of the E6

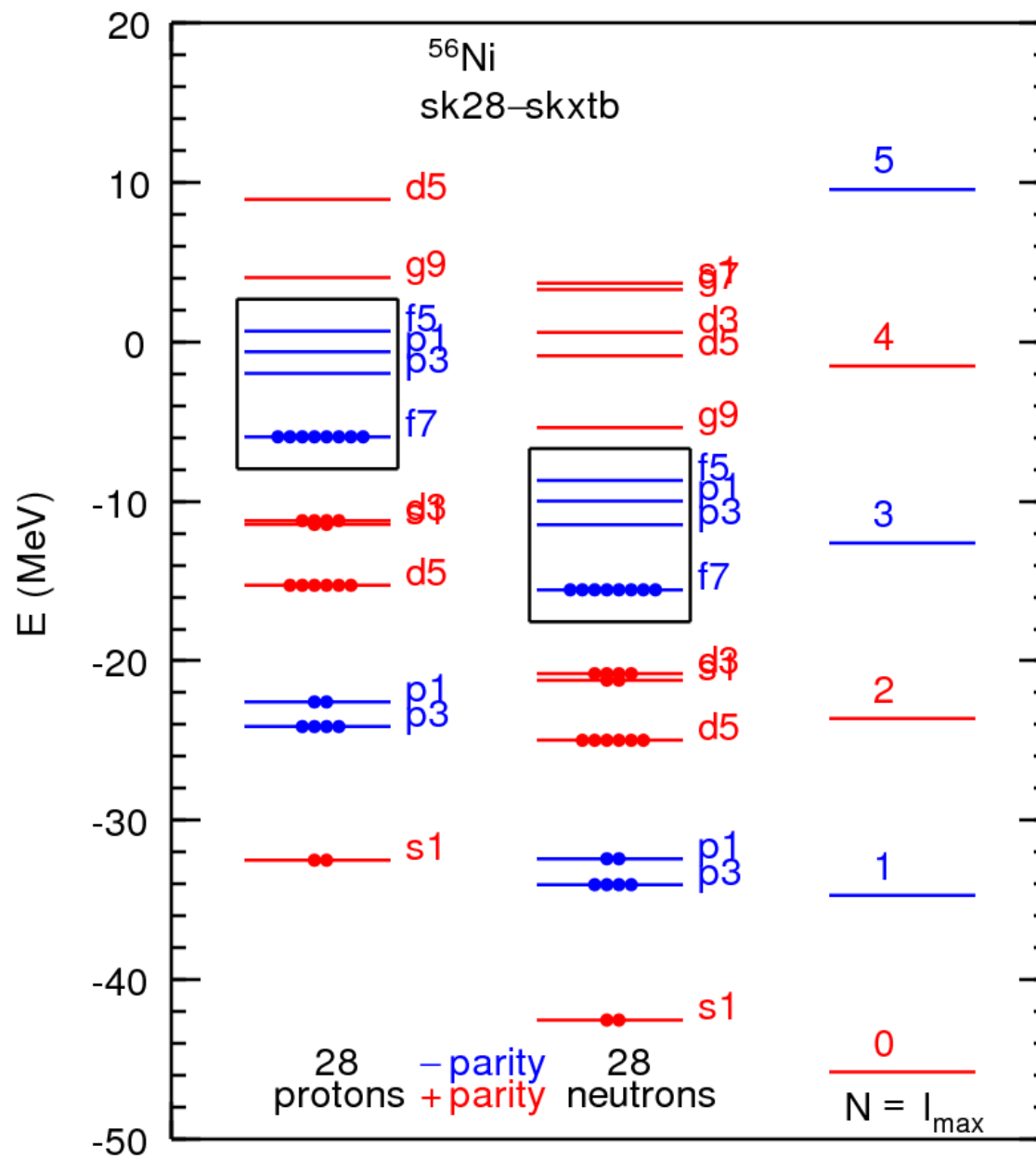
Alex Brown
Michigan State University

Workshop on Nuclear Isomers: Structure and Applications

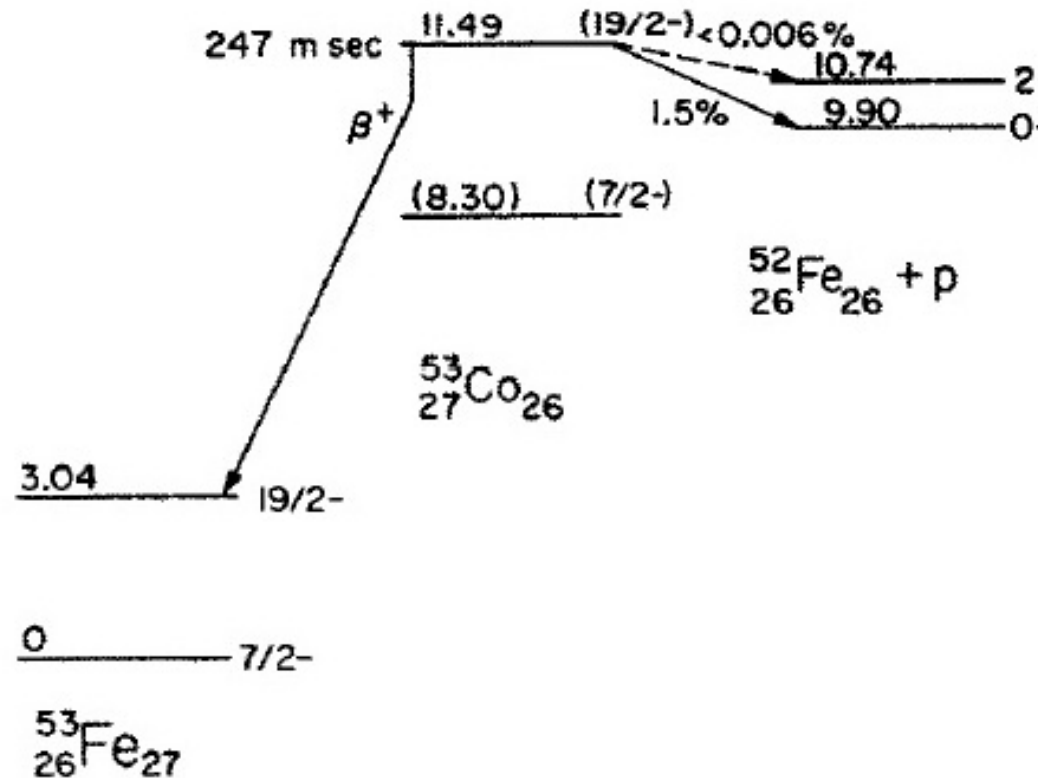
University of Surrey, Guildford, UK
May 19-21, 2010



Alex Brown, May 19, 2010



1970 first proton decay from an isomer - in ^{53}Co



$^{53}\text{Co}^{\text{m}}$: A PROTON-UNSTABLE ISOMER[†]K. P. JACKSON *, C. U. CARDINAL **, H. C. EVANS [‡] and N. A. JELLEY*Nuclear Physics Laboratory, University of Oxford, England*J. CERNY^{‡‡}*Nuclear Physics Laboratory, University of Oxford, England; and
Lawrence Radiation Laboratory and Department of Chemistry,
University of California, Berkeley, California 94720, USA.*

Received 23 September 1970

A 1.53 ± 0.04 MeV proton activity with a 245 ± 20 ms half-life has been observed in the reaction of ^{16}O on ^{40}Ca . The most plausible origin of this activity is the proton radioactivity of $^{53}\text{Co}^{\text{m}}$, although the decay of this isomer by beta-delayed proton emission remains a possibility.

CONFIRMED PROTON RADIOACTIVITY[‡] OF $^{53}\text{Co}^{\text{m}}$

J. CERNY, J. E. ESTERL, R. A. GOUGH* and R. G. SEXTRO

*Department of Chemistry and Lawrence Radiation Laboratory
University of California, Berkeley, California 94720, USA*

Received 23 September 1970

Proton-induced reactions on ^{54}Fe produce a proton activity [1.57 ± 0.03 MeV; 242 ± 15 ms] with a threshold of 26.3 ± 0.4 MeV which can only arise from $^{53}\text{Co}^{\text{m}}$. Failure to detect positron-proton coincidences in the decay of this isomer establishes its *direct* proton radioactivity.

1.E.4

Nuclear Physics A188 (1972) 666—672; © North-Holland Publishing Co., Amsterdam

Not to be reproduced by photoprint or microfilm without written permission from the publisher

FURTHER RESULTS ON THE PROTON RADIOACTIVITY OF $^{53\text{m}}\text{Co}$

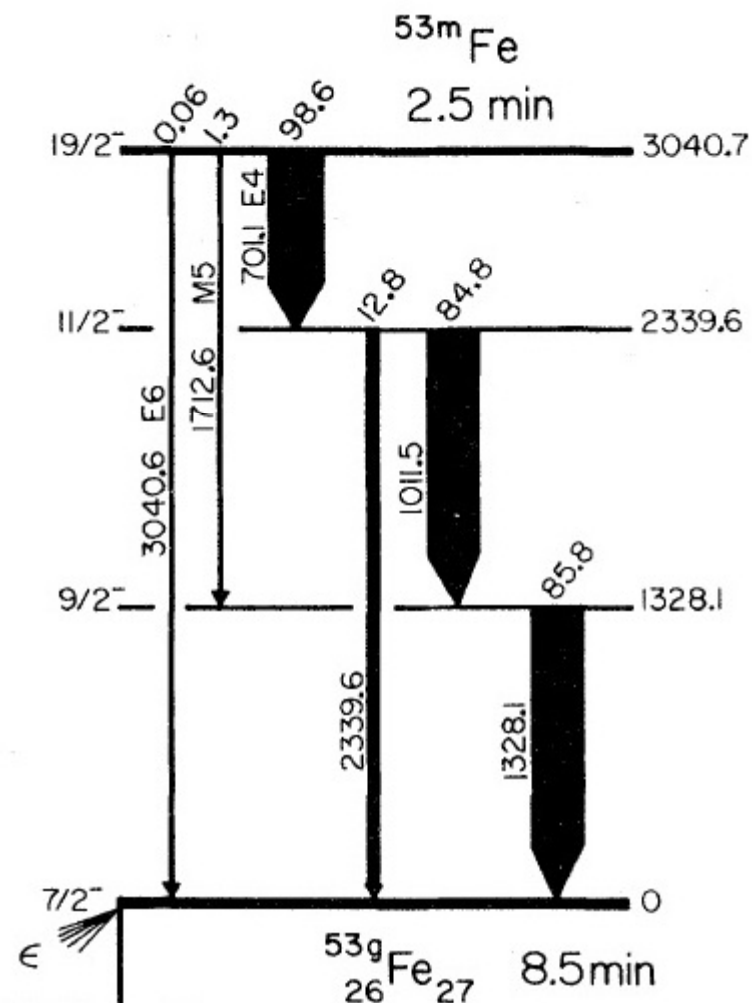
JOSEPH CERNY, R. A. GOUGH[†], R. G. SEXTRO and JOHN E. ESTERL^{††}

*Department of Chemistry and Lawrence Berkeley Laboratory, University of California,
Berkeley, California 94720^{†††}*

Received 7 March 1972

Abstract: Additional studies on the proton radioactivity of the 247 ± 12 msec isomer $^{53\text{m}}\text{Co}$ lead to an improved estimate of ≈ 17 sec for its partial half-life for emission of 1.59 ± 0.03 MeV protons to the ^{52}Fe ground state. An upper limit of 1/250 for the ratio of direct proton decay to the $^{52}\text{Fe}^*(2^+, 0.84 \text{ MeV})$ state relative to decay to the $^{52}\text{Fe}(\text{g.s.})$ can be set.

1975 first E6 decay - from an isomer ^{53}Fe



Alex Brown, May 19, 2010

PHYSICAL REVIEW C

VOLUME 11, NUMBER 3

MARCH 1975

Decays of the $f_{7/2}$ isomers $^{53}\text{Fe}^g$ and $^{53}\text{Fe}^m$

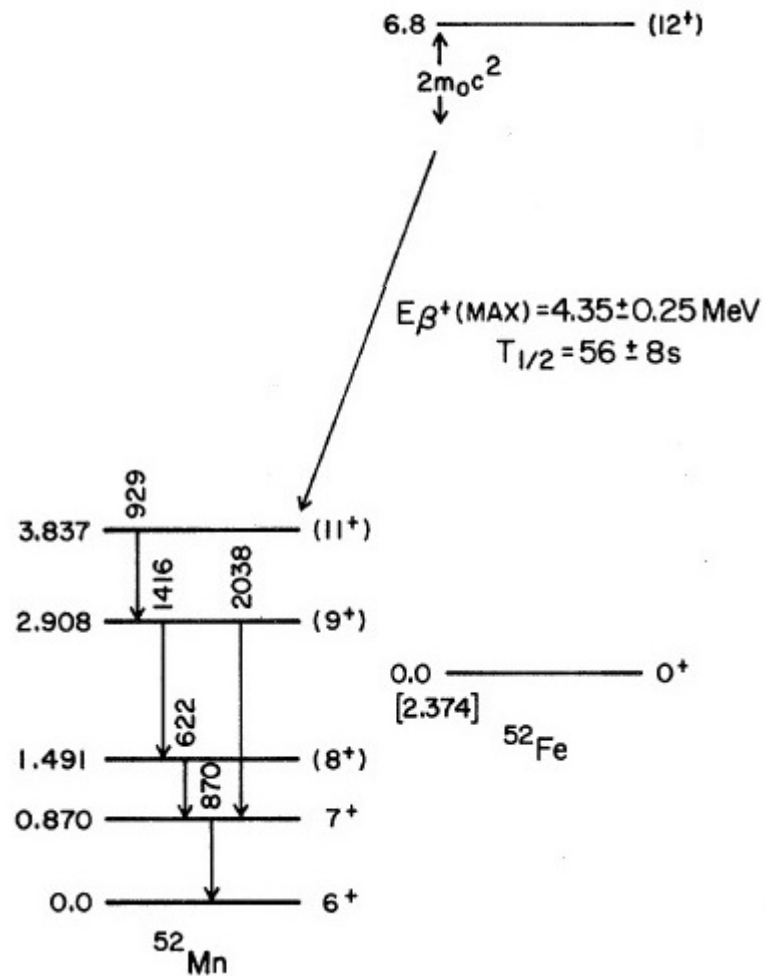
J. N. Black* and Wm. C. McHarris†

*Department of Chemistry,‡ Cyclotron Laboratory,§ and Department of Physics,
Michigan State University, East Lansing, Michigan 48824*

W. H. Kelly and B. H. Wildenthal

Cyclotron Laboratory§ and Department of Physics, Michigan State University, East Lansing, Michigan 48824
(Received 25 July 1974)

1975 beta isomer in ^{52}Fe



$^{52}\text{Fe}(6.8\text{ MeV})\beta\text{-Decaying Isomeric State}^*$

D. F. Geesaman, R. Malmin, R. L. McGrath, and J. W. Noé

Department of Physics, State University of New York, Stony Brook, New York 11974

and

J. Cerny

*Lawrence Berkeley Laboratory and Department of Chemistry, University of California,
Berkeley, California 94720**(Received 26 August 1974)*

An isomeric state in ^{52}Fe has been located at $E_x = 6.83 \pm 0.25$ MeV with the reaction $^{40}\text{Ca}(^{14}\text{N}, pn)^{52}\text{Fe}$. The state decays by positron emission to the (11^+) 3.837-MeV state of ^{52}Mn with $T_{1/2} = 56 \pm 8$ sec. The probable spin and parity of the isomer is 12^+ .

1979 search for E4 gamma in ^{52}Fe – not found

PHYSICAL REVIEW C

VOLUME 19, NUMBER 5

MAY 1979

Yrast states in ^{52}Fe , ^{52}Mn and the decay of $^{52}\text{Fe}^m$

D. F. Geesaman,* R. L. McGrath, J. W. Noé, and R. E. Malmin†

Department of Physics, State University of New York, Stony Brook, New York 11794

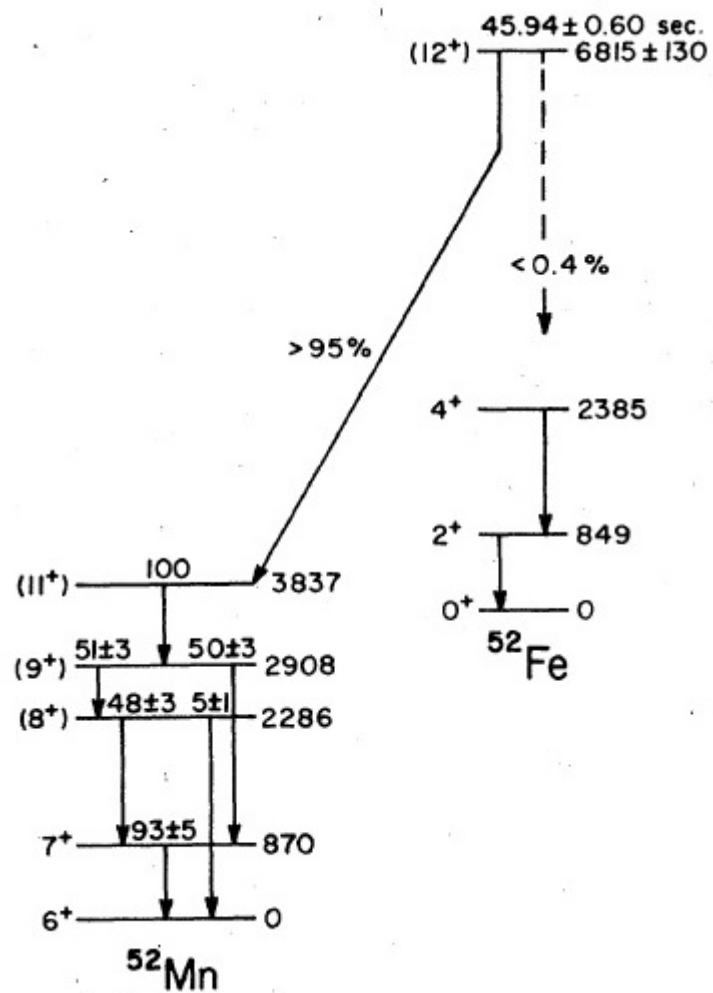
(Received 5 December 1978)

^{43}Sc		^{53}Fe	
Exp.	Calc.	Calc.	Exp.
$\frac{3.12}{2.99} \begin{matrix} 19/2^- \\ 15/2^- \end{matrix}$	$\frac{3.64}{3.51} \begin{matrix} 19/2^- \\ 15/2^- \end{matrix}$	$\frac{3.31}{3.03} \begin{matrix} 15/2^- \\ 19/2^- \end{matrix}$	$\frac{3.04}{2.34} \begin{matrix} 19/2^- \\ 11/2^- \end{matrix}$
$\frac{1.83}{0.0} \begin{matrix} 11/2^- \\ 7/2^- \end{matrix}$	$\frac{2.34}{1.68} \begin{matrix} 11/2^- \\ 9/2^- \end{matrix}$	$\frac{2.36}{1.58} \begin{matrix} 11/2^- \\ 9/2^- \end{matrix}$	$\frac{1.33}{0.0} \begin{matrix} 9/2^- \\ 7/2^- \end{matrix}$

FIG. 10. Comparison of experimental and $(1f_{7/2})^{\pm 3}$ model level schemes of ^{43}Sc and ^{53}Fe . Effective interactions taken from ^{42}Sc and ^{54}Co spectra were used for ^{43}Sc and ^{53}Fe , respectively.

^{44}Ti		^{52}Fe	
Exp.	Calc.	Calc.	Exp.
<u>8.04</u> (12 ⁺)	<u>7.69</u> 12 ⁺	<u>7.04</u> 10 ⁺	<u>6.82</u> (12 ⁺)
<u>7.67</u> (10 ⁺)	<u>7.38</u> 10 ⁺	<u>6.97</u> 12 ⁺	
<u>6.51</u> (8 ⁺)	<u>6.08</u> 8 ⁺	<u>5.99</u> 8 ⁺	
		<u>4.34</u> 6 ⁺	
<u>4.02</u> 6 ⁺	<u>4.06</u> 6 ⁺		
	<u>2.79</u> 4 ⁺	<u>2.78</u> 4 ⁺	<u>2.38</u> 4 ⁺
<u>2.45</u> 4 ⁺			
<u>1.08</u> 2 ⁺	<u>1.16</u> 2 ⁺	<u>1.05</u> 2 ⁺	<u>0.85</u> 2 ⁺
<u>0.0</u> 0 ⁺	<u>0.0</u> 0 ⁺	<u>0.0</u> 0 ⁺	<u>0.0</u> 0 ⁺

FIG. 9. Comparison of experimental and $(1f_{7/2})^{\pm 4}$ model level schemes of ^{44}Ti and ^{52}Fe . Two different empirical effective interactions taken from ^{42}Sc and ^{54}Co spectra were used for ^{44}Ti and ^{52}Fe , respectively.



Alex Brown, May 19, 2010

2005 search for E4 gamma in ^{52}Fe – found (GASP)



Available online at www.sciencedirect.com

SCIENCE @ DIRECT®

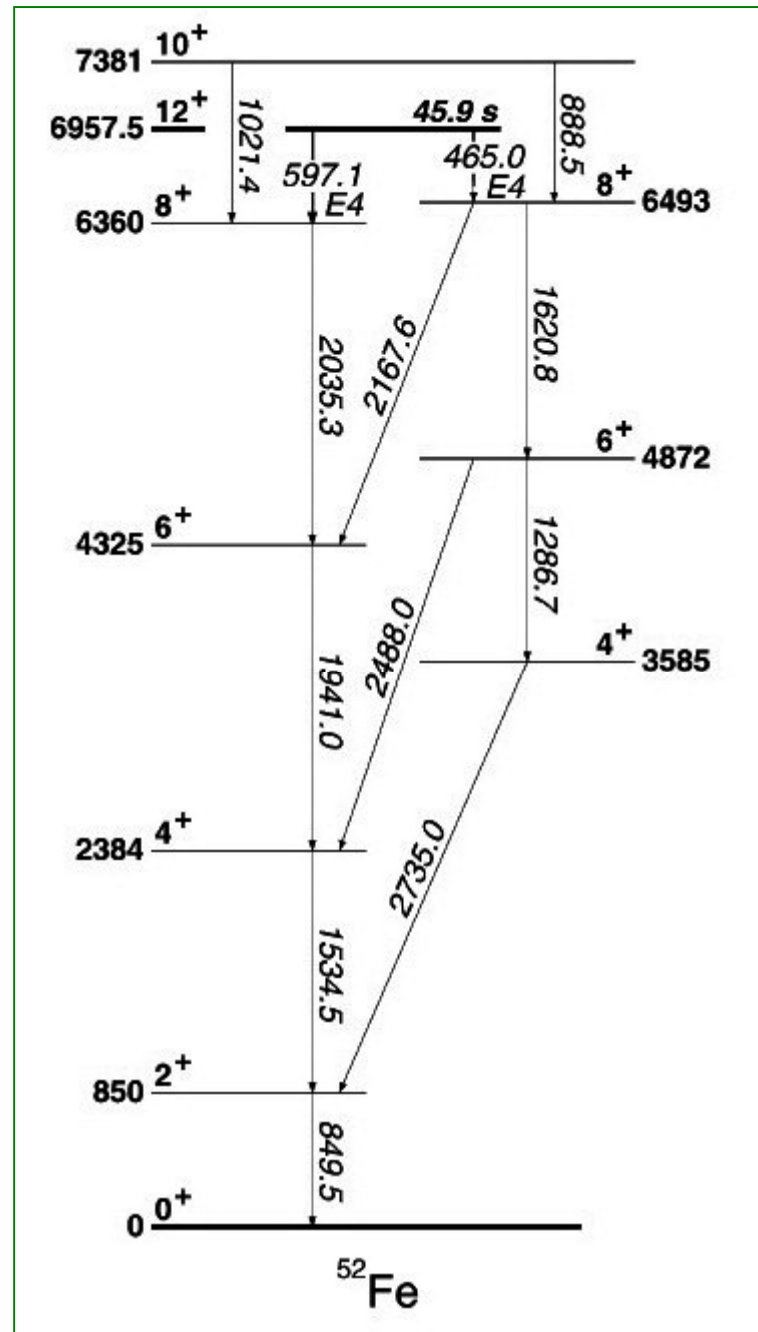
Physics Letters B 619 (2005) 88–94

PHYSICS LETTERS B

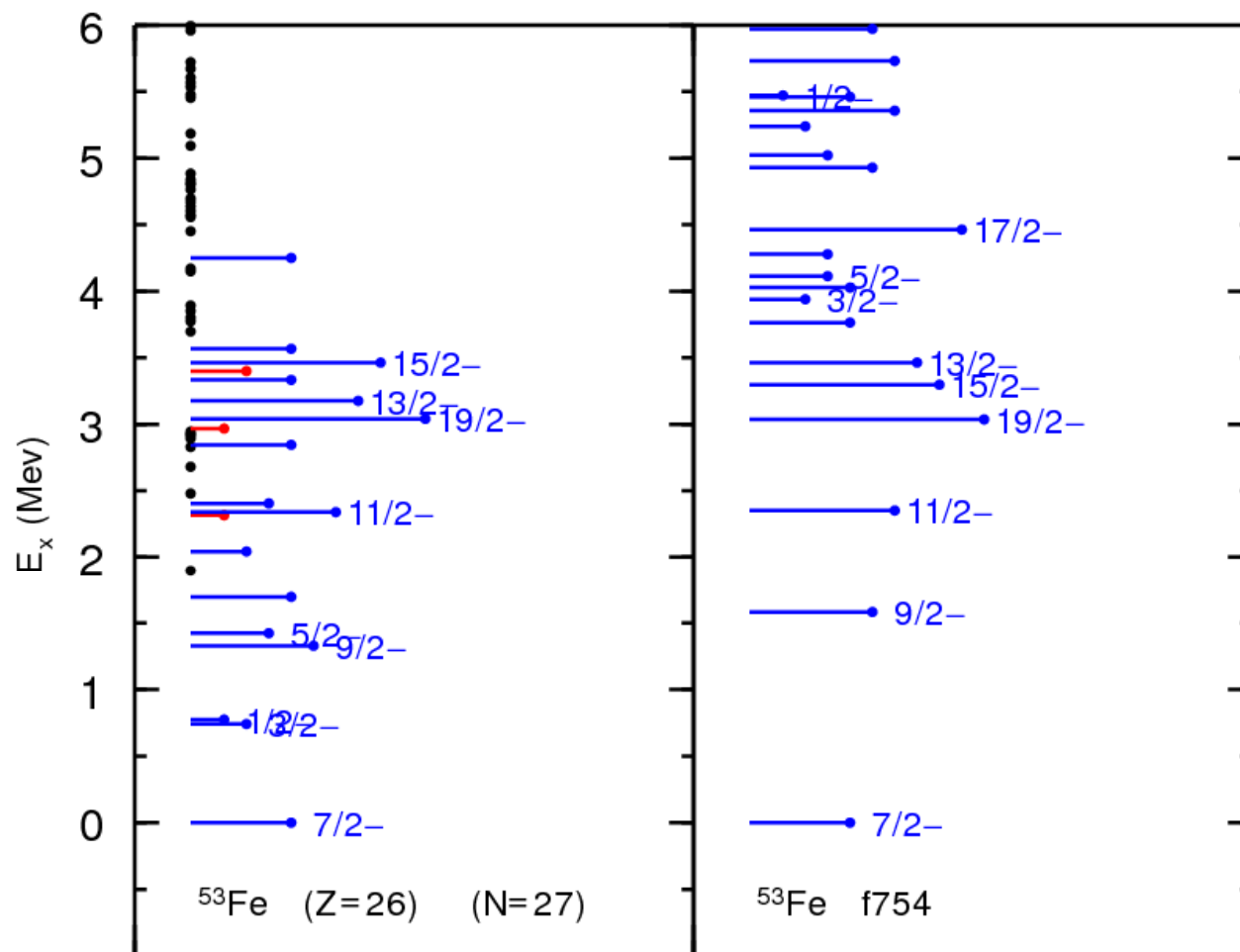
www.elsevier.com/locate/physletb

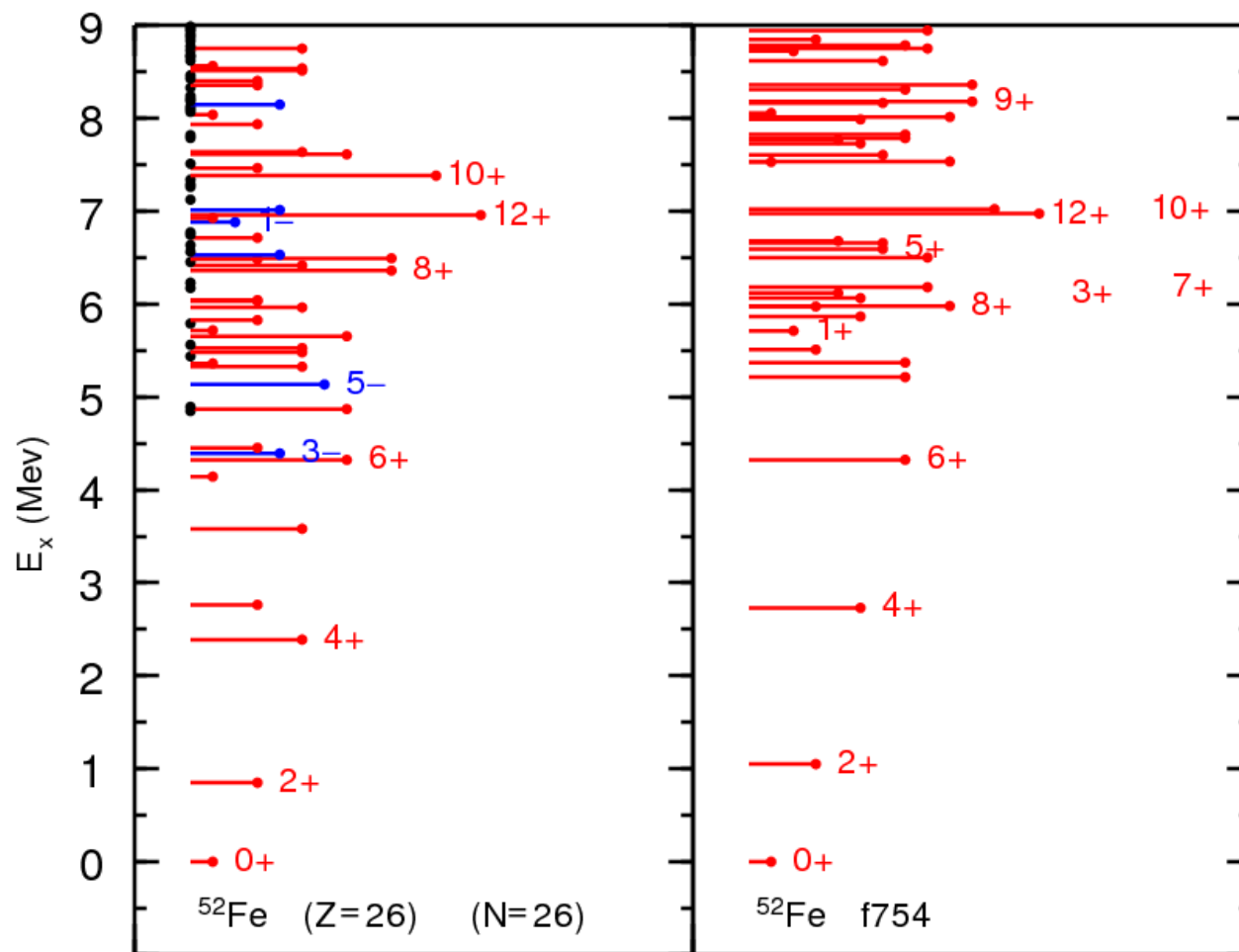
Hindered E4 decay of the 12^+ yrast trap in ^{52}Fe

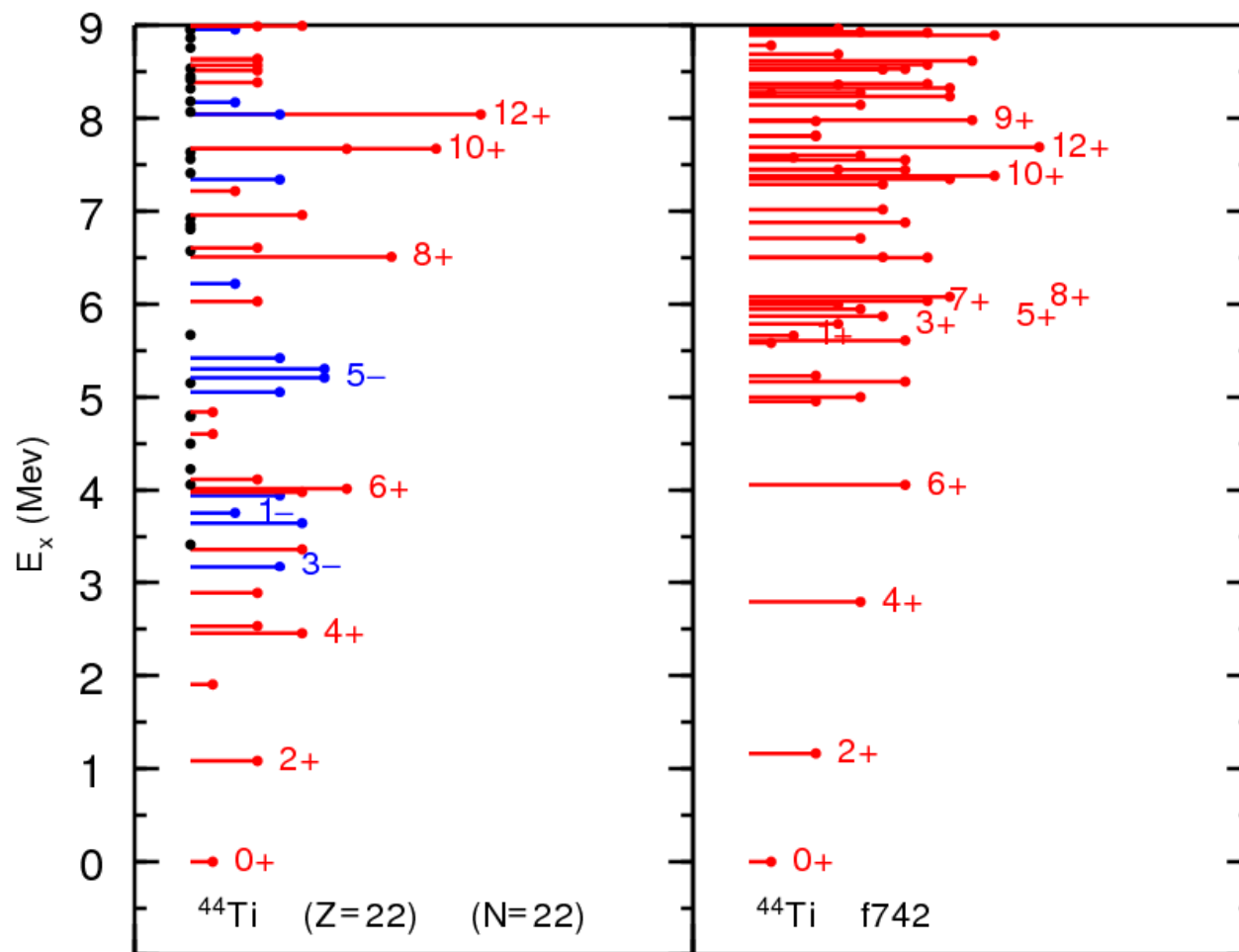
A. Gadea^a, S.M. Lenzi^b, D.R. Napoli^a, M. Axiotis^a, C.A. Ur^{b,c}, G. Martínez-Pinedo^d,
M. Górska^e, E. Roeckl^e, E. Caurier^f, F. Nowacki^f, G. de Angelis^a, L. Batist^g,
R. Borcea^e, F. Brandolini^b, D. Cano-Ott^h, J. Döring^e, C. Fahlanderⁱ, E. Farnea^b,
H. Grawe^e, M. Hellströmⁱ, Z. Janas^{e,j}, R. Kirchner^e, M. La Commara^e,
C. Mazzocchi^{e,k}, E. Nácher^h, C. Plettner^l, A. Płochocki^j, B. Rubio^h, K. Schmidt^e,
R. Schwengner^l, J.L. Tain^h, J. Żylicz^j

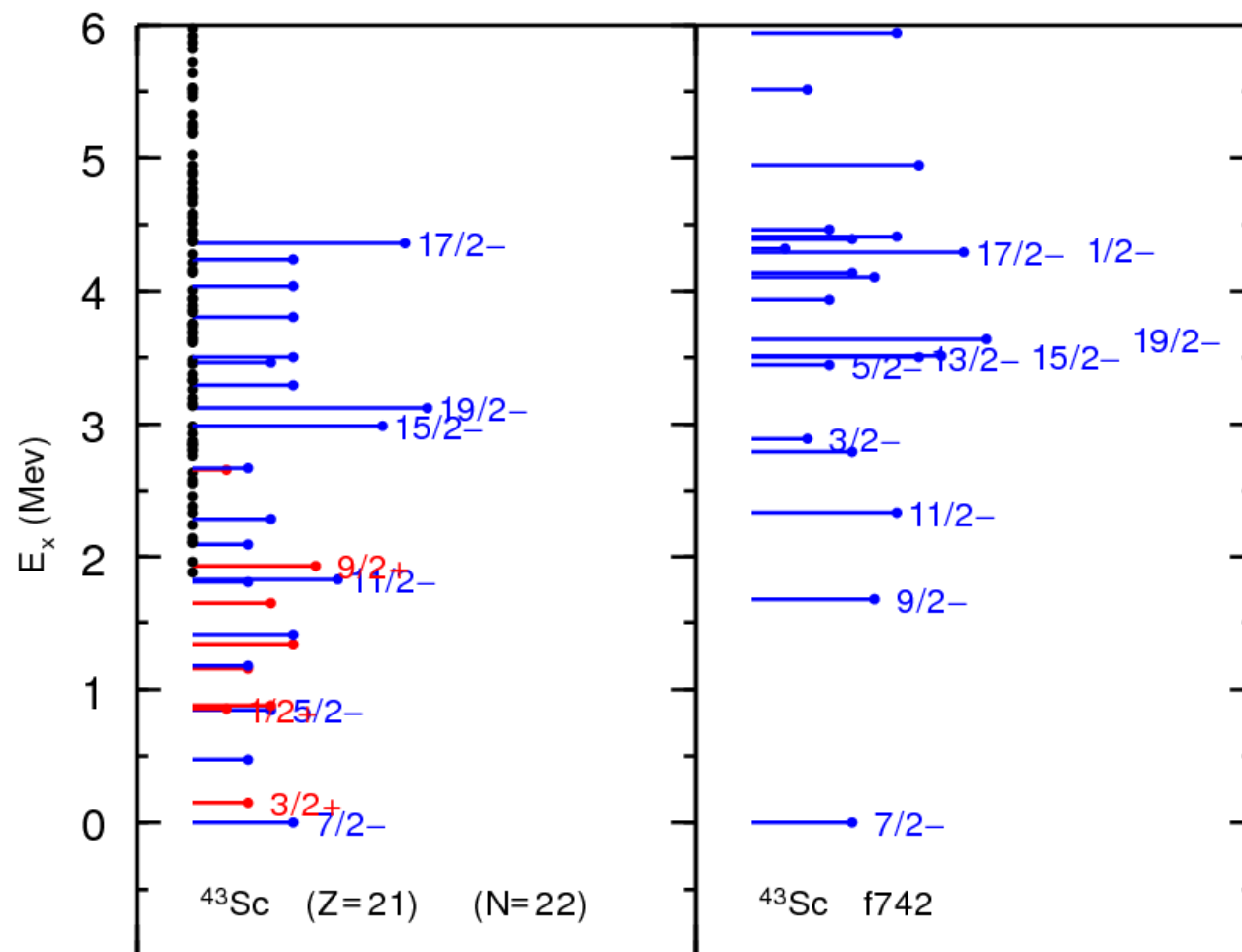


Alex Brown, May 19, 2010









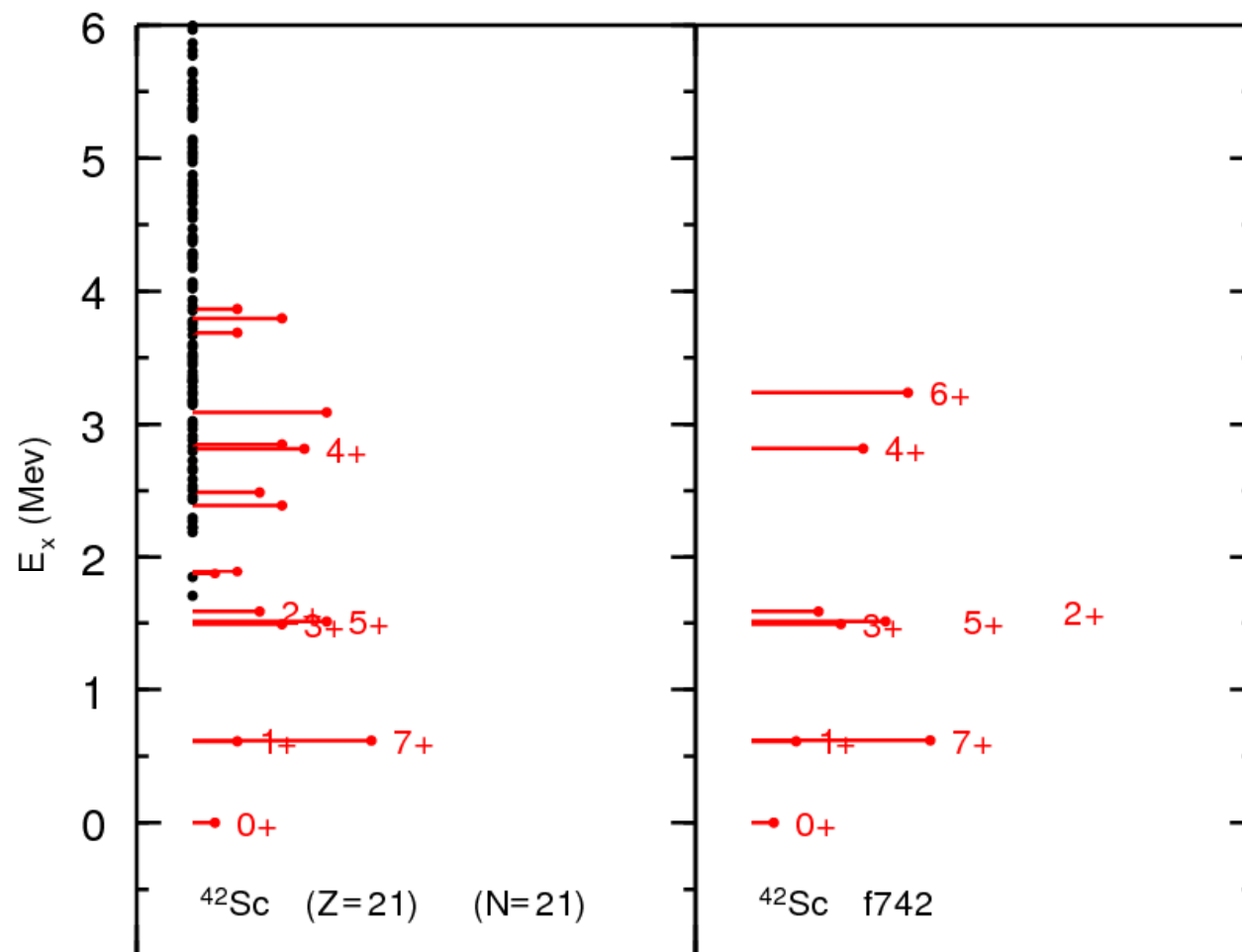
Why is there an isomer for holes and not for particles?
The energy difference can be expressed in terms of $f_{7/2}$
two-body matrix elements

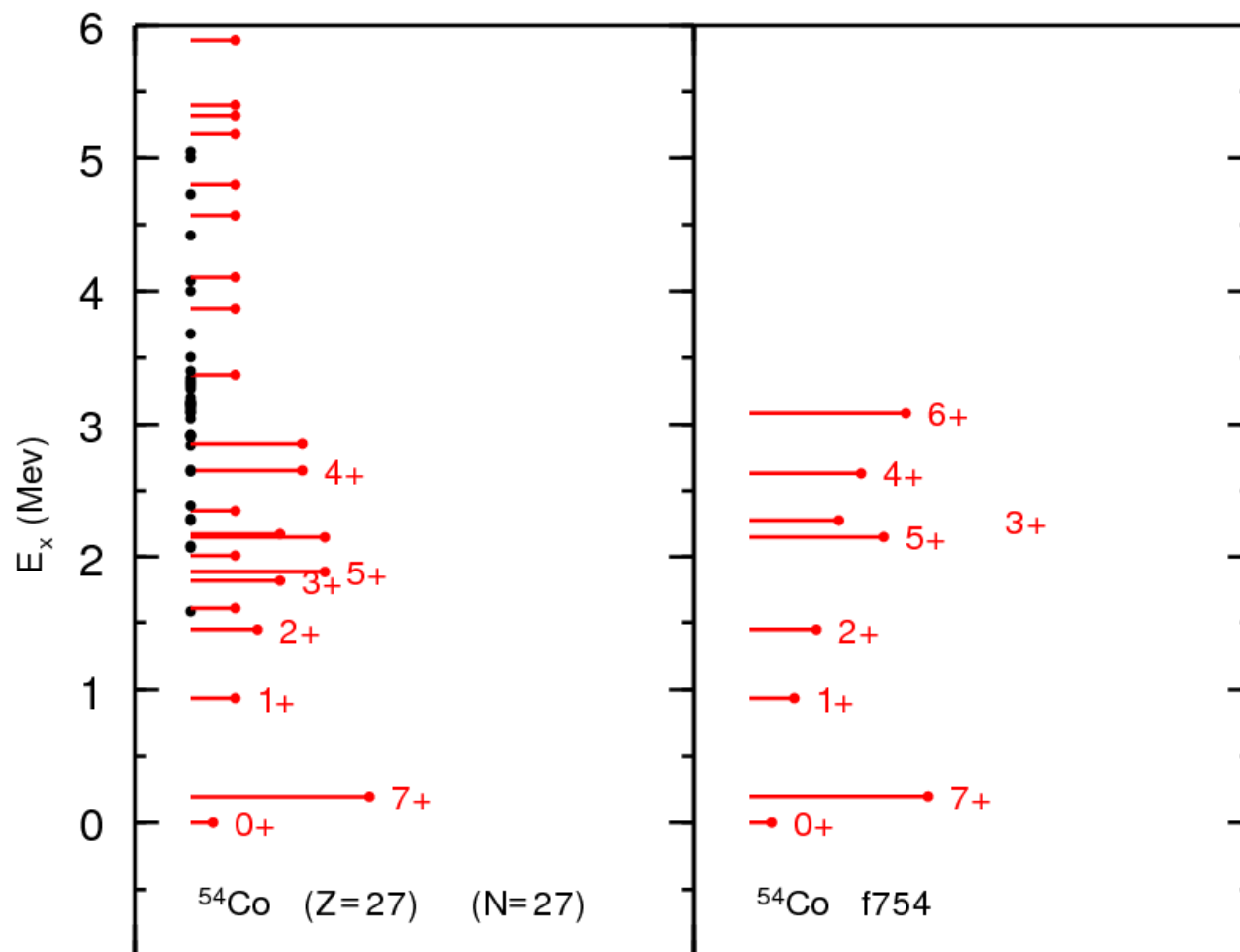
$$V_{JT} = \langle f_{7/2}, f_{7/2}, J, T | V | f_{7/2}, f_{7/2}, J, T \rangle$$

$$E(12^+) - E(10^+) =$$

$$+0.35 V_{70} - 0.11 V_{50} - 0.24 V_{30}$$

$$+1.47 V_{61} - 1.47 V_{41}$$



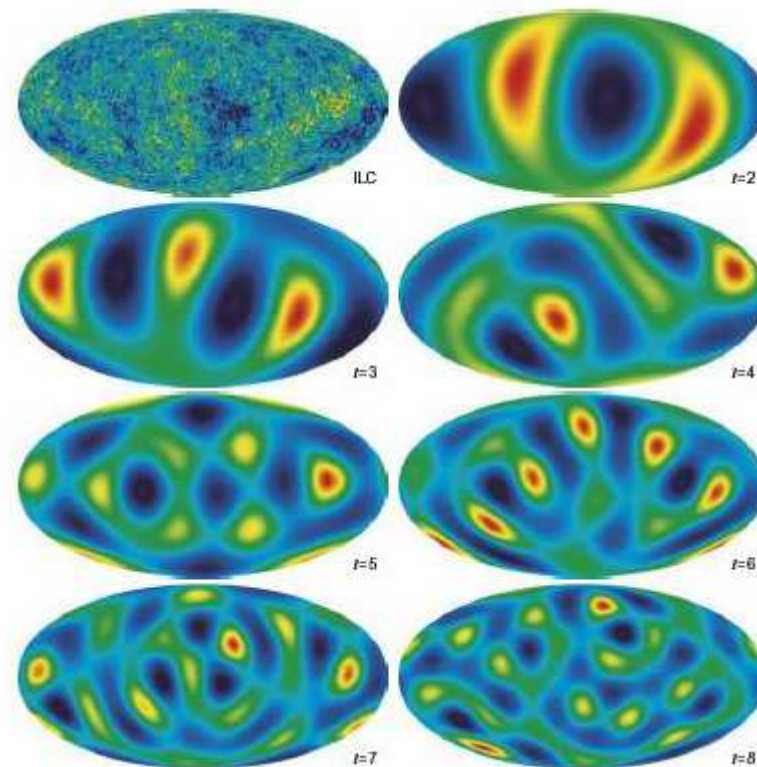


E6 decay - from the $19/2^-$ ^{53}Fe isomer

E2 $2^2 = 4$ tetrapole

E4 $2^4 = 16$ hexadecapole

E6 $2^6 = 64$ hexacontatetrapole



^{53}Fe E6 decay $19/2^-$ to $7/2^-$

$$B(E6)_{exp} = 0.26(4) \cdot 10^6 \text{e}^2 \text{fm}^{12}$$

$f_{7/2}$ model space with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$, $e_p = 1.5$
and $e_n = 0.5$

$$B(E6) = 6.03 \cdot 10^6 \text{e}^2 \text{fm}^{12}$$

$f_{7/2}$ model space with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$, $e_p = 1$
and $e_n = 0$

$$B(E6) = 2.62 \cdot 10^6 \text{e}^2 \text{fm}^{12}$$

$$B(E6) = \frac{M^2}{2J_i + 1}$$

$$M_{exp} = 2.3 \cdot 10^3 \text{efm}^6$$

$f_{7/2}$ model space with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$, $e_p = 1$
and $e_n = 0$

$$M = 7.2 \cdot 10^3 \text{efm}^6$$

The $E6$ operator is

$$O(E6) = Y^{(6)}(\hat{r}_q) r_q^6 e_q$$

summed over all protons ($q = p$) and neutrons ($q = n$).

Where does this factor of three come from?

Isomer is “pure” compared to ground state in terms of
mixing beyond $f_{7/2}$?

The radial integral $\langle f_{7/2} | r^6 | f_{7/2} \rangle$ is uncertain?

$$M = A_p e_p + A_n e_n$$

with A_p and A_n in units of 10^3 e fm^6 $f_{7/2}$ model space
with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$,

$$A_p = 7.25$$

$$A_n = 0.21$$

$$M_{exp} = 2.3$$

BAB notes from around 1980

$\overline{(B|E|V)}$

$$\langle 11/2 \parallel E4 \parallel 19/2 \rangle \times \sqrt{28}$$

$$\begin{array}{l} \delta e \times \Delta E \\ -0.846 \quad \sqrt{12} \quad \left[0.794 \left\{ \begin{array}{l} 2 \quad 11/2 \quad 7/2 \\ 19/2 \quad 6 \quad 4 \end{array} \right\} \langle 2 \parallel E4 \parallel 6 \rangle - 0.738 \right. \\ 0.655 \\ 0.323 \quad + 0.561 \left\{ \begin{array}{l} 4 \quad 11/2 \quad 7/2 \\ 19/2 \quad 6 \quad 4 \end{array} \right\} \langle 4 \parallel E4 \parallel 6 \rangle - 0.270 \\ 0.402 \\ 0.090 \quad + 0.234 \left\{ \begin{array}{l} 6 \quad 11/2 \quad 7/2 \\ 19/2 \quad 6 \quad 4 \end{array} \right\} \langle 6 \parallel E4 \parallel 6 \rangle + 0.006 \\ 2.627 \quad + 0.234 \left\{ \begin{array}{l} 7/2 \quad 11/2 \quad 6 \\ 19/2 \quad 7/2 \quad 4 \end{array} \right\} \langle 7/2 \parallel E4 \parallel 7/2 \rangle \end{array}$$

$$\times 14.393 \rightarrow (1.01 A^{1/3})^2$$

$$= -49.86 [-1.002 e_p + 0.0949 e_n]$$

1975 considered one-nucleon excited to $f_{5/2}$

PHYSICAL REVIEW C

VOLUME 11, NUMBER 5

MAY 1975

$E6$ transition in $^{53}\text{Fe}^\dagger$

D. H. Gloeckner* and R. D. Lawson

Argonne National Laboratory, Argonne, Illinois 60439

(Received 24 February 1975)

The $\frac{19}{2}^- \rightarrow \frac{7}{2}^-$ $E6$ transition in ^{53}Fe is calculated in a model including all basis states of the configurations $(f_{7/2})^{13}_{IT}$ and $[(f_{7/2})^{12}_{IT'} \times f_{5/2}]_{IT}$. Several interactions, which yield the observed amount of $f_{5/2}$ configuration mixing, have been considered. In all cases an effective charge $\delta \cong -0.4$ is needed to fit experiment (where $e_p = 1 + \delta$, $e_n = \delta$).

Thanks to Bill Rae with NuShellX and many years work on the effective Hamiltonian, the full pf shell can now be done.

$$0f_{7/2} \ D(M = 7/2) = 16$$

$$0f_{7/2} \ D(J = 7/2) = 4$$

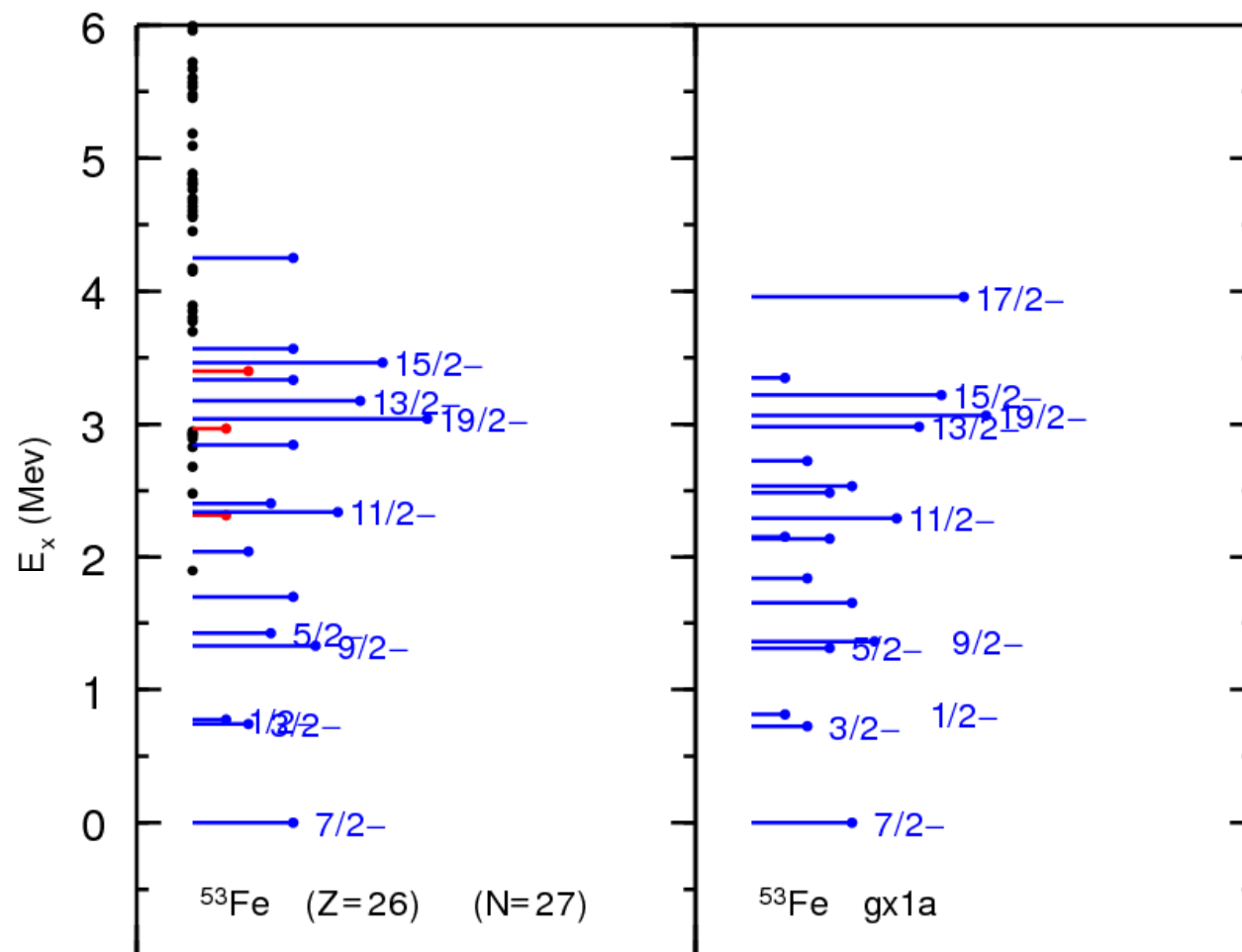
$$0f_{7/2} \ D(J = 19/2) = 1$$

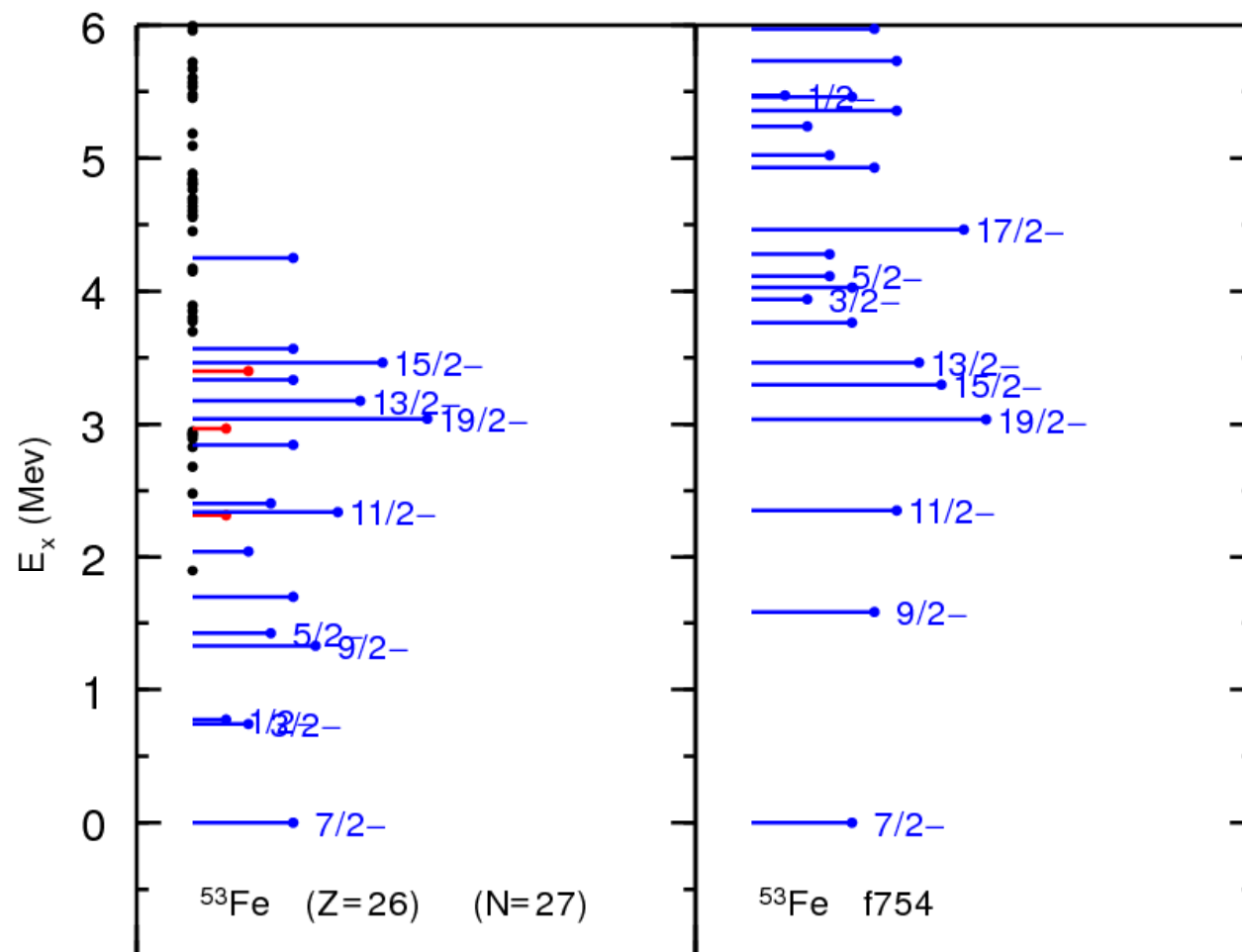
$$pf \ D(M = 7/2) = 177,805,002$$

$$pf \ D(J = 7/2) = 21,131,892$$

$$pf \ D(J = 19/2) = 14,333,584$$

model space	J	$n(f_{7/2})$	percent $(f_{7/2})^{13}$
$f_{7/2}$	7/2	13	100
pf	7/2	12.0	54
$f_{7/2}$	19/2	13	100
pf	19/2	12.3	62





Results for the $E6$ matrix elements obtained with various pf shell Hamiltonians with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$.

Hamiltonian	A_p $10^3 \text{ (e fm}^6\text{)}$	A_n $10^3 \text{ (e fm}^6\text{)}$
$f_{7/2}$	7.25	0.21
FPD6	3.76	0.27
KB3G	4.66	0.36
GPFX1A	4.40	0.22
experiment	$M = 2.3$	

For FPD6 we would conclude for the effective charge $e_p = 0.60$ or with $e_p = 1 + \delta e_p$, $\delta e_p = -0.4$.

2005 search for E4 gamma in ^{52}Fe – found



Available online at www.sciencedirect.com

SCIENCE @ DIRECT®

Physics Letters B 619 (2005) 88–94

PHYSICS LETTERS B

www.elsevier.com/locate/physletb

Hindered E4 decay of the 12^+ yrast trap in ^{52}Fe

A. Gadea^a, S.M. Lenzi^b, D.R. Napoli^a, M. Axiotis^a, C.A. Ur^{b,c}, G. Martínez-Pinedo^d,
M. Górska^e, E. Roeckl^e, E. Caurier^f, F. Nowacki^f, G. de Angelis^a, L. Batist^g,
R. Borcea^e, F. Brandolini^b, D. Cano-Ott^h, J. Döring^e, C. Fahlanderⁱ, E. Farnea^b,
H. Grawe^e, M. Hellströmⁱ, Z. Janas^{e,j}, R. Kirchner^e, M. La Commara^e,
C. Mazzocchi^{e,k}, E. Nácher^h, C. Plettner^l, A. Płochocki^j, B. Rubio^h, K. Schmidt^e,
R. Schwengner^l, J.L. Tain^h, J. Żylicz^j

$$e_p = 1.5 \text{ and } e_n = 0.5$$

$J_i \rightarrow J_f$		$B(E4) \text{ (W.u.)}$			
		Exp	FPD6	KB3G	GXPFI
^{52}Fe	$12^+ \rightarrow 8_1^+$	$4.6(17) \times 10^{-4}$	2.4×10^{-3}	3.3×10^{-1}	6.5×10^{-2}
^{52}Fe	$12^+ \rightarrow 8_2^+$	$3.5(13) \times 10^{-3}$	4.7×10^{-3}	2.6×10^{-2}	2.3×10^{-2}
^{44}Sc	$6^+ \rightarrow 2^+$	1.42	1.96	1.79	1.65
^{46}Ti	$4^+ \rightarrow 0^+$	1.6	10.7	7.9	7.39
^{52}Mn	$2^+ \rightarrow 6^+$	0.138	0.272	0.422	0.728
^{53}Fe	$\frac{19}{2}^- \rightarrow \frac{11}{2}^-$	0.256	0.151	1.23	0.84
^{54}Fe	$10^+ \rightarrow 6^+$	0.79	1.80	0.98	1.25

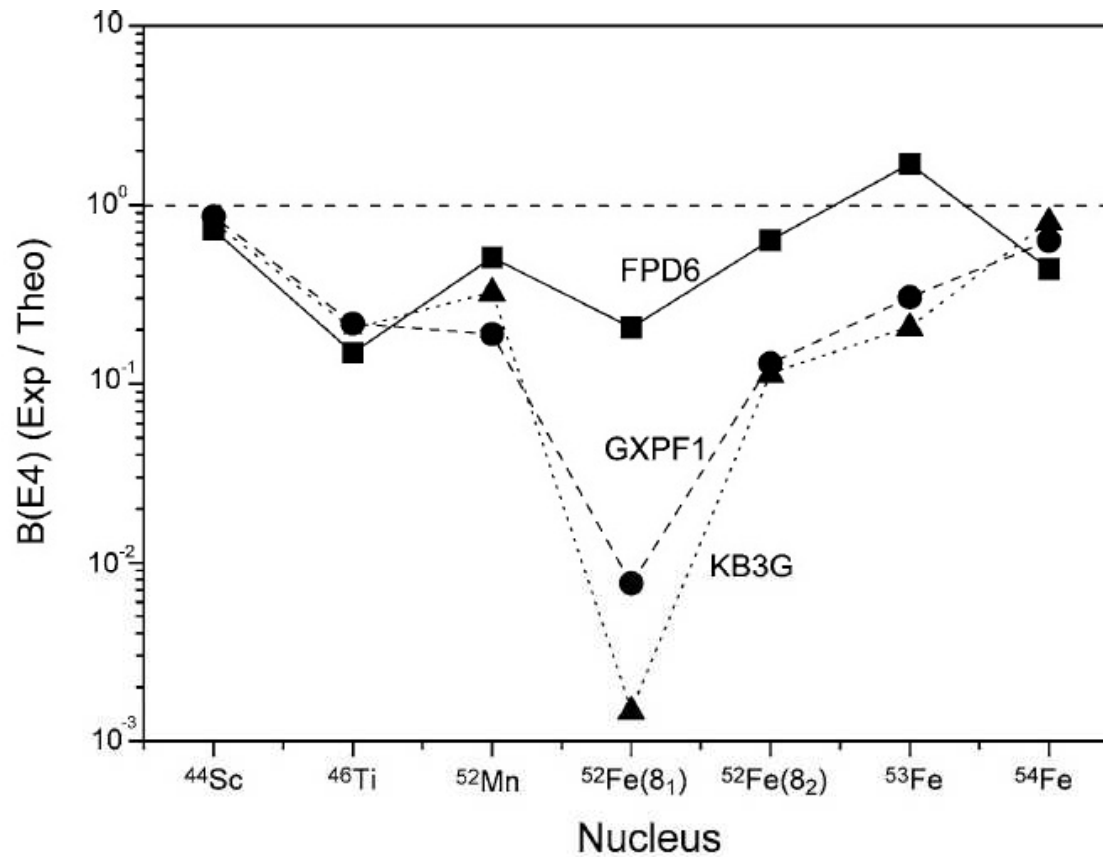


Fig. 4. Ratio between experimental and theoretical $B(E4)$ values for nuclei in the $f_{7/2}$ shell. Results obtained by using the FPD6, GXPF1 and KB3G interactions are shown by squares (full line), full circles (dashed-line) and triangles (dotted-line), respectively. See Table 2 for details.

Results for the $E6$ matrix elements obtained with various radial wavefunctions for GPFX1A.

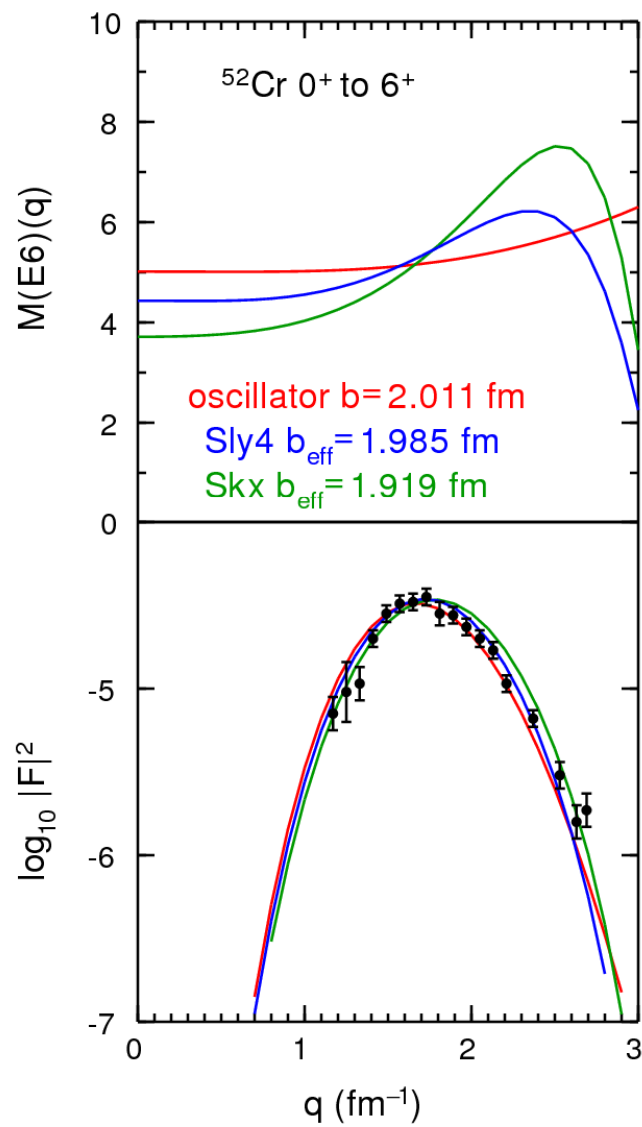
Radial	A_p $10^3 \text{ (e fm}^6\text{)}$	A_n $10^3 \text{ (e fm}^6\text{)}$
$\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$	4.66	0.27
Skx	3.23	0.15
SLy4	3.73	0.18
experiment	$M = 2.3$	



Alex Brown, May 19, 2010

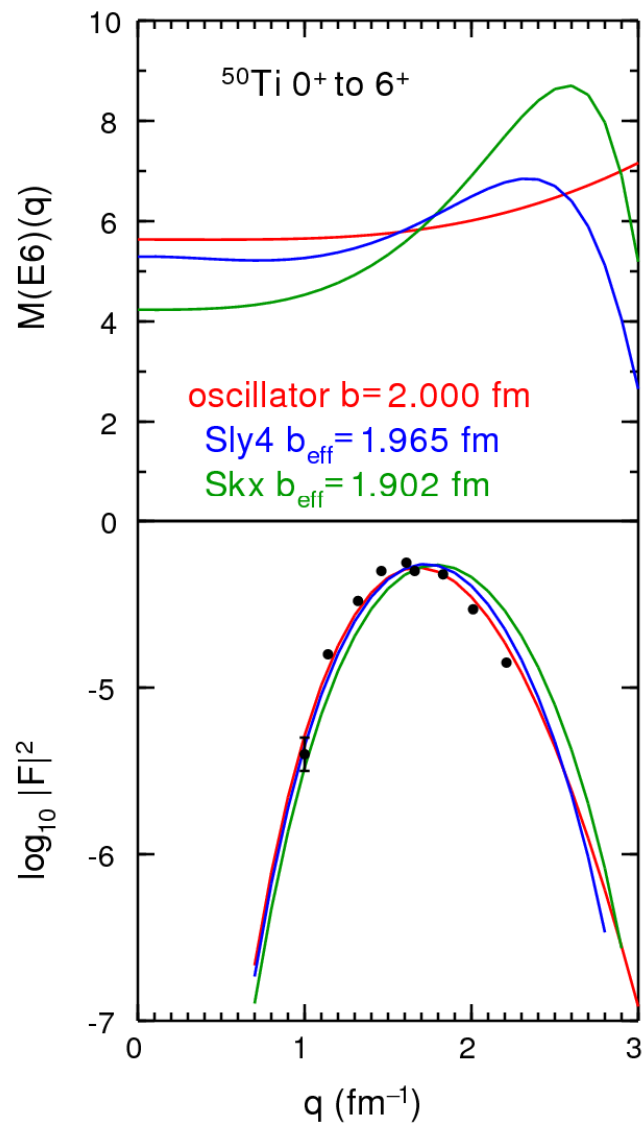
	E6 transition	A_p $10^3 \text{ (e fm}^6\text{)}$	A_n $10^3 \text{ (e fm}^6\text{)}$
^{53}Fe	$19/2^- \rightarrow 7/2^-$	4.40	0.22
^{52}Cr	$0^+ \rightarrow 6^+$	5.01	1.51
^{50}Ti	$0^+ \rightarrow 6^+$	5.63	1.62
^{58}Ni	$0^+ \rightarrow 6^+(2)$	6.42	7.25
^{58}Ni	$0^+ \rightarrow 6^+(3)$	2.98	-3.50

1983 $^{52}\text{Cr}(e,e')$



$$e_p = 1 \text{ and } e_n = 0$$

1988 $^{50}\text{Ti}(e,e')$



$$e_p = 1 \text{ and } e_n = 0$$

Longitudinal form factor for $E6(C6)$ in the oscillator model ($L = 6$, b is the oscillator length)

$$F(q) \approx (qb)^L \exp[-(bq)^2/2]$$

has a maximum at

$$q_{max} = \sqrt{2L/b^2}$$

and since

$$q_{max}b = \sqrt{2L}$$

the value at the maximum is independent of b

Isoscalar Character of the $J^\pi = 6^+$, $E_x = 5.125$ MeV State in ^{58}Ni

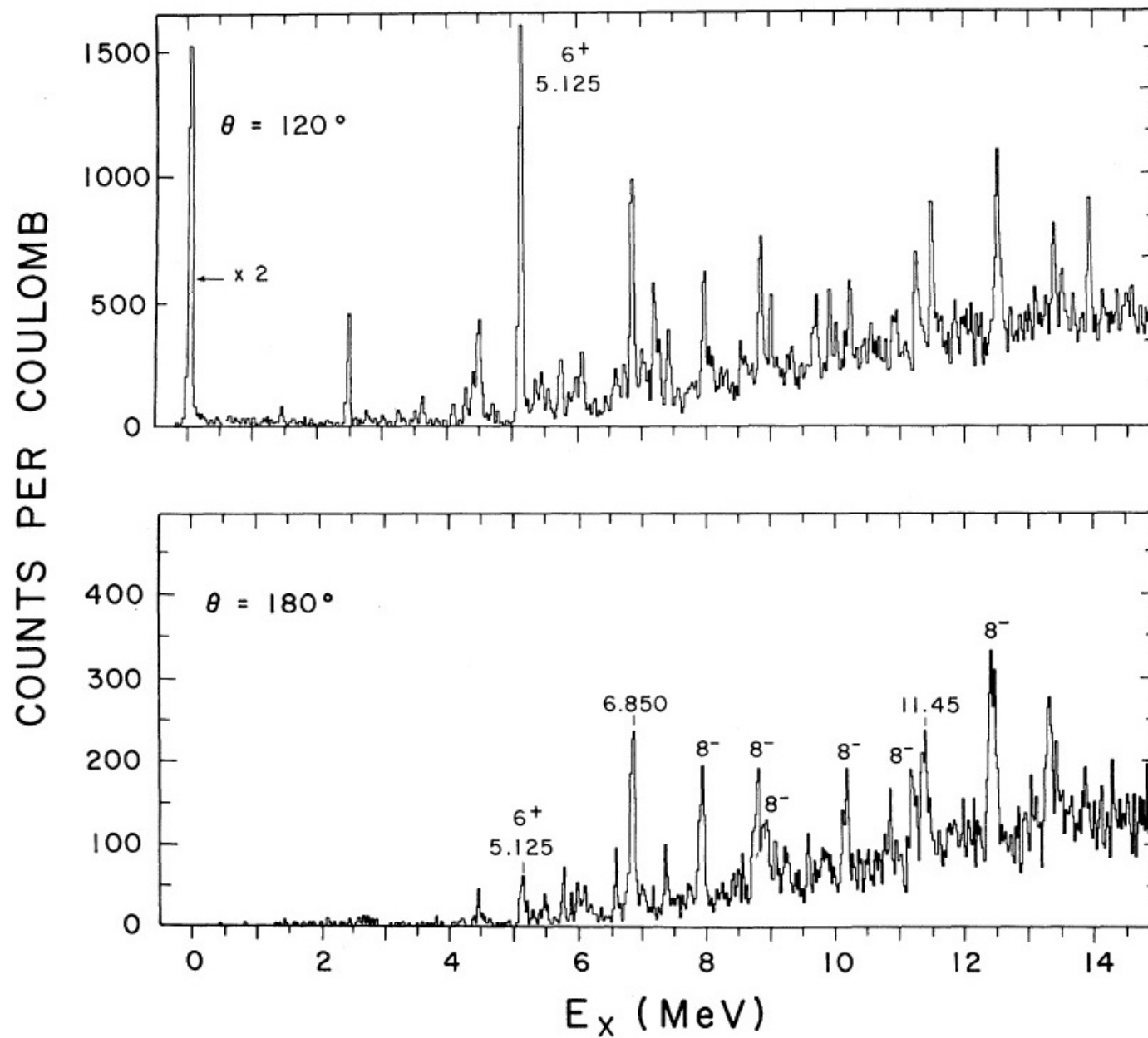
R. A. Lindgren, J. B. Franz, W. J. Gerace, R. S. Hicks, A. Hotta,^(a) D. Huse,
G. A. Peterson, and R. C. York

Department of Physics and Astronomy, University of Massachusetts, Amherst, Massachusetts 01003

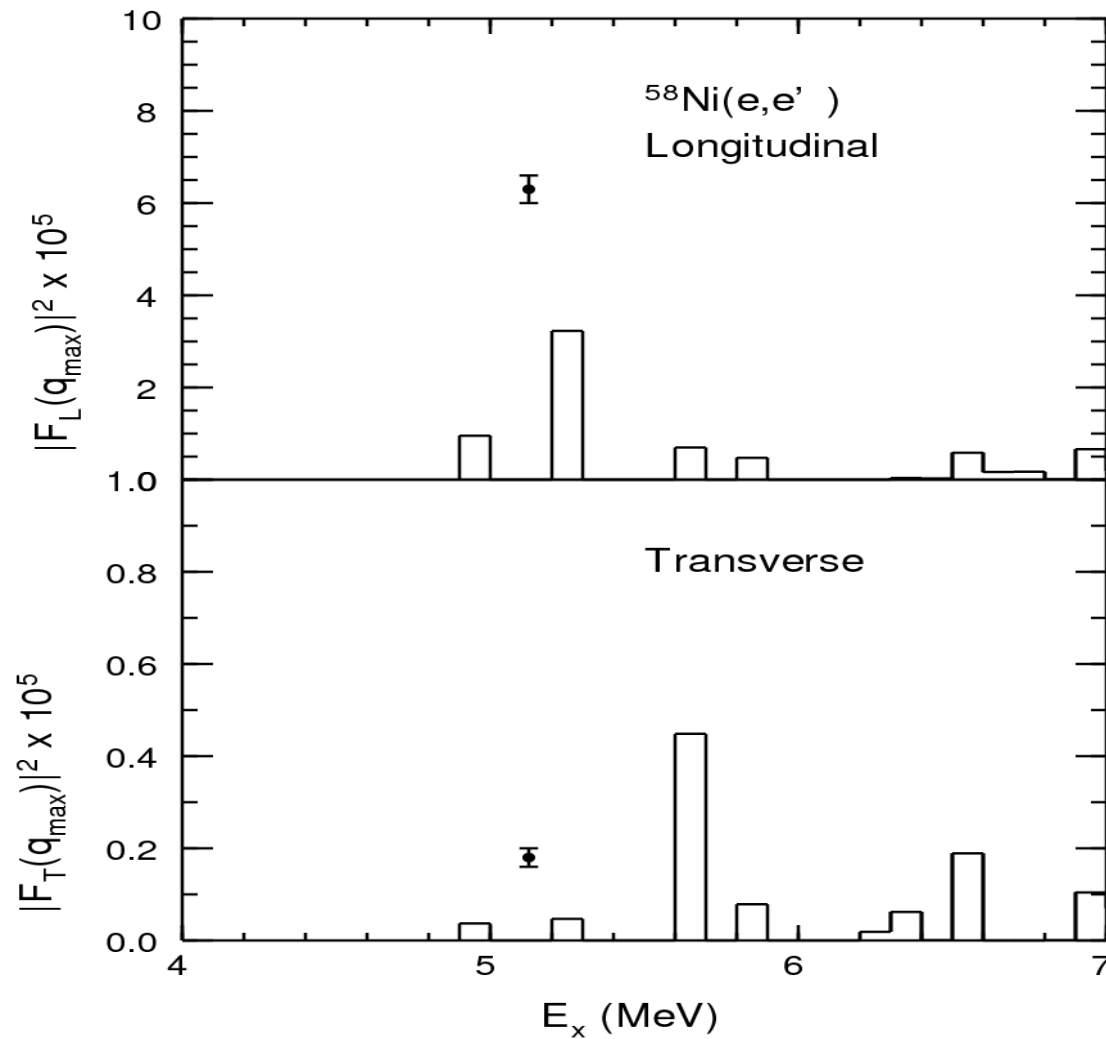
and

C. F. Williamson and S. Kowalski

1979 $^{58}\text{Ni}(e,e')$



The main component for the E6 excitation in ^{58}Ni is
 $(f_{7/2})^{16}(p_{3/2})^2(0^+) \rightarrow (f_{7/2})^{15}(p_{3/2})^2, f_{5/2}(6^+)$
 e.g. an $f_{7/2}$ to $f_{5/2}$ transition



own, May 19, 2010

Core polarization charge for $E6$ transition

Hiroyuki Sagawa*

L	δe_p			δe_η		
	2	4	6	2	4	6
Gillet	0.095	0.114	0.103	0.457	0.428	0.212
G matrix	0.154	0.115	0.076	0.428	0.363	0.267
Serber	0.257	0.191	0.126	0.514	0.382	0.253
Wigner	0.483	0.067	-0.138	0.664	0.299	0.076
Rosenfeld	0.079	0.156	0.164	0.357	0.402	0.351
ATO	0.289	0.040	-0.083	0.462	0.344	0.227
Schematic	0.19	0.18	-0.06	0.81	0.82	0.52
Exp.	0.06 ± 0.07		-0.3 ± 0.1	0.57 ± 0.03		

Sagawa – theory summary

	δe_p	δe_n	$\delta e_p + \delta e_n$	$\delta e_p - \delta e_n$
E2	0.19	0.81	1.00	-0.62
E4	0.18	0.82	1.00	-0.64
E6	-0.06	0.52	0.46	-0.58

experimental summary

	δe_p	δe_n	$\delta e_p + \delta e_n$	$\delta e_p - \delta e_n$
E2	0.2	0.8	1.0	-0.6
E4			1.0	
E6	-0.2	0.6	0.4	-0.8

$\delta e_p + \delta e_n$ is determined by coupling of the valence nucleon with the L -pole isoscalar ($\Delta T=0$) giant resonance. Attractive particle-hole interaction for $\Delta T=0$ means that the energy of the resonance is lower than $L\hbar\omega$ and that $\delta e_p + \delta e_n > 0$.

$\delta e_p - \delta e_n$ is determined by coupling of the valence nucleon with the L -pole isovector ($\Delta T=1$) giant resonance. Repulsive particle-hole interaction for $\Delta T=1$ means that the energy of the resonance is higher than $L\hbar\omega$ and that $\delta e_p - \delta e_n < 0$.

Effective Charges in the fp Shell

R. du Rietz,¹ J. Ekman,¹ D. Rudolph,¹ C. Fahlander,¹ A. Dewald,² O. Möller,² B. Saha,² M. Axiotis,³ M. A. Bentley,⁴ C. Chandler,⁴ G. de Angelis,³ F. Della Vedova,⁵ A. Gadea,³ G. Hammond,⁴ S. M. Lenzi,⁵ N. Mărginean,³ D. R. Napoli,³ M. Nespolo,⁵ C. Rusu,³ and D. Tonev³

¹*Department of Physics, Lund University, S-22100 Lund, Sweden*

²*Institut für Kernphysik der Universität zu Köln, D-50937 Köln, Germany*

³*Instituto Nazionale di Fisica Nucleare, Laboratori Nazionali di Legnaro, I-35020 Legnaro, Italy*

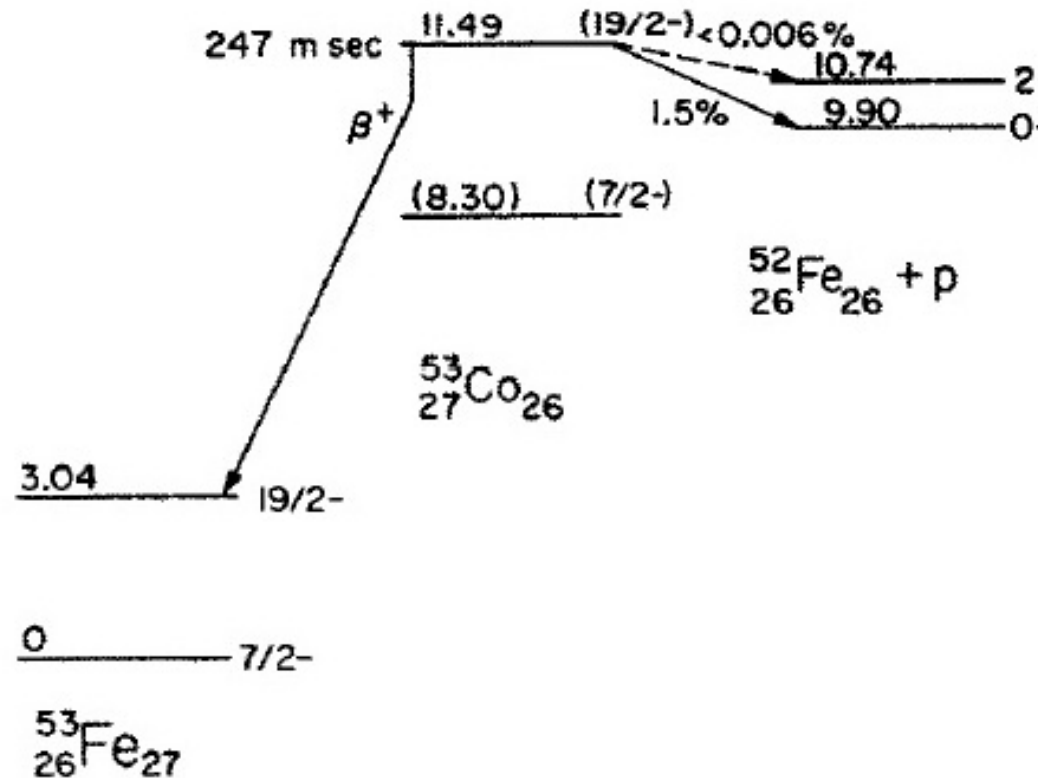
⁴*School of Chemistry and Physics, Keele University, Keele, Staffordshire ST5 5BG, United Kingdom*

⁵*Dipartimento di Fisica dell'Università and INFN, Sezione di Padova, I-35141 Padova, Italy*

(Received 16 August 2004; published 22 November 2004)

Following the heavy-ion fusion-evaporation reaction $^{32}\text{S} + ^{24}\text{Mg}$ at 95 MeV beam energy the lifetimes of analogue states in the $T_z = \pm 1/2$ $A = 51$ mirror nuclei ^{51}Fe and ^{51}Mn have been measured using the Cologne plunger device coupled to the GASP γ -ray spectrometer. The deduced $B(E2; 27/2^- \rightarrow 23/2^-)$ values afford a unique opportunity to probe isoscalar and isovector polarization charges and to derive effective proton and neutron charges, ϵ_p and ϵ_n , in the fp shell. A comparison between the experimental results and several different large-scale shell-model calculations yields $\epsilon_p \sim 1.15e$ and $\epsilon_n \sim 0.80e$.

1970 first proton decay from an isomer - in ^{53}Co



Isomeric proton decay $^{53}\text{Co } 19/2^-$ to $^{52}\text{Fe } 0^+$

$$Q_p = 1.59(3) \text{ MeV}$$

$$T_{1/2} = 17 \text{ s}$$

Must go by $\ell=9$ due to mixing with the $(n, \ell, j^\pi) = (0, 9, 19/2^-)$ orbital

With Oxbash we can do a shell-model calculation in the model space

$$(f_{7/2})^n + (f_{7/2})^{n-1} \ell_{19/2}$$

with an Hamiltonian based on N3LO with V_{lowk}

	S in units of 10^{-9}
exp with $r_0 = 1.2$ fm	57(20)
exp with $r_0 = 1.4$ fm	4(2)
theory	12

Typical two-body interaction matrix element

$$\langle f_{7/2}f_{7/2}6^+ | V | f_{7/2}\ell_{19/2}6^+ \rangle = 50 \text{ keV}$$