

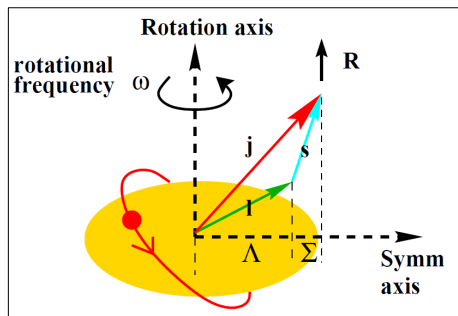
High-K Isomers and Gamma Softness

David M. Cullen.

*School of Physics and Astronomy, University of
Manchester, Manchester, M13 9PL, U.K.*

High-K isomers or Isomeric states

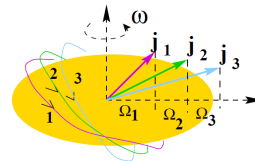
Consider an odd-mass deformed nucleus (Nilsson quantum numbers)



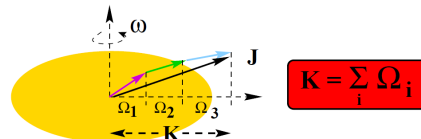
$$\Omega = \Sigma + \Lambda$$

The projection, K is the intrinsic single-particle spin of the band-head state.

Many Unpaired Nucleons



The High-K state



$$K = \sum_i \Omega_i$$

K = Projection of Total Intrinsic angular momentum onto symmetry axis
approx good Q.N. under axial symmetry

K-hindrance and the K-selection rule

$$f_{\nu} = \left(\frac{T_{\frac{1}{2}}^{\gamma}}{T_{\frac{1}{2}}^W} \right)^{\frac{1}{\nu}}$$

$T_{1/2}^{\gamma}$ = Measured Partial half-life
 $T_{1/2}^W$ = Weisskopf half-life

$\lambda(E1) = 1.0 \times 10^{14} A^{\frac{2}{3}} E^3$	$\lambda(M1) = 5.6 \times 10^{13} E^3$
$\lambda(E2) = 7.3 \times 10^7 A^{\frac{4}{3}} E^5$	$\lambda(M2) = 3.5 \times 10^7 A^{\frac{2}{3}} E^5$
$\lambda(E3) = 34 A^2 E^7$	$\lambda(M3) = 16 A^{\frac{4}{3}} E^7$
$\lambda(E4) = 1.1 \times 10^{-5} A^{\frac{8}{3}} E^9$	$\lambda(M4) = 4.5 \times 10^{-6} A^2 E^9$

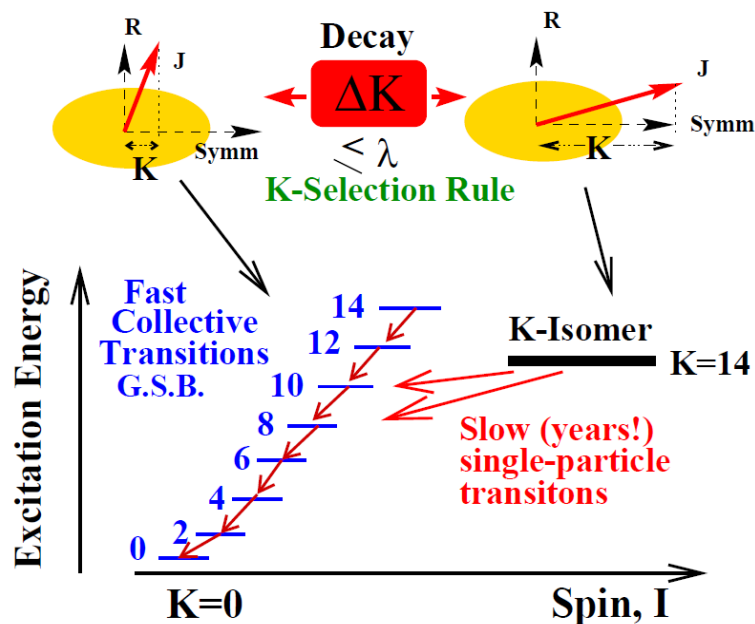
Reduced Hindrance Factor

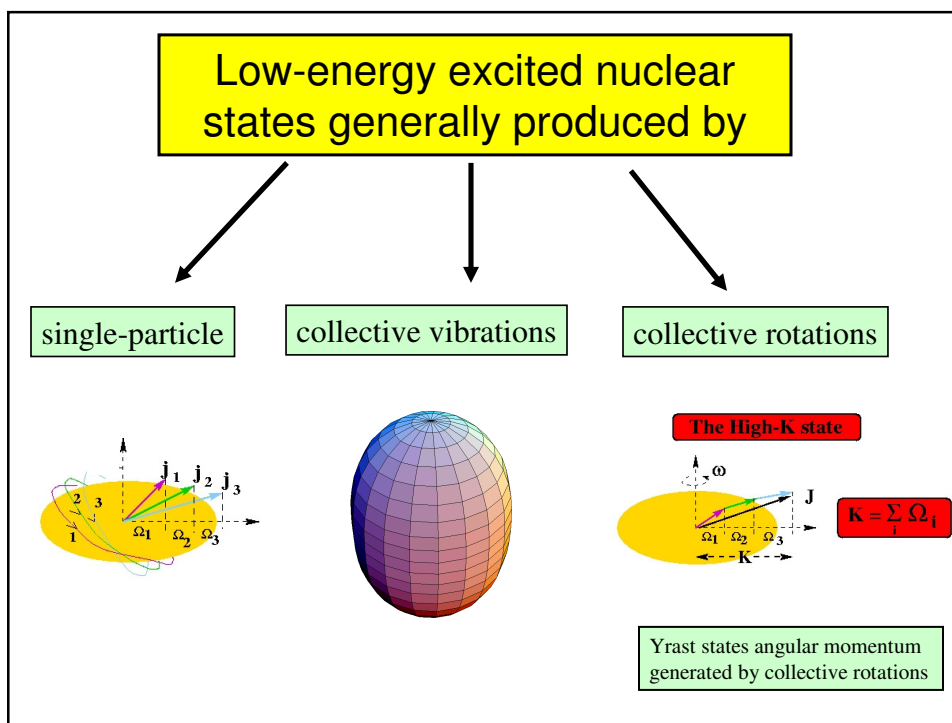
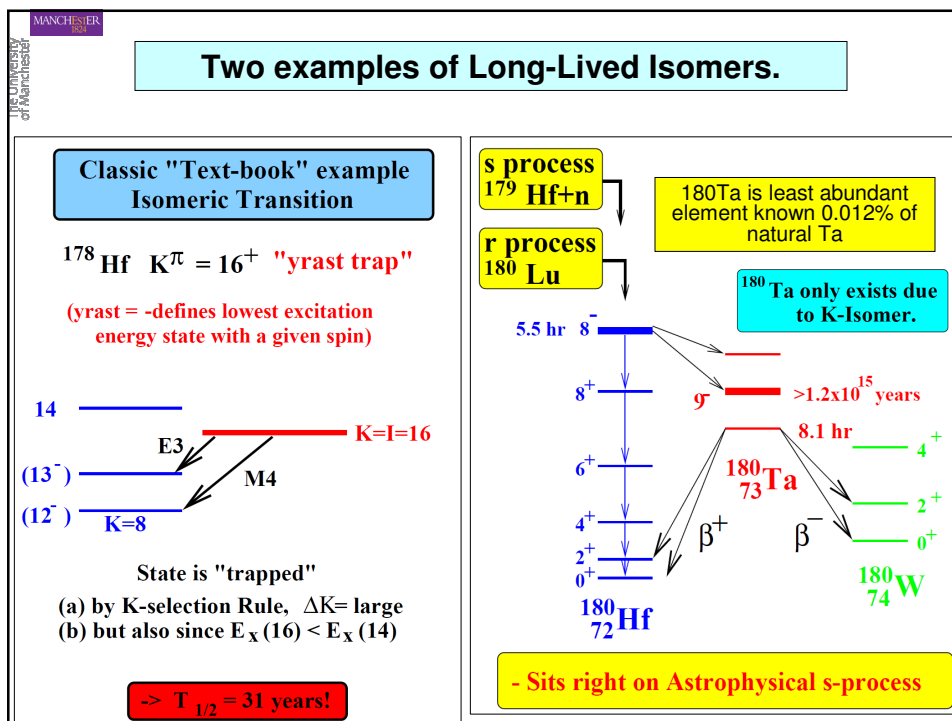
$\nu = \Delta K - \lambda$ λ = transition multipolarity
 ν = degree of K forbiddenness.

The K-Selection Rule:

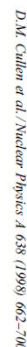
The change in K should be less than or equal to the multipolarity of the transition making the decay, otherwise the transition should be hindered by 100 per degree of K forbiddenness, ν (Lobner 1965/6)

K-hindrance and the K-selection rule





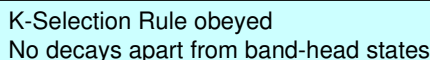
Collective rotation of deformed high-K structures generates angular momentum, $I(I+1) \hbar^2/2J$
→ strongly-coupled rotational bands result

$$0 \rightarrow AB \rightarrow AB_{pB_p}$$


Angular momentum of Yrast states usually dominated by Collective Rotation

K-Selection Rule implies that Isomer decays follow stepwise path, minimising $\Delta K - \lambda$ at each step

PHYSICAL REVIEW C 60 064301



Circumvention of K-selection rule in isomer decay

3 main methods where K-Selection Rule is known not to be obeyed:

1. **Coriolis Mixing** (^{172}Hf , T-Bands, Band Crossings...)
2. **Density of States** arguments (K-isomers can be highly non-yrast and decay because of very high-level density.)
3. **Gamma-Softness** (^{182}Os), loss of axial symmetry and gamma tunnelling.

1. Coriolis mixing (^{172}Hf , ^{138}Gd ,... T-Bands, Band Crossings...)

Coriolis interaction **mixes** states differing in K by $\Delta K = \pm 1$

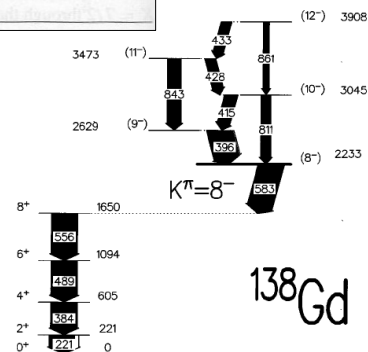
Table 9.3 Theoretical values $\langle K | j_{\perp} | K + 1 \rangle^*$

	$9/2^- [505]$	$7/2^- [503]$	$3/2^- [512]$	$1/2^- [510]$	$5/2^- [512]$	$1/2^- [521]$	$7/2^- [514]$
$9/2^- [505]$		-0.973					2.847
$7/2^- [503]$	-0.973				2.858		
$3/2^- [512]$				0.951	0.045	2.546	
$1/2^- [510]$			0.951			-2.541	
$5/2^- [512]$		2.858	0.045				-1.151
$1/2^- [521]$			2.546	-2.541			
$7/2^- [514]$	2.847				-1.151		

High-K isomeric state with e.g. $K=8$ can **mix** with ground-state rotational band (expected $K \approx 0$)

Happens especially in the band-crossing region where nucleons are aligning with the rotation axis.

This reduces the effective ΔK for the isomer decay

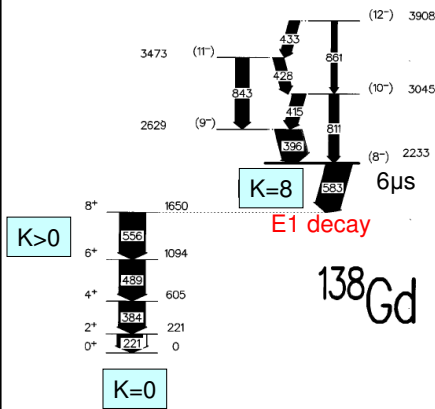


1. Coriolis mixing (^{172}Hf , T-Bands, Band Crossings...)

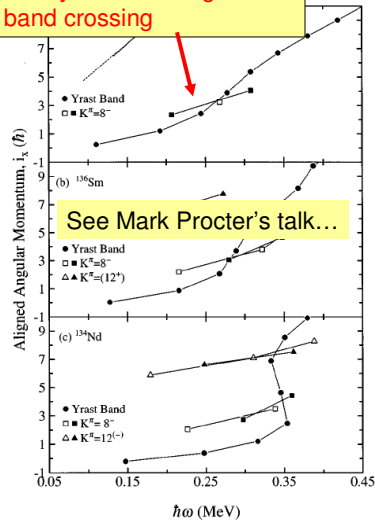
Coriolis force **mixes** states differing in K by $\Delta K=\pm 1$

Identification of the $K^\pi=8^-$ rotational band in ^{138}Gd

D. M. Cullen, N. Anzai, A. J. Boston, P. A. Butler, A. Keenan, E. S. Paul, and H. C. Scraggs
Oliver Lodge Laboratory, Department of Physics, University of Liverpool, Liverpool L69 7ZE, United Kingdom
Phys Rev C58 (98) 846



E1 decay occurs in region of 1st band crossing

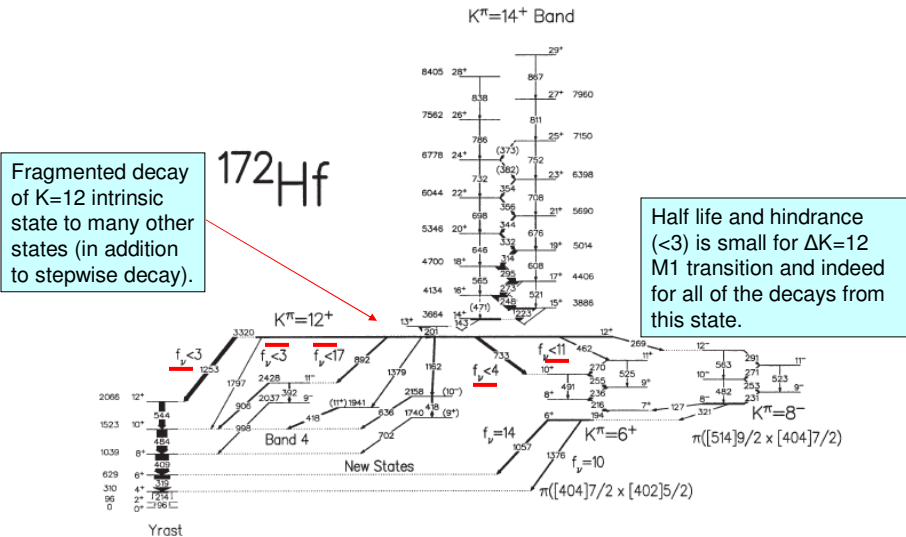


See Mark Procter's talk...

2. Density of states arguments (K-isomers can be highly non-yrast and decay because of very high-level density.)

D.M. Cullen et al./Nuclear Physics A 638 (1998) 662-700

677

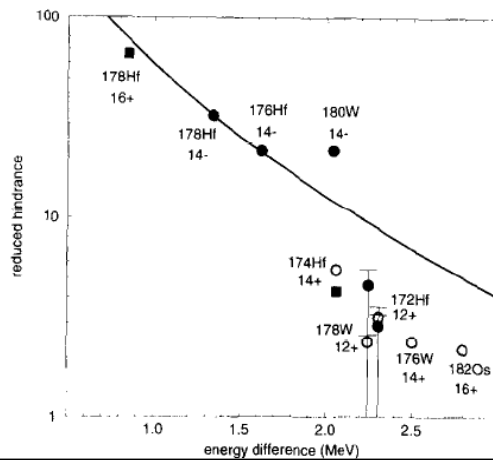


2. Density of states arguments (K-isomers can be highly non-yrast and decay because of very high-level density.)

K-forbidden transitions from multi-quasiparticle states

P.M. Walker^{a,1}, D.M. Cullen^b, C.S. Purry^a, D.E. Appelbe^b, A.P. Byrne^c, G.D. Dracoulis^c,
T. Kibédi^c, F.G. Kondev^{c,2}, I.Y. Lee^d, A.O. Macchiavelli^d, A.T. Reed^b, P.H. Regan^a,
F. Xu^a

Physics Letters B 408 (1997) 42–46

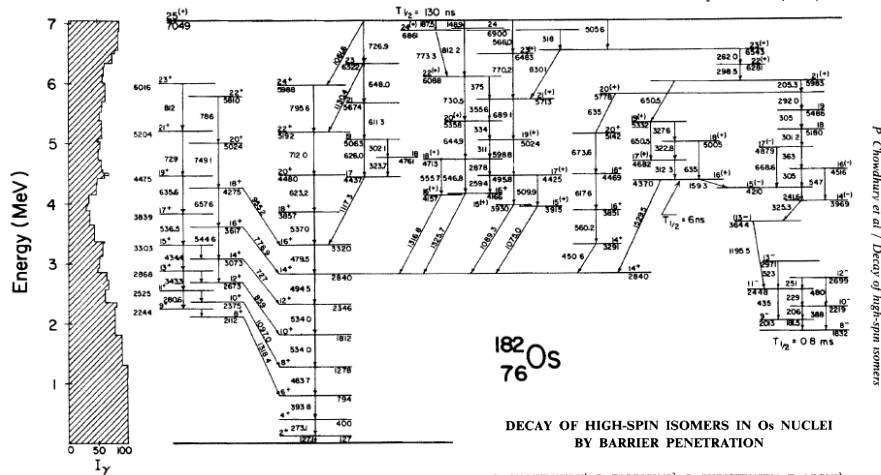


$$f_v = F_v \exp \left[-\frac{3}{\nu} \sqrt{\frac{\pi^2}{6}} g_0 \Delta E \right]$$

Fig. 1. Reduced hindrance, f_v , as a function of energy relative to a rigid rotor, $E_K - E_R$, for $\Delta K \geq 6$, E2 and E3 decays from 4-quasiparticle states. Open circles correspond to E2 decays to $K^\pi = 0^+$ bands, and filled circles correspond to E2, $\Delta K = 6$ decays. The filled squares are for $\Delta K = 8$ decays in ^{178}Hf (E3) and ^{174}Hf (E2). The data points for ^{172}Hf and ^{178}W correspond to half their upper-limit half-lives. The values for the other nuclei have statistical uncertainties that are smaller than the data points. Note that there are two data points for each of ^{172}Hf (12^+), ^{174}Hf (14^+) and ^{178}W (12^+). The line through the data represents a statistical-mixing estimate for $\Delta K = 6$ transitions, normalised to ^{178}Hf (14^-).

3. Gamma-softness (^{182}Os), loss of axial symmetry and gamma tunnelling.

Nuclear Physics A485 (1988) 136–160



Long-Standing Issue:

The $K=25$ isomer in ^{182}Os , decays to the ground-state band ($K \approx 0$) with a 1061-keV $\Delta K=25$ M1 transition.

According to the K-Selection Rule, this should have a very long half-life not 130 ns!

3. Gamma-softness (^{182}Os), loss of axial symmetry and gamma tunnelling

DECAY OF HIGH-SPIN ISOMERS IN Os NUCLEI BY BARRIER PENETRATION
P. CHOWDHURY¹, B. FABRICIUS², C. CHRISTENSEN, F. AZGUP³,
S. BJØRNHOLM, J. BØRGREEN, A. HOLM, J. PEDERSEN and G. SLETTEN
Niels Bohr Institute, DK-4000 Roskilde, Denmark
Nuclear Physics **A485** (1988) 136-160

Physics Letters B 435 (1998) 257-263
Multi-quasiparticle potential-energy surfaces
F.R. Xu ^{a,1}, P.M. Walker ^a, J.A. Sheikh ^{a,2}, R. Wyss ^b
^a Department of Physics, University of Surrey, Guildford, Surrey GU2 5XH, UK
^b Royal Institute of Technology, Physics Department, Frescativägen 24, S-104 05 Stockholm, Sweden

The loss of axial symmetry implies K is no longer a good quantum number...

Mentioned Gamma softness in ^{182}Os

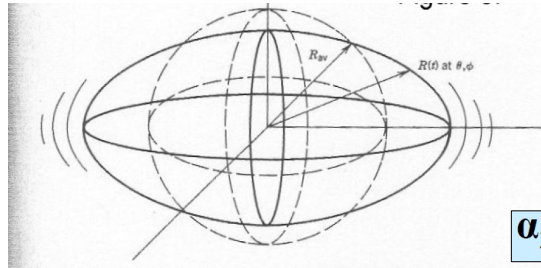
→ possibility of nuclear vibrations (gamma vibration)

Nuclear Vibrations

Nuclear Vibrations

Nuclear vibrations are considered as a liquid vibrating at high frequency.

Although the *average* nuclear shape is spherical, at any given instant it may not be spherical.



$$R(t) = R_{av} \left\{ 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{+\lambda} \alpha_{\lambda, \mu} Y_{\lambda, \mu}(\theta, \Phi) \right\}$$

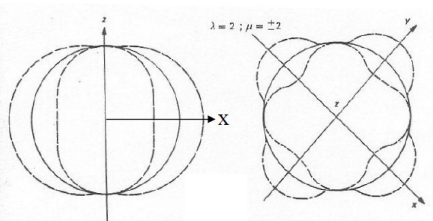
$Y_{\lambda, \mu}(\theta, \Phi)$ are the spherical harmonics with amplitude $\alpha_{\lambda, \mu}$

Consider $\lambda=2$ **Quadrupole** Phonons in Mass 180 Region (quadrupole deformed shape)

$$R(t) = R_{av} \left\{ 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{+\lambda} \alpha_{\lambda, \mu} Y_{\lambda, \mu}(\theta, \Phi) \right\}$$

Gamma Vibrations

For $\lambda=2, \mu=\pm 2$,
 $Y_{2\pm 2}(\theta, \Phi) = 3 \sin^2 \theta \cos 2\Phi$

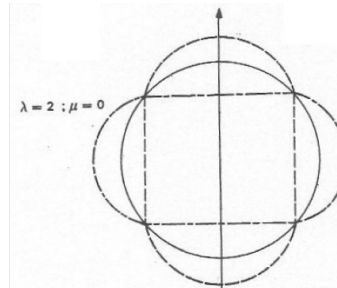


A gamma (γ) vibration in which a wave runs equatorially with no variation of polar diameter

The transportation of mass involves increasing the angular momentum about the z-axis, for this second-order harmonic, by $2\hbar$ units.

Beta Vibrations

For $\lambda=2, \mu=0$,
 $Y_{2+0}(\theta, \Phi) = \frac{1}{2} (3 \cos^2 \theta - 1)$



A beta (β) vibration in which the polar diameter oscillates with no variation in shape of section at different values of Φ

This mode **transports** mass away from the nuclear poles, i.e. in a plane of constant Φ .

This does **not** involve any angular momentum generation about the z-axis.

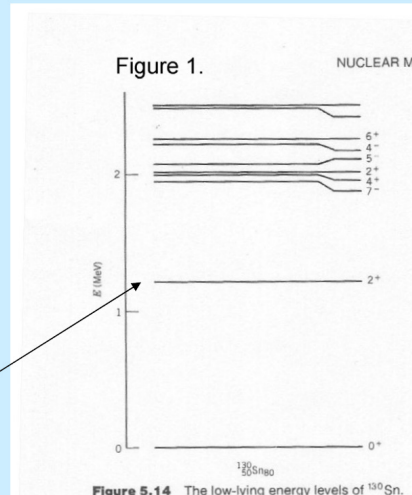
"Pushing" & "pulling" on **sides** of rugby ball

"Pushing" & "pulling" on **ends** of rugby ball

Consider adding **one** $\lambda=2$ phonon vibration to the 0^+ **ground state** of an **even-even** nucleus.

This phonon adds $2\hbar$ of angular momentum & has **even** parity due to the $(-1)^\lambda$ dependence of the $Y_{\lambda\mu}(\theta, \Phi)$

Adding 2^+ units of angular momentum to a 0^+ ground state gives a 2^+ state, in **exact** agreement with the observed spin and parity of the 1st excited states of **spherical** even-Z even-N nuclei, see Fig. 1.

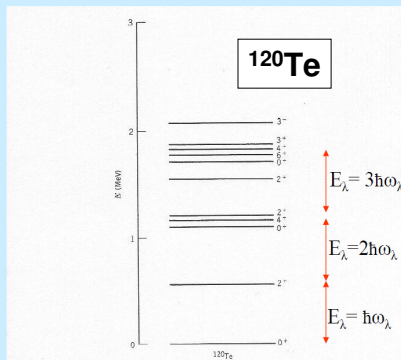


Possibility to generate angular momentum by **vibrations** in competition with collective **rotation**

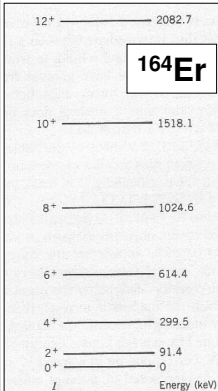
$$E_\lambda = n_\lambda \cdot \hbar \cdot \omega_\lambda \quad \text{Vibration}$$

This $0^+, 2^+, 4^+$ **triplet** is a common feature of vibrational nuclei & gives **strong** support to the model.

A similar calculation for 3-phonon states gives $0^+, 2^+, 4^+, 6^+$



Contrast with rotor
 $E_I = I(I+1)\hbar^2/2J$



"Nuclear Tidal waves"

- Stefan Frauendorf

Combination of

- Angular momentum reorientation
- Triaxial deformation

→ Shape change at nearly constant angular velocity

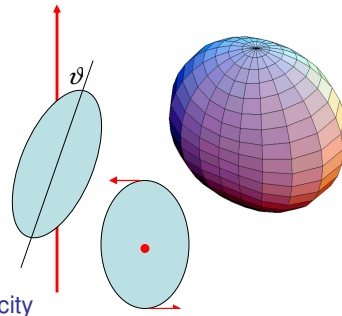
Rotating mean field gives a reliable microscopic description
No new parameters

$$R(\vartheta, \varphi, t) = R_0[1 + 2a_2 \cos(2\varphi - \Omega t)Y_{22}(\vartheta, \varphi = 0)]$$

$$\omega = \frac{\Omega}{2} \quad E = \omega L_z$$

Spin (\hbar)	γ°	θ°
26.0	-7.4	19.0
27.0	-9.7	23.7
28.0	-12.2	26.8
29.0	-15.0	28.5
30.0	-17.6	29.2
31.0	-20.4	30.7
32.0	-22.9	31.9
33.0	-25.1	33.3
34.0	-27.2	34.8
35.0	-29.0	36.3
36.0	-31.1	37.3
37.0	-33.4	37.4
38.0	-35.0	36.0

Experimental rotational frequency well defined & constant in SC-TAC calculations.

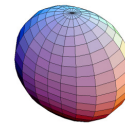


Multi-phonon Quadrupole Vibrations.

Nuclear Tidal Wave :

Angular momentum generated by:

- phonon vibration in intrinsic frame
- coupled with collective rotation
- Shape change at nearly constant angular velocity

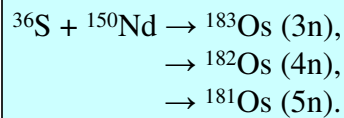


Can become **Favoured** high-spin mode in soft osmium nuclei
where the energy of rotation is > energy of vibration

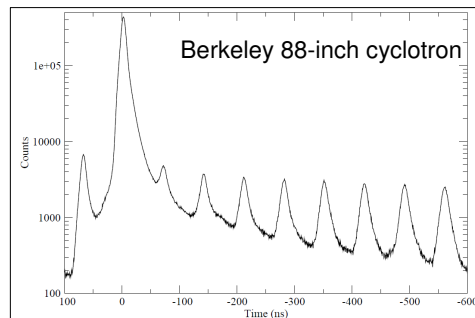
(PRL 91(03)182501)

Results of Gammasphere Experiments

^{181}Os , ^{182}Os , ^{183}Os (Berkeley)



Thick target $1.0\text{mg}/\text{cm}^2$



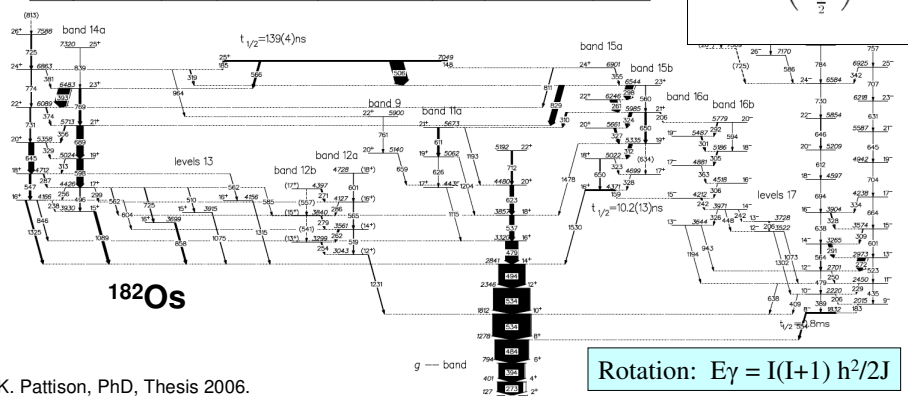
$K^\pi = 25^+$ Six Quasi-particle Isomer Decay in ^{182}Os .

Table 6.2: Reduced hindrance factor calculations for the decay paths of the $K^\pi = 25^+$, $139 \pm 4\text{ns}$ isomer.

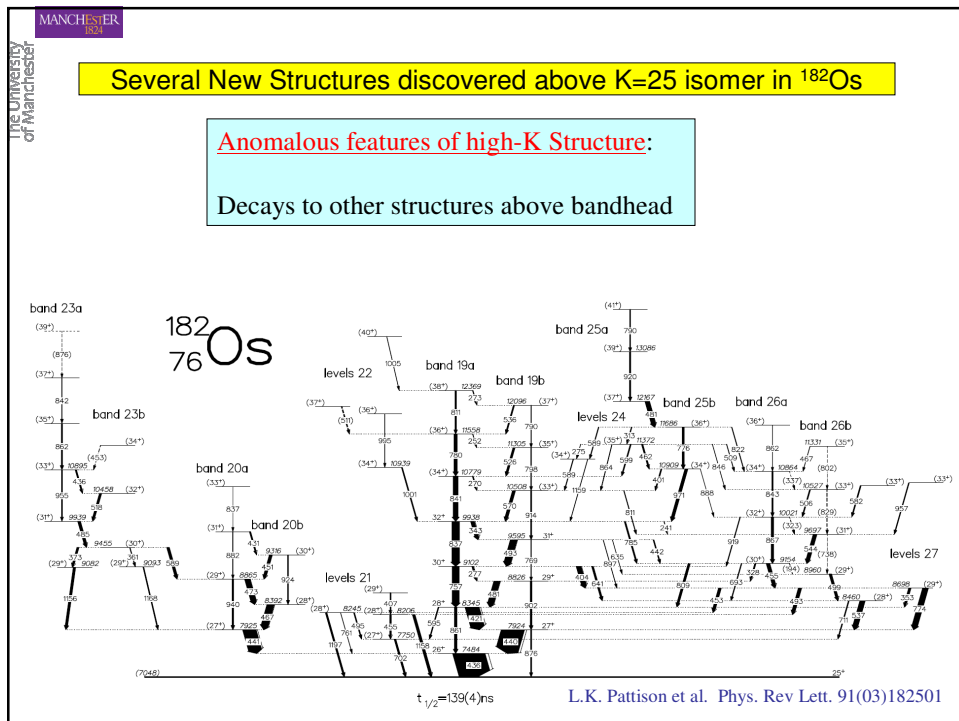
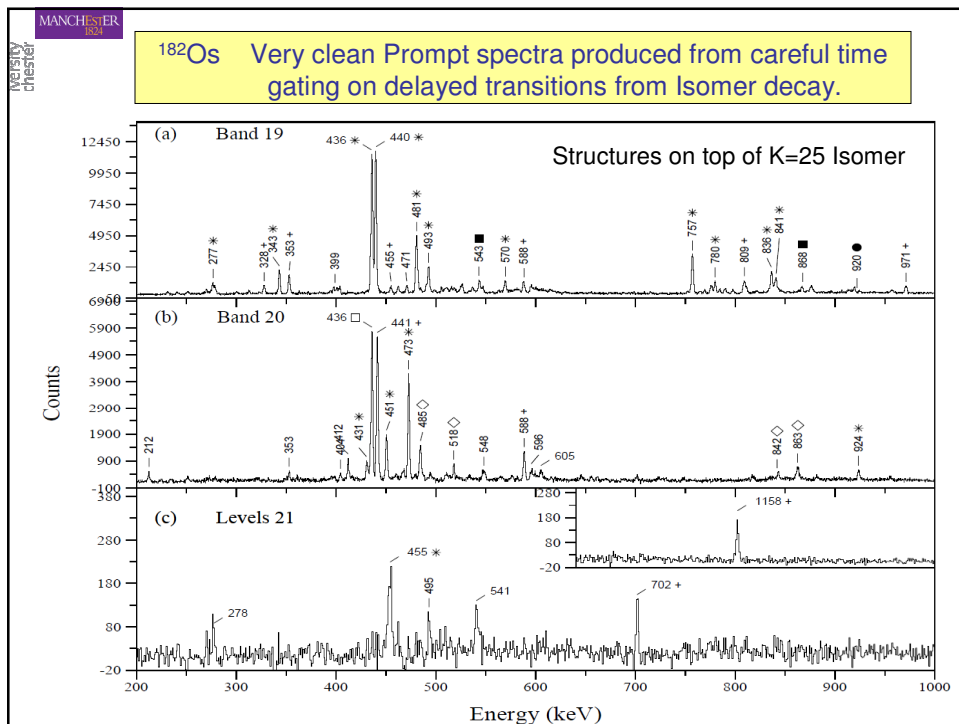
K^π	E_γ (KeV)	Band	$T_{1/2}^{\text{partial}}$ (ns)	Multipolarity	ΔK	$\nu = \Delta K - \lambda$	f_ν
25^+	186	14	1534	M1	10	9	4.5
25^+	566	14	1970	E2	10	8	3.3
25^+	506	15	297	E2	9	7	2.7
25^+	148	15	16655	M1	9	8	6.8
25^+	386	8	6819	(M1)	(5)	(4)	75
25^+	727	11	435	E2	8	6	4.6
25^+	679	7	20771	(M1)	(7)	(6)	28
25^+	1062	gsb	8214	M1	≈ 17	≈ 16	≈ 3.6

Small hindrance factors for new decays

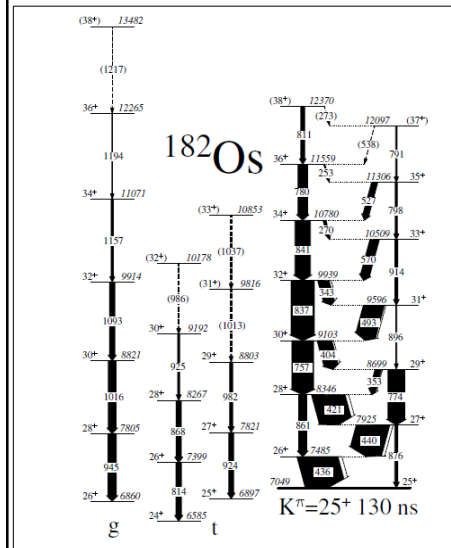
$$f_\nu = \left(\frac{T_{1/2}^\gamma}{T_{1/2}^W} \right)^{\frac{1}{\nu}}$$



L.K. Pattison, PhD, Thesis 2006.



Focus on main structure above K=25 isomer in ^{182}Os



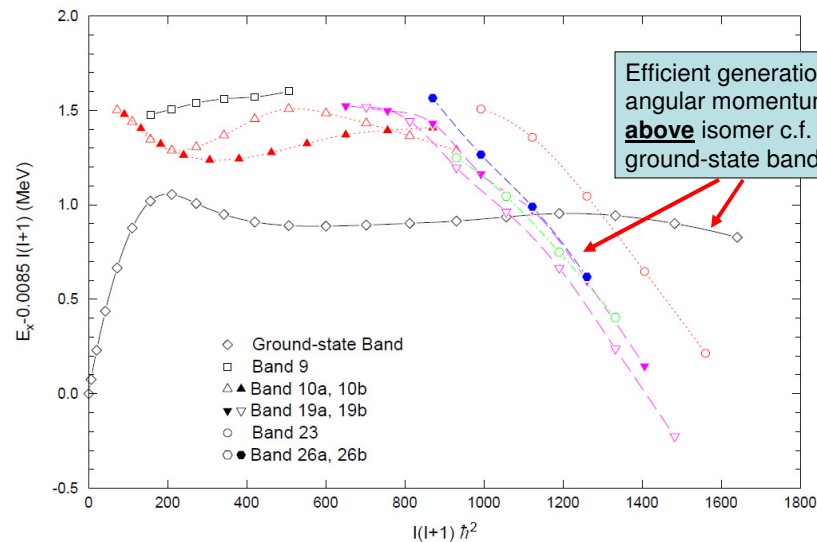
Anomalous features of high-K

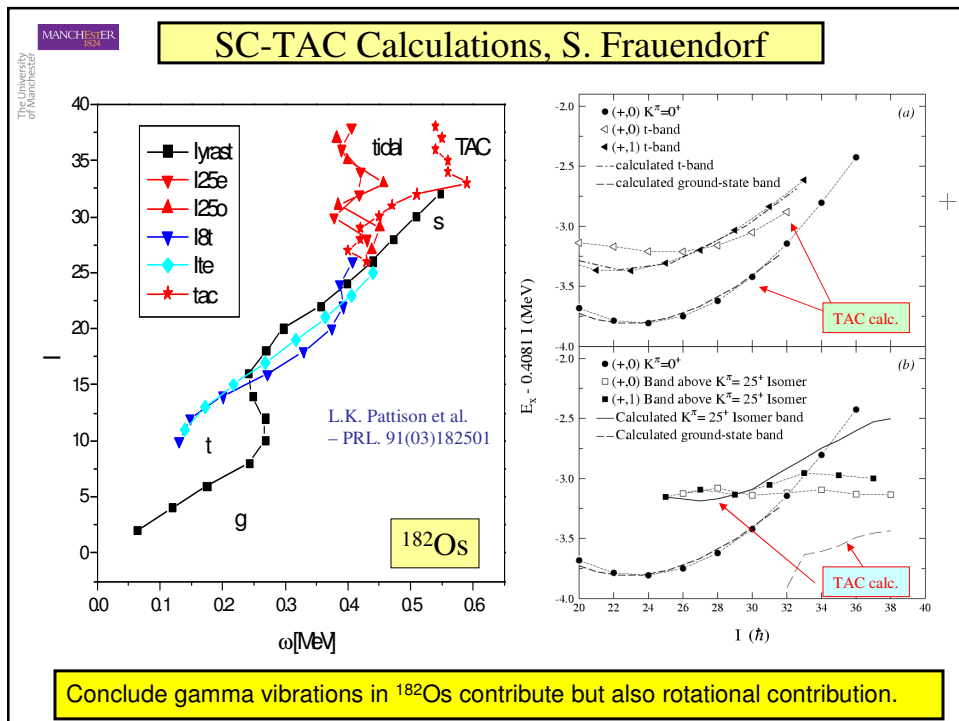
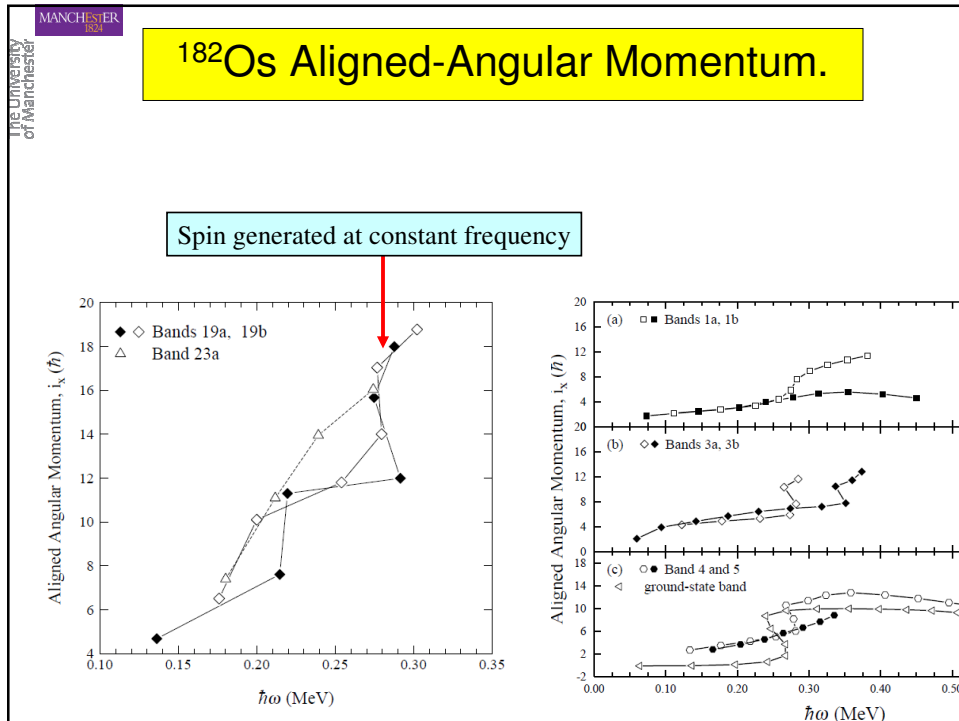
Band:

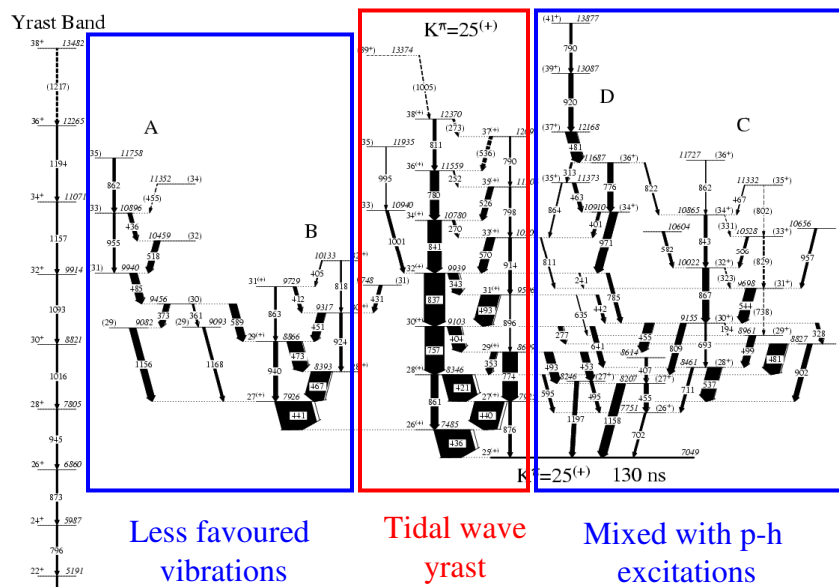
1. Strong E2s
2. Intensity Staggering of Signatures
3. $\Delta E_\gamma \approx \text{Constant}$ (c.f. rotational g and t bands)

L.K. Pattison et al. Phys. Rev Lett. 91(03)182501

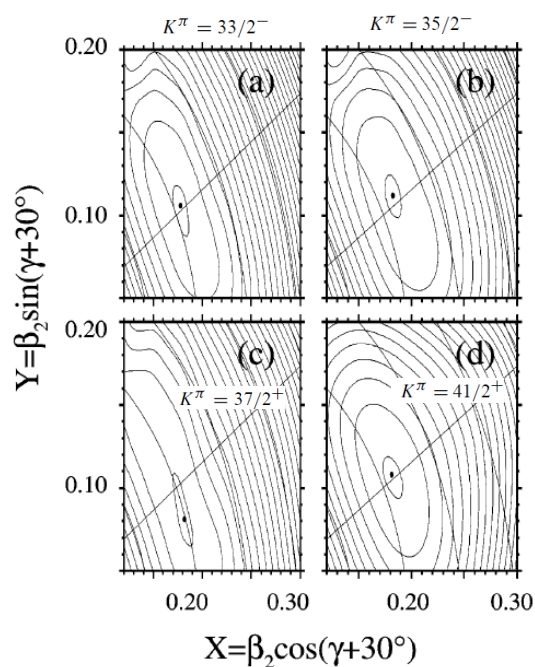
^{182}Os Excitation energy minus rigid-rotor reference.





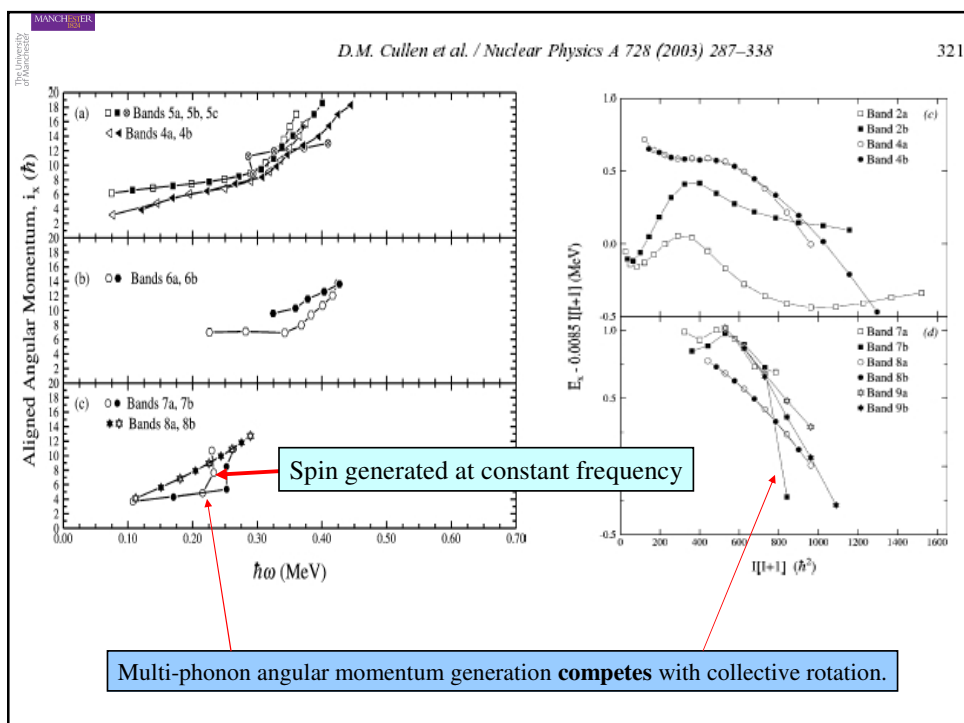
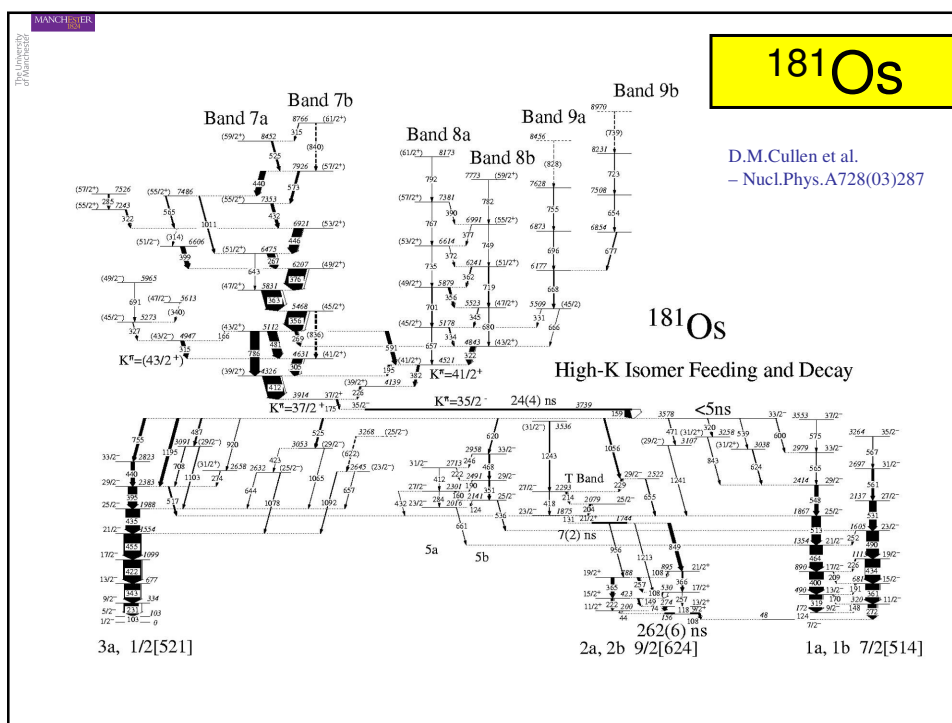
^{182}Os 

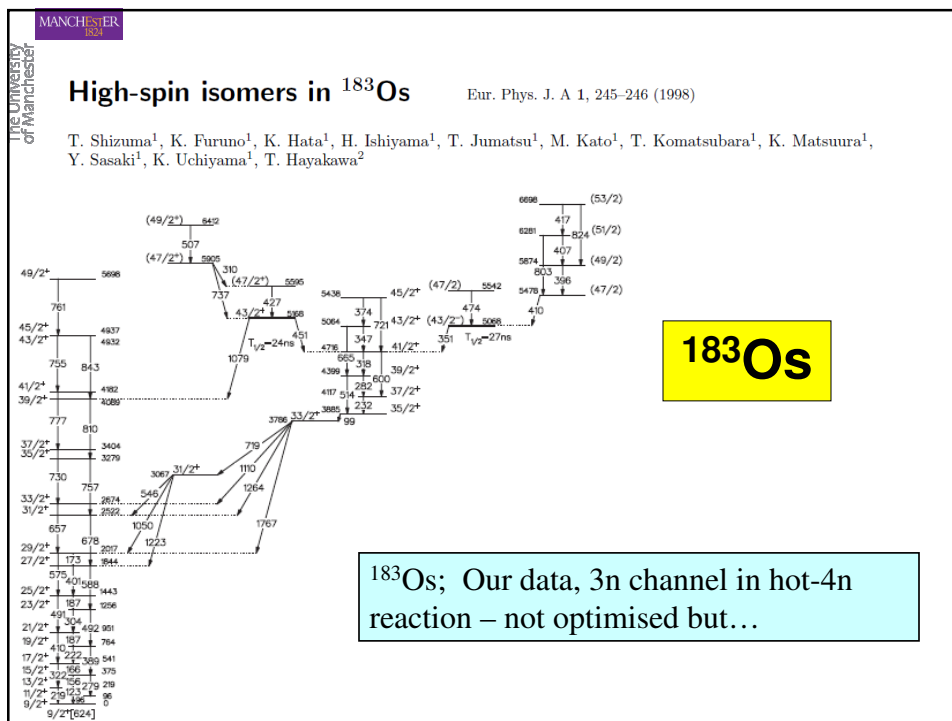
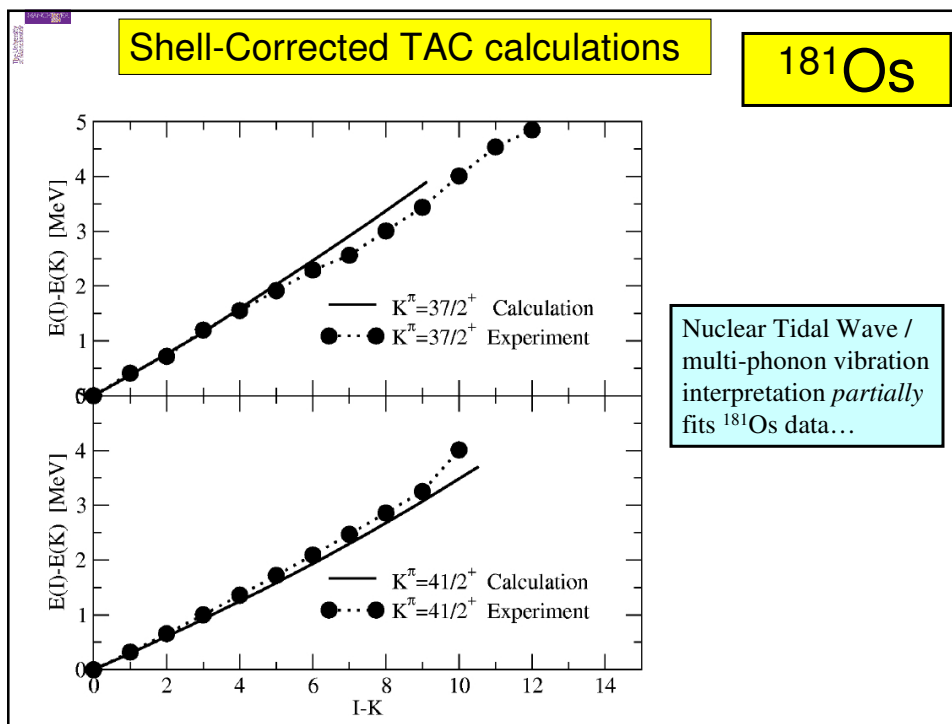
Configuration constrained potential energy surface calculation

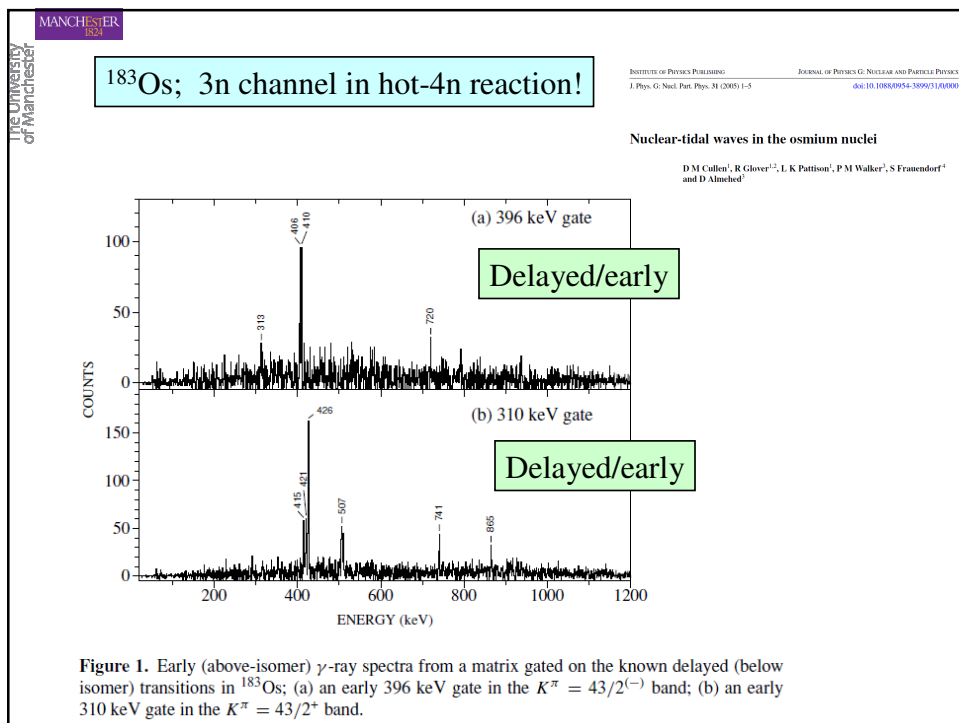
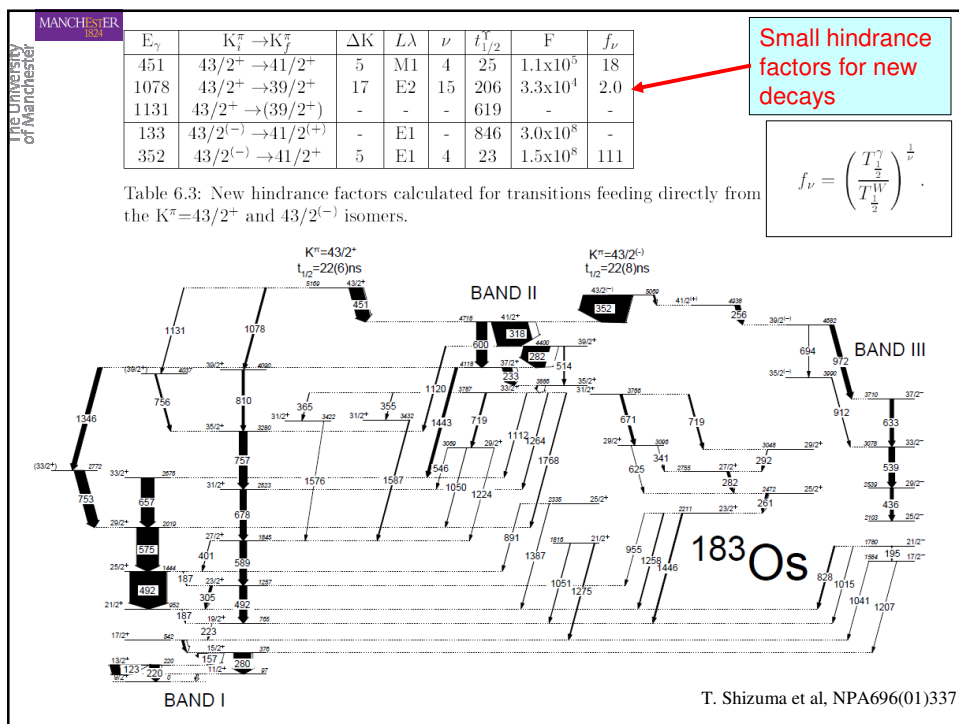
 ^{181}Os 

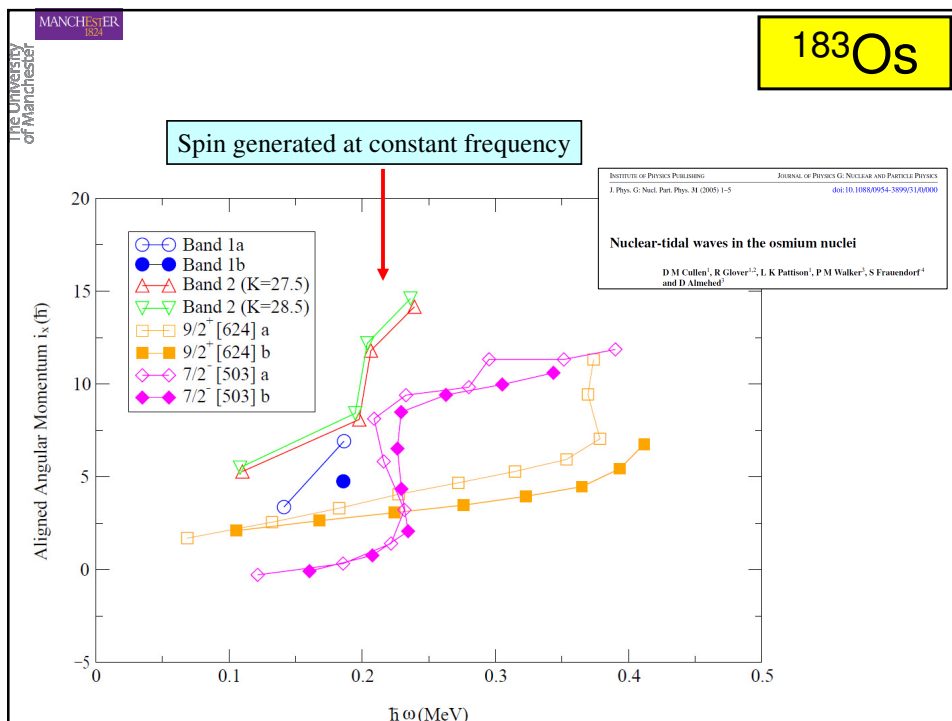
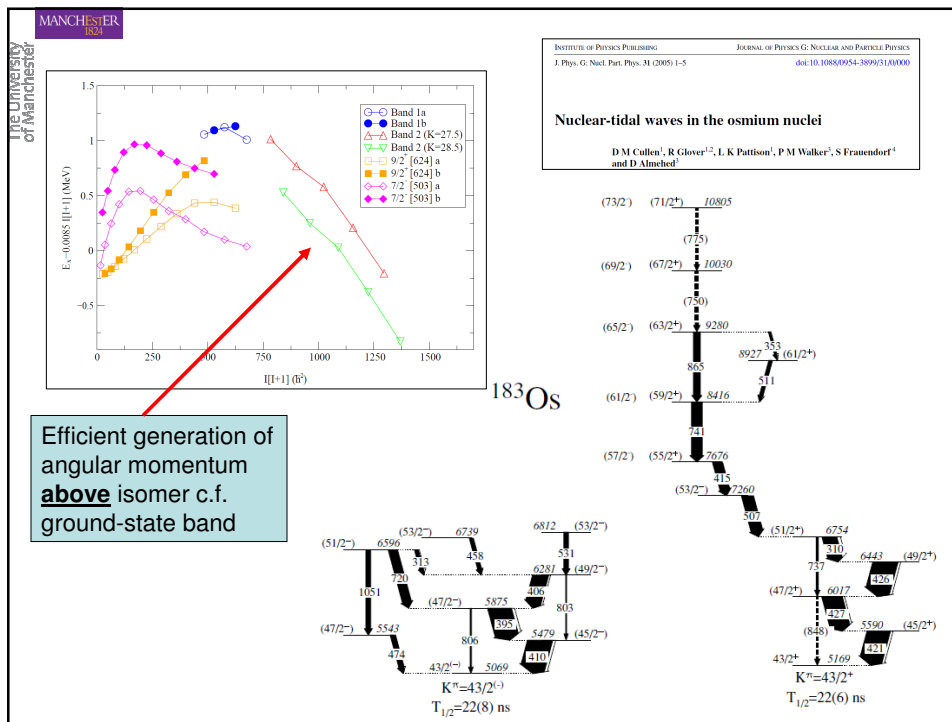
^{181}Os ; 5n channel
in hot-4n reaction
– quite optimised

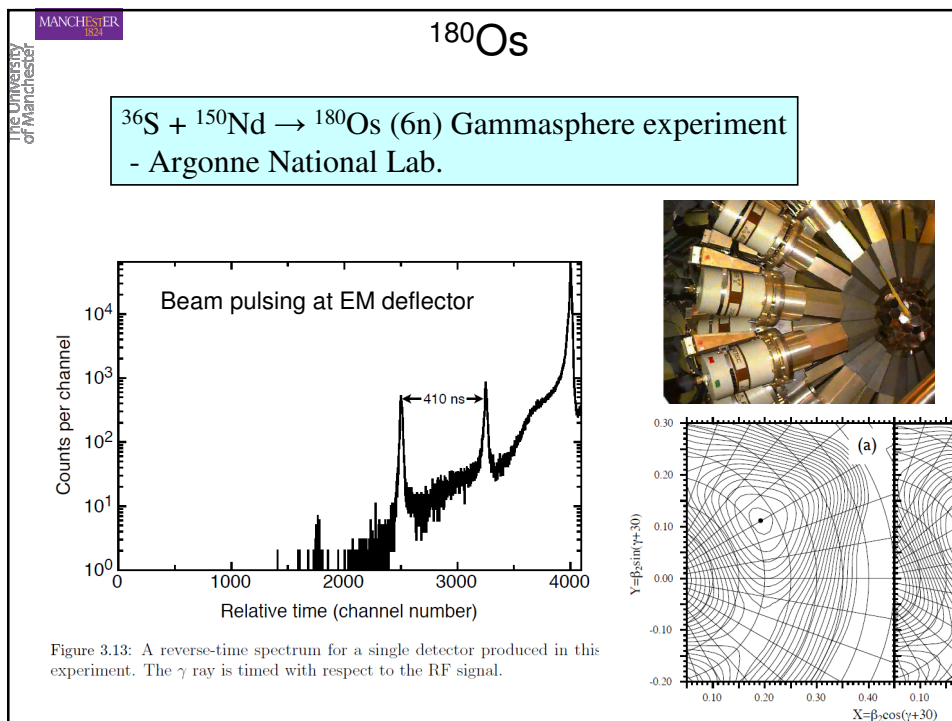
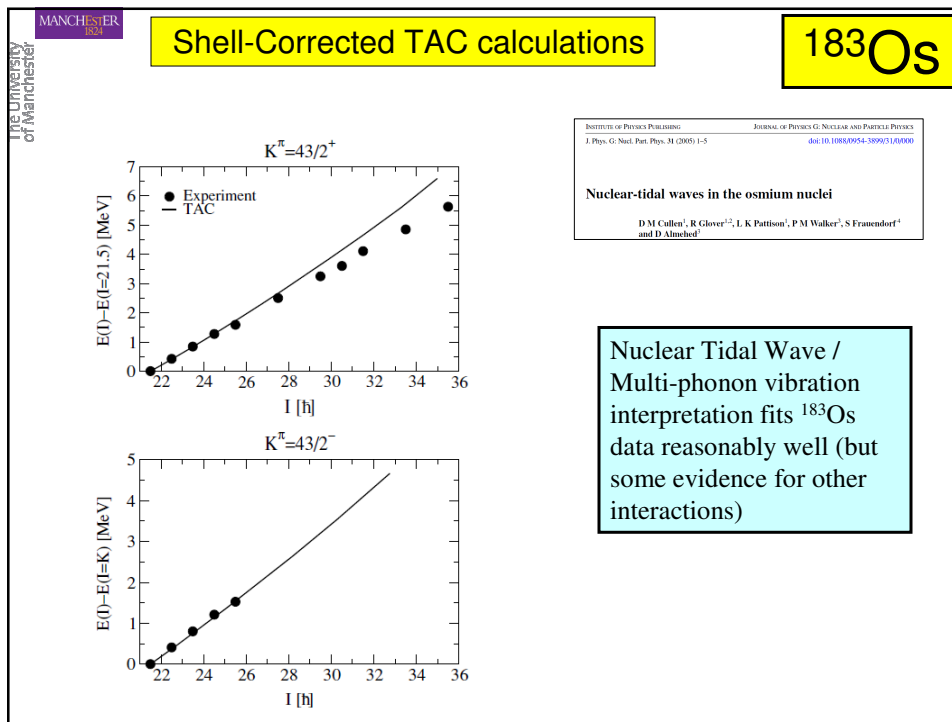
Nuclear Physics A 728 (2003) 287–338

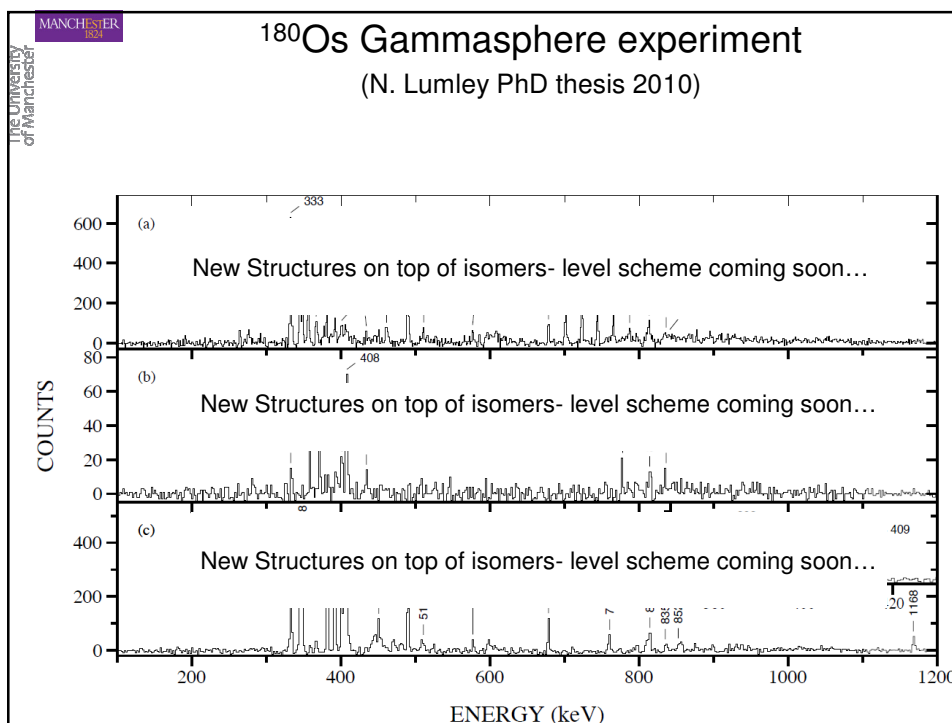
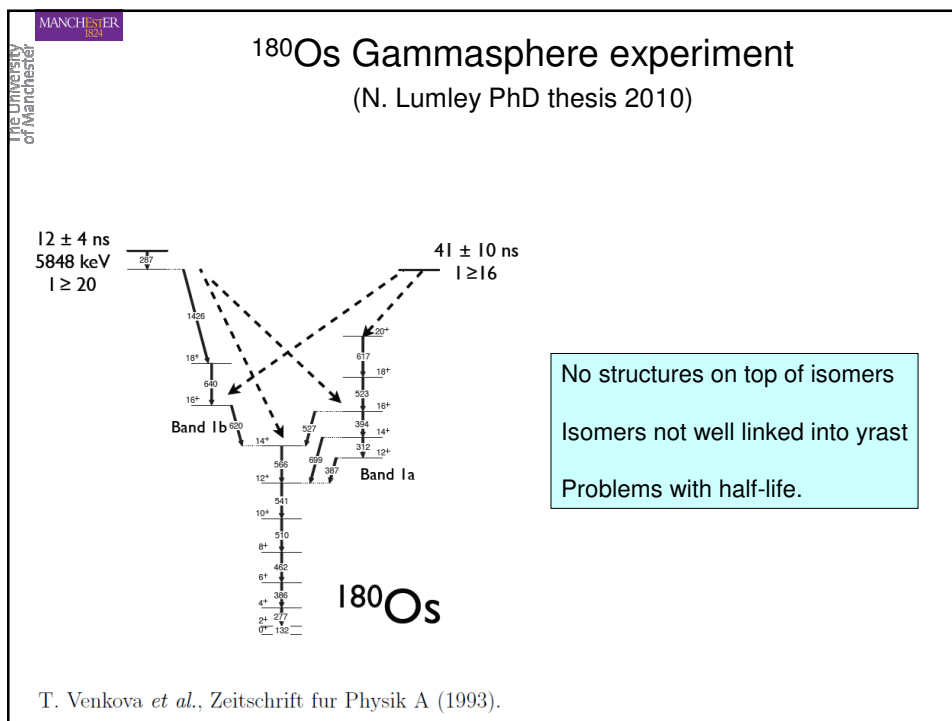


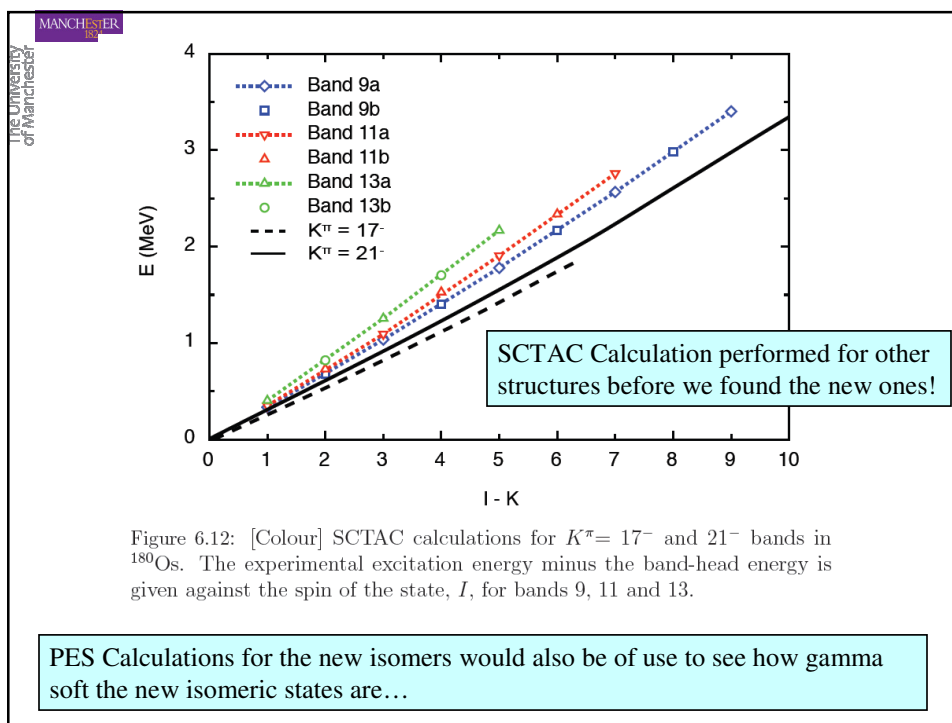
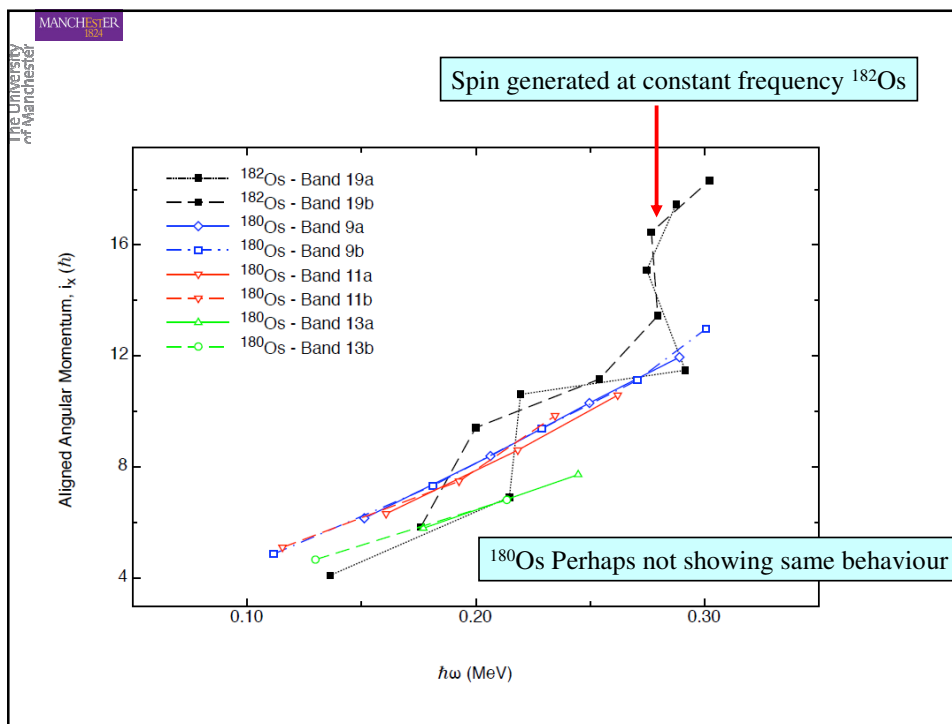












Conclusions

Nuclear Tidal Wave / Multi-phonon Interpretation:

- Gives good explanation for anomalous high-K behaviour in **soft** osmium nuclei ^{181}Os , ^{182}Os , ^{183}Os [and perhaps ^{180}Os ?]
- Angular momentum generated by shape change at nearly constant angular velocity
- **Competes** with collective rotation
- Look for future examples...
2006 - Octupole ($\lambda=3$) tidal waves in discovered in ^{220}Th
W. Reviol, Phys. Rev. C 74 (06) 044305

Thanks to the collaborators...

VOLUME 91, NUMBER 18

PHYSICAL REVIEW LETTERS

week ending
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Multiphonon Vibrations at High Angular Momentum in ^{182}Os

L. K. Pattison,¹ D. M. Cullen,¹ J. F. Smith,¹ A. M. Fletcher,¹ P. M. Walker,² H. M. El-Masri,² Zs. Podolyák,² R. J. Wood,² C. Scholey,³ C. Wheldon,³ G. Mukherjee,⁴ D. Balabanski,⁵ M. Djongolov,⁶ Th. Dalsgaard,⁷ H. Thysgaard,⁷ G. Sletten,⁷ F. Kondev,⁸ D. Jenkins,⁸ G. J. Lane,⁹ I.-Y. Lee,⁹ A. O. Macchiavelli,⁹ S. Frauendorf,¹⁰ and D. Almedid¹¹

¹Schuster Laboratory, University of Manchester, Manchester M13 9PL, United Kingdom

²Department of Physics, University of Surrey, Guildford GU2 7XH, United Kingdom

³Oliver Lodge Laboratory, University of Liverpool, Liverpool L69 7ZE, United Kingdom

⁴Department of Physics, University of Massachusetts, Lowell, Massachusetts 01854, USA

⁵Faculty of Physics, University of Sofia, BG-1164 Sofia, Bulgaria

⁶Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA

⁷Niels Bohr Institute, Blegdamsvej 17, DK-2100, Copenhagen, Denmark

⁸Physics Division, Argonne National Laboratory, Argonne, Illinois 60439, USA

⁹Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

¹⁰Department of Physics, University of Notre Dame, Notre Dame, Indiana 46556, USA

¹¹Department of Physics, UMIST, P.O. Box 88, Manchester M60 1QD, United Kingdom

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N. Lumley (^{180}Os), R. Glover (^{183}Os)