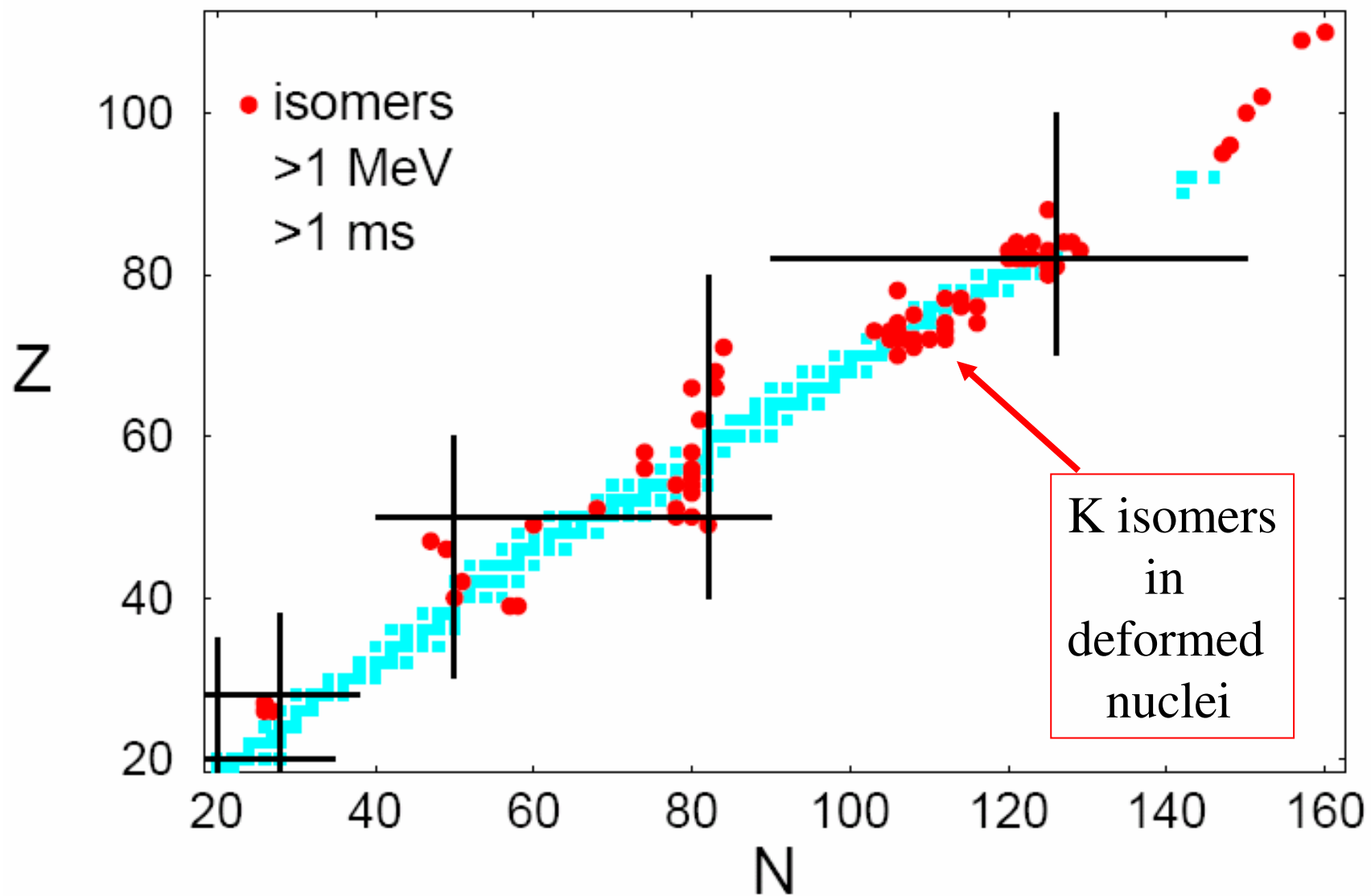




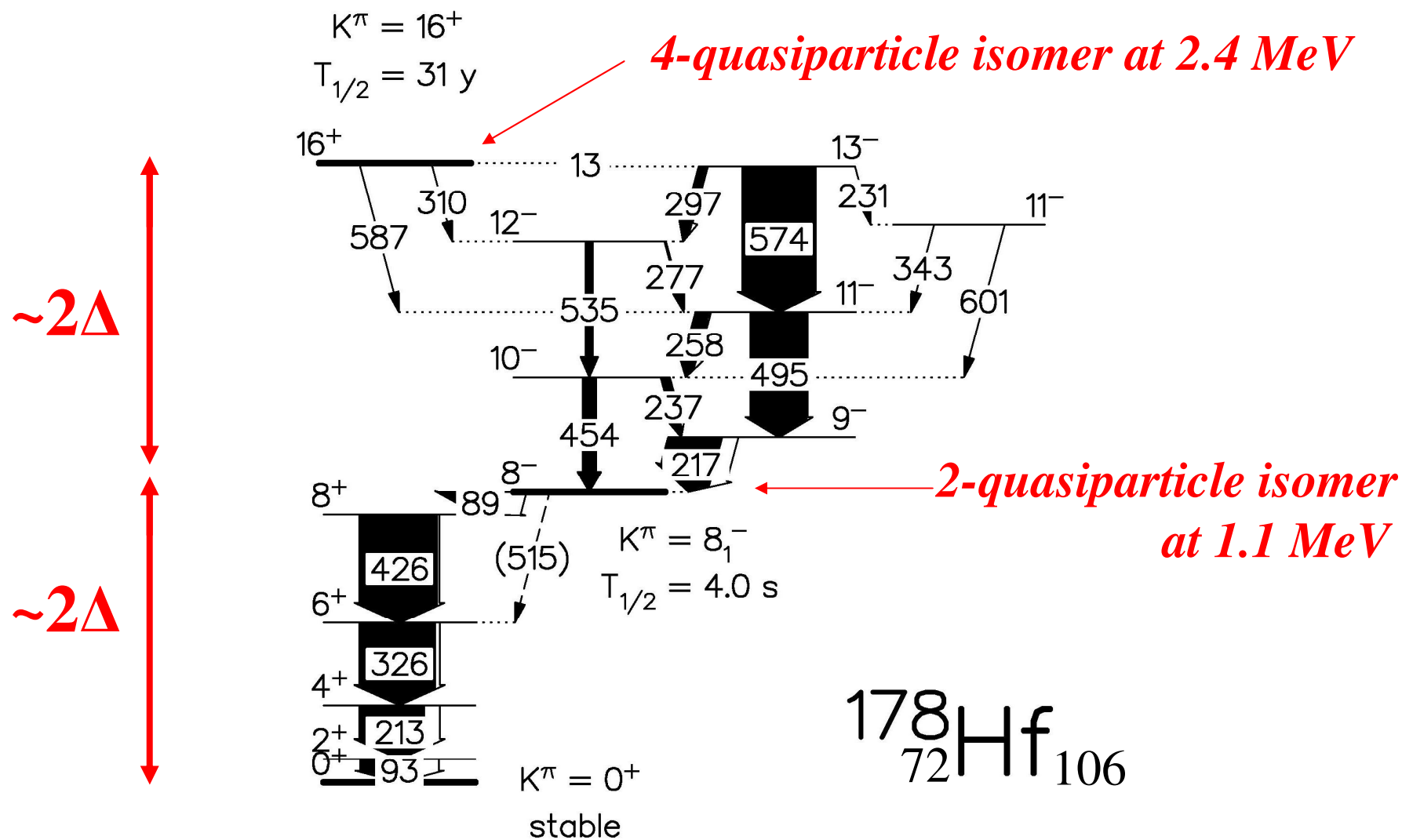
K-isomer decay rates

Phil Walker

- introduction
- exploring the different degrees of freedom
- exotic nuclei

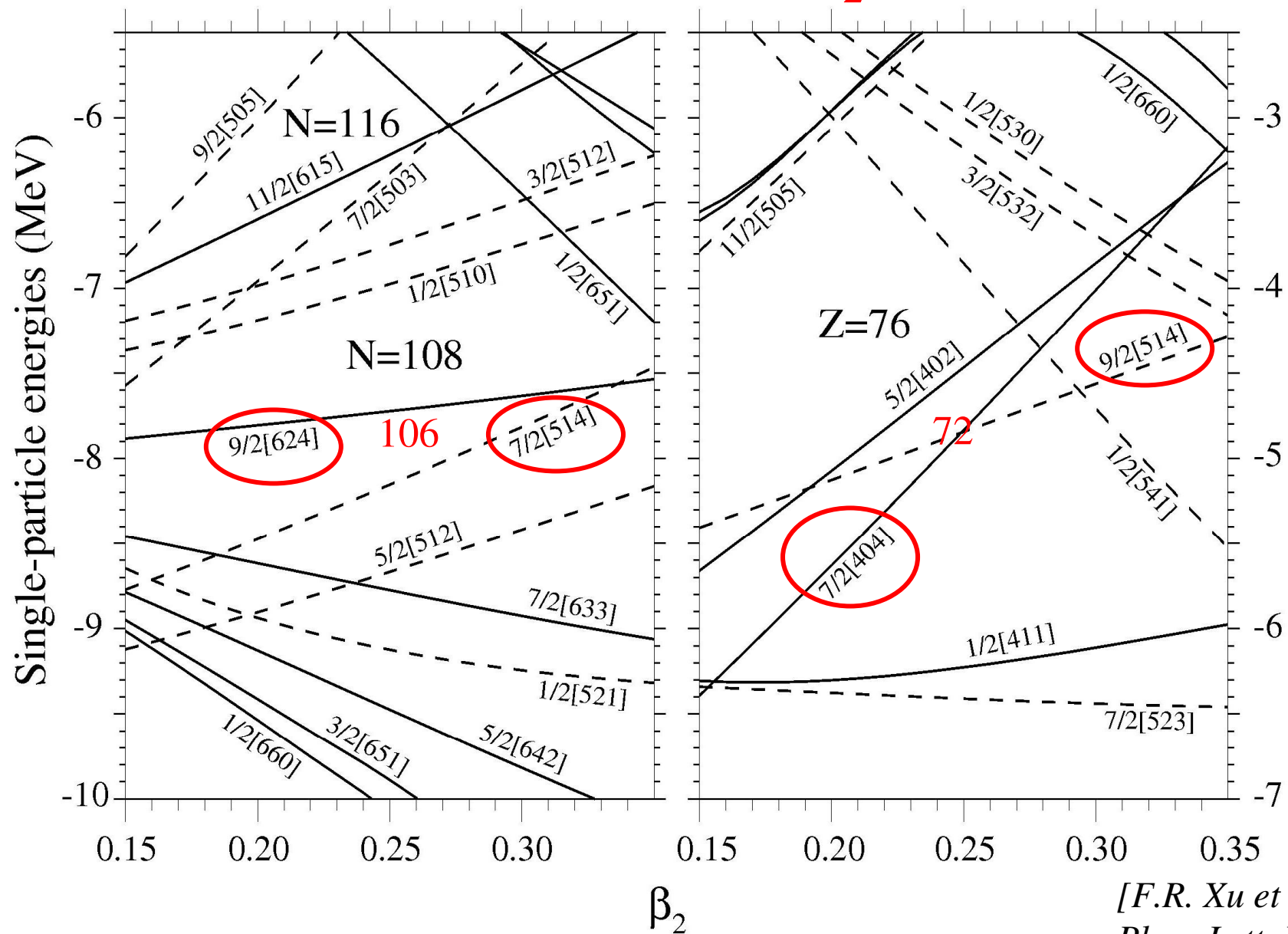


adapted from Walker and Dracoulis, Nature 399 (1999) 35



[Smith et al., Phys. Rev. C68 (2003) 031302(R)]

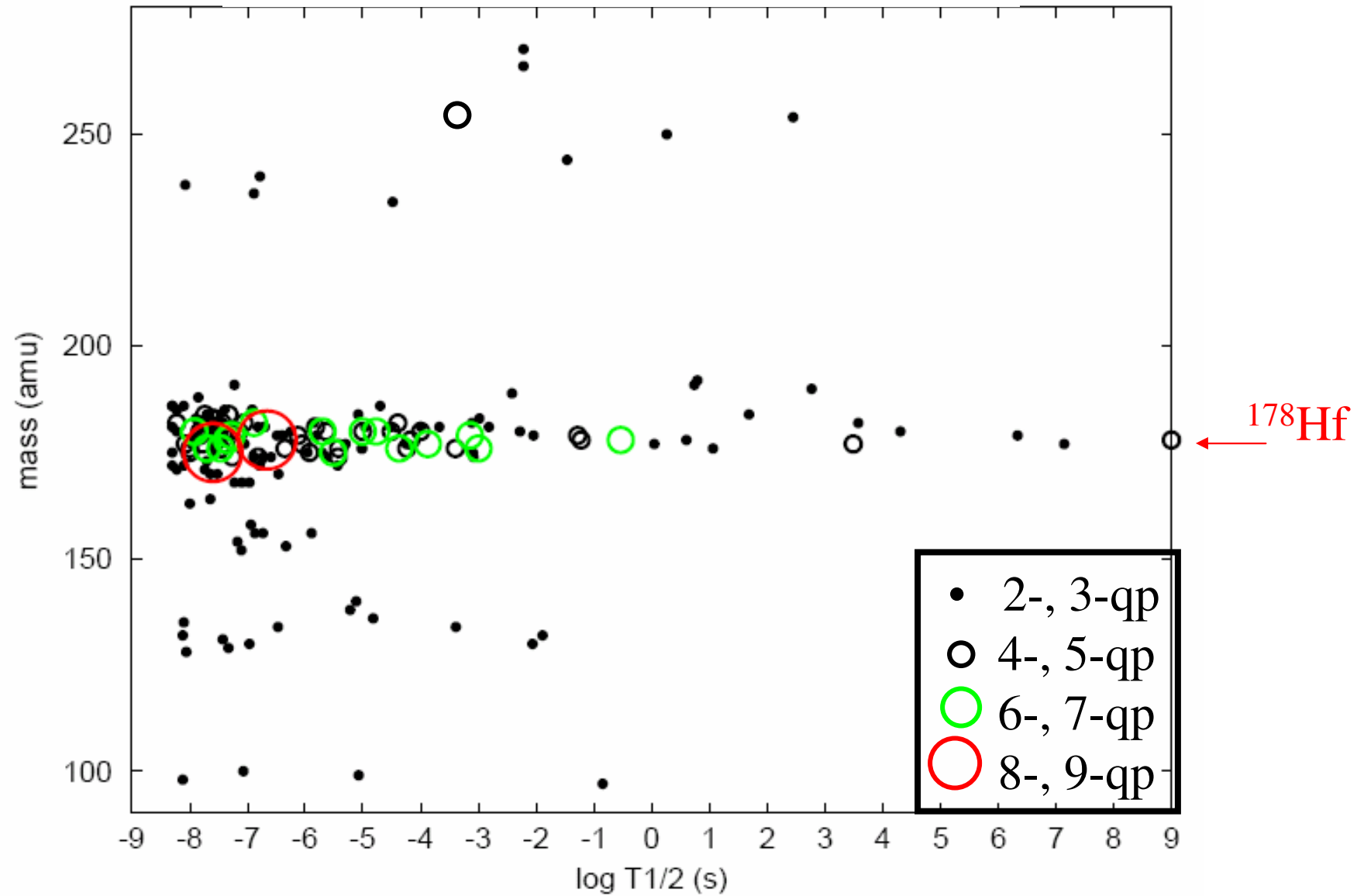
^{178}Hf has $N=106$, $Z=72$, $\beta_2 \sim 0.25$



Woods-Saxon potential

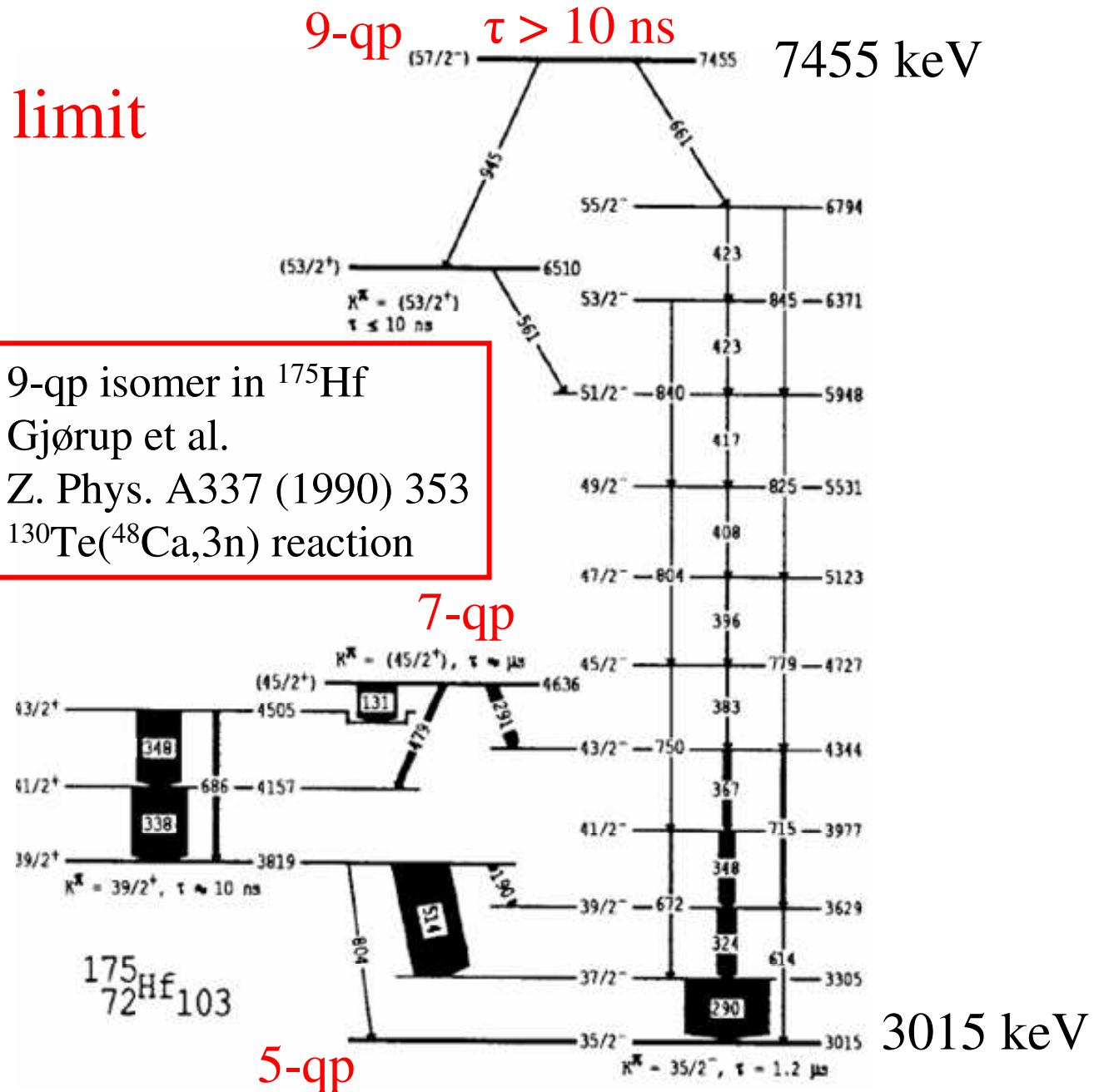
[F.R. Xu et al.,
Phys. Lett. B435
(1998) 257]

multi-quasiparticle K isomers > 5ns



K-isomer energy/spin limit

9-qp isomer in ^{175}Hf
Gjørup et al.
Z. Phys. A337 (1990) 353
 $^{130}\text{Te}(^{48}\text{Ca}, 3n)$ reaction



K isomers

- structure
 - energies
 - transition rates?
- deformed shell model
-
- ```
graph LR; A[deformed shell model] --- B[- structure]; A --- C[- energies]; A --- D[- transition rates?];
```

# transition-rate hindrance factors

$$F_W = T_{1/2}^\gamma / T_{1/2}^W$$

*Weisskopf hindrance*

$$\nu = \Delta K - \lambda$$

*degree of K forbiddenness*

$$f_\nu = (F_W)^{1/\nu}$$

*reduced hindrance*  
(hindrance per degree of  
K forbiddenness)



*contains the physics*

# Weisskopf transition rates

Weisskopf single-particle half-lives<sup>a</sup>

---

Electric dipole (E1)  $T_{1/2}^W = 6.76 \times 10^{-6} E^{-3} A^{-2/3}$

Magnetic dipole (M1)  $T_{1/2}^W = 2.20 \times 10^{-5} E^{-3}$

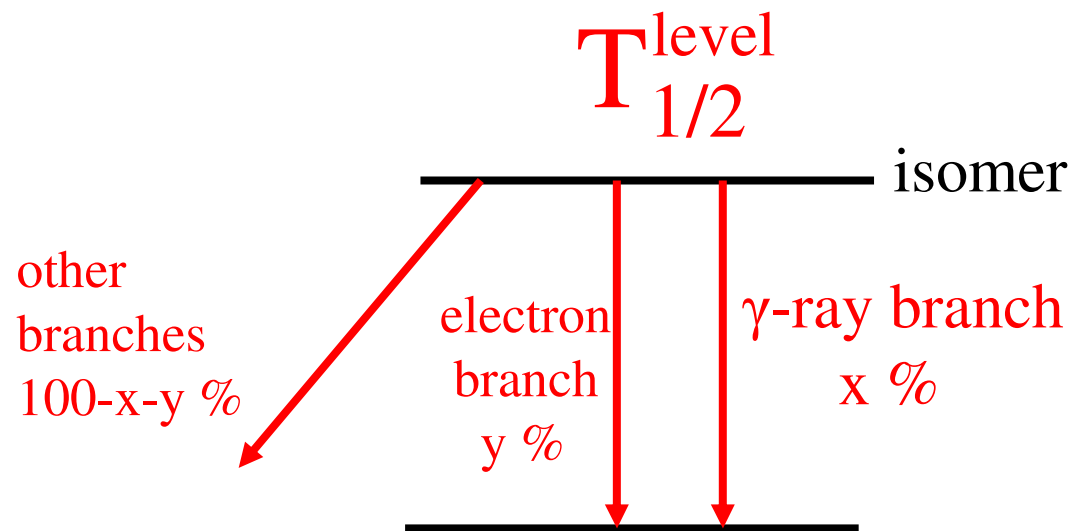
Electric quadrupole (E2)  $T_{1/2}^W = 9.52 \times 10^6 E^{-5} A^{-4/3}$

Magnetic quadrupole (M2)  $T_{1/2}^W = 3.10 \times 10^7 E^{-5} A^{-2/3}$

---

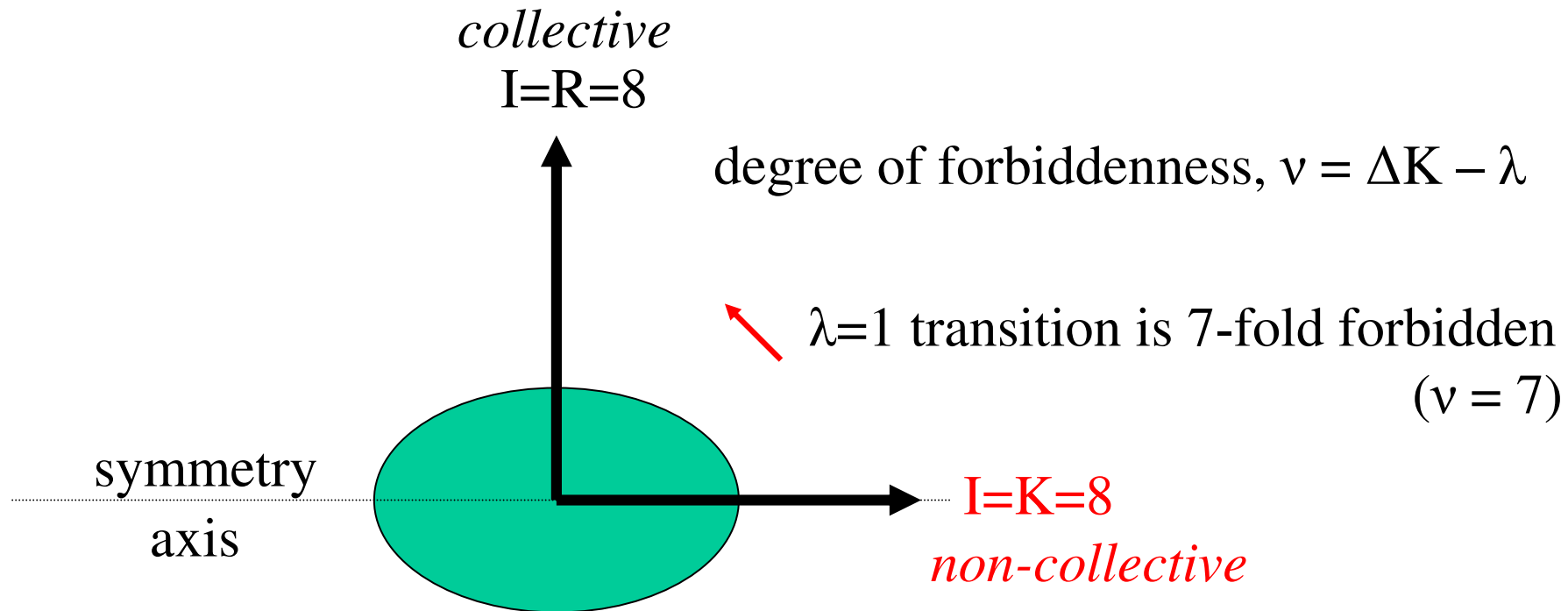
<sup>a</sup>For transition energies ( $E$ ) in keV, the half-lives are in seconds

partial  $\gamma$ -ray half-life:  $T_{1/2}^{\gamma}$

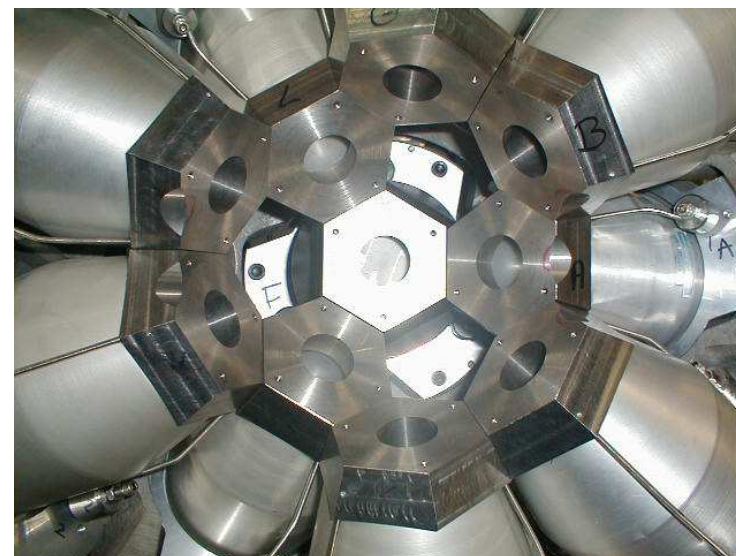
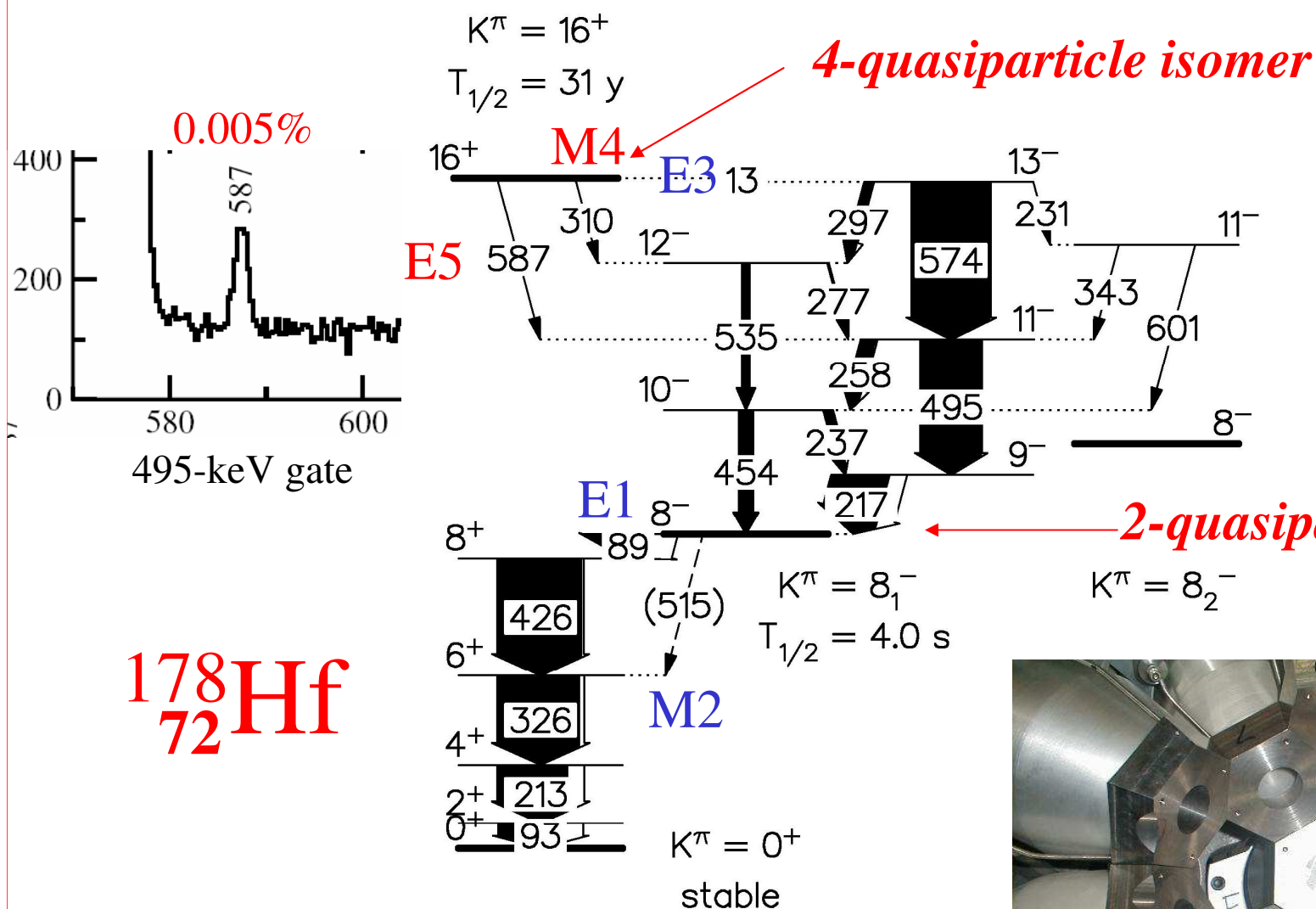


$$T_{1/2}^{\gamma} = T_{1/2}^{\text{level}} \cdot 100/x$$

# K-forbidden $\gamma$ -ray transitions

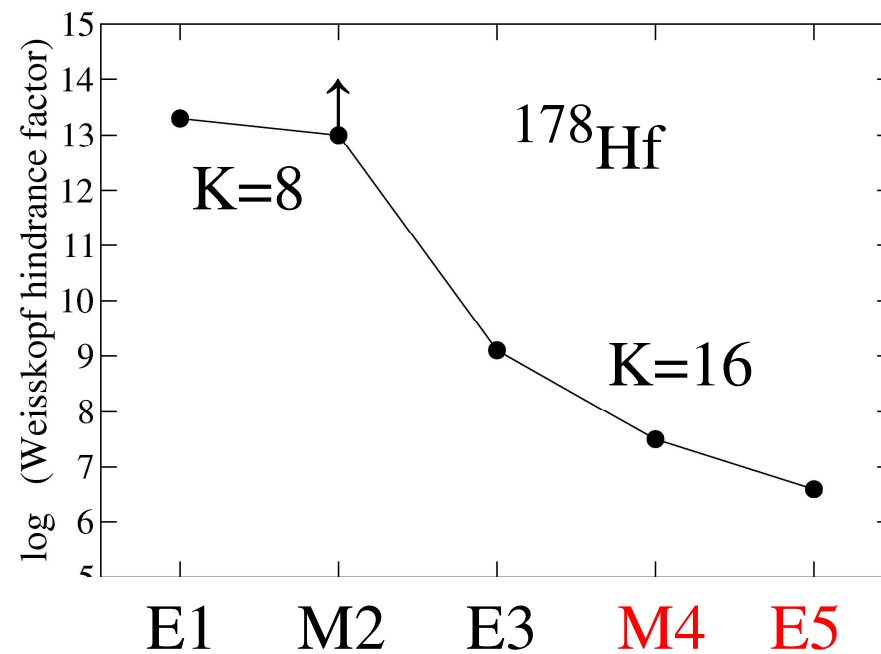


*angular momentum has both magnitude and direction!*



*data from the  $8\pi$  spectrometer at TRIUMF*

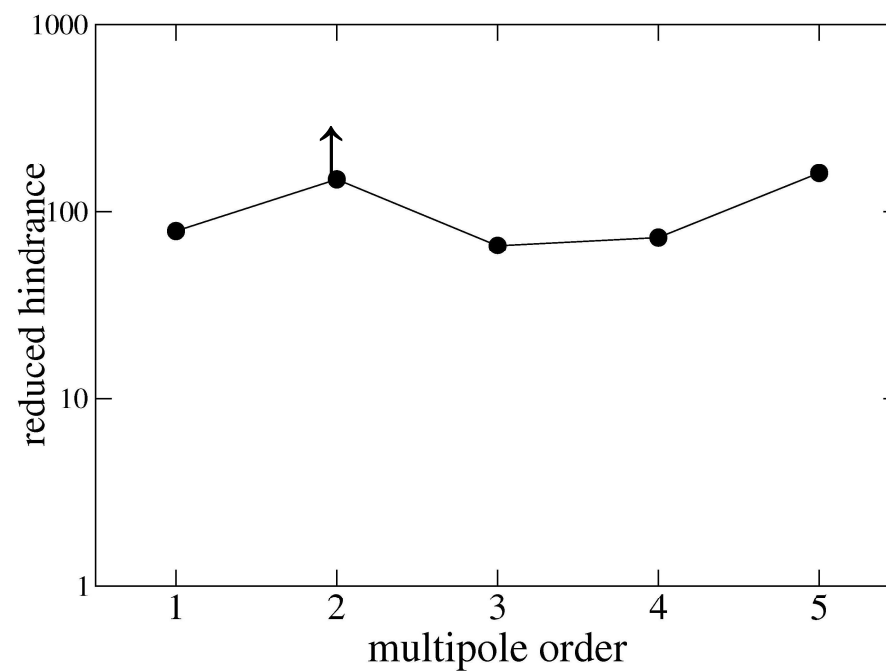
*[Smith et al., Phys. Rev. C68 (2003) 031302(R)]*



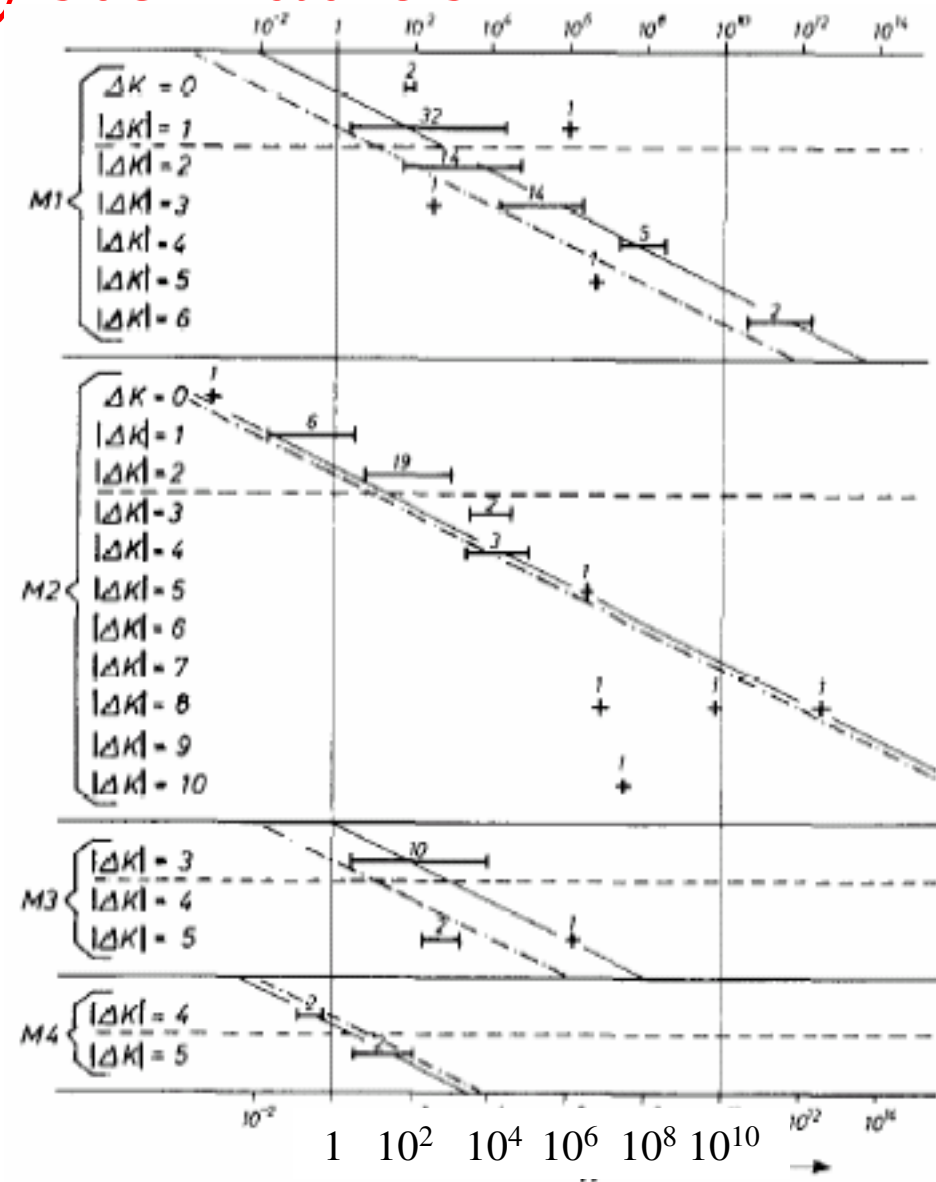
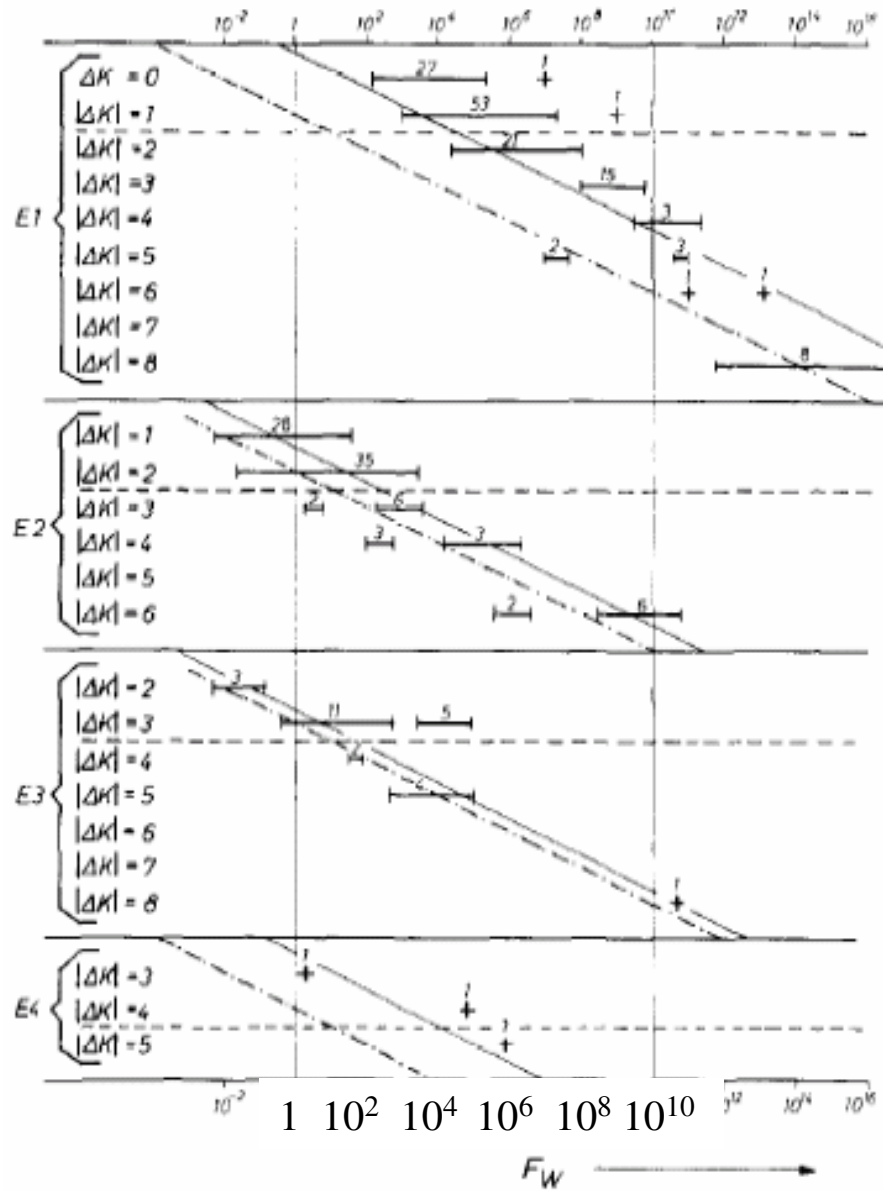
$$F_W = T_{1/2}^\gamma / T_{1/2}^W$$

$$\nu = \Delta K - \lambda$$

$$f_\nu = (F_W)^{1/\nu}$$

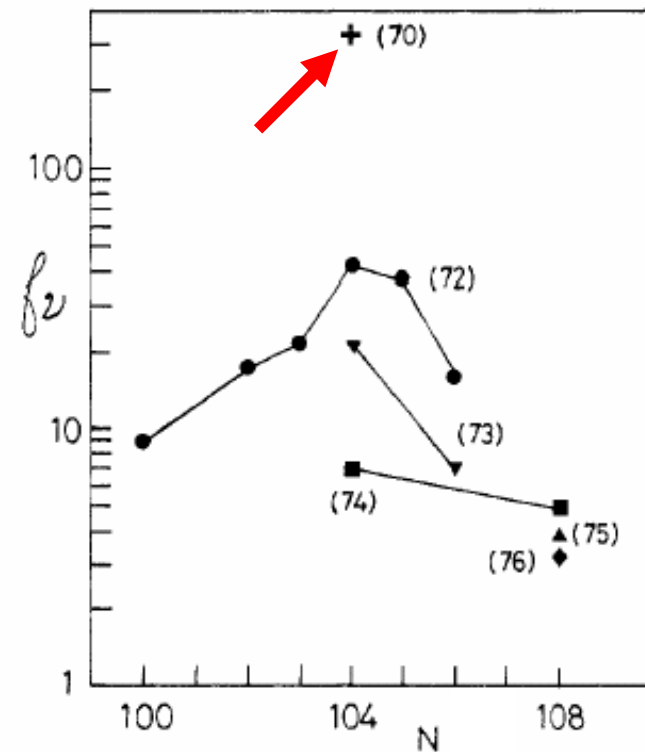
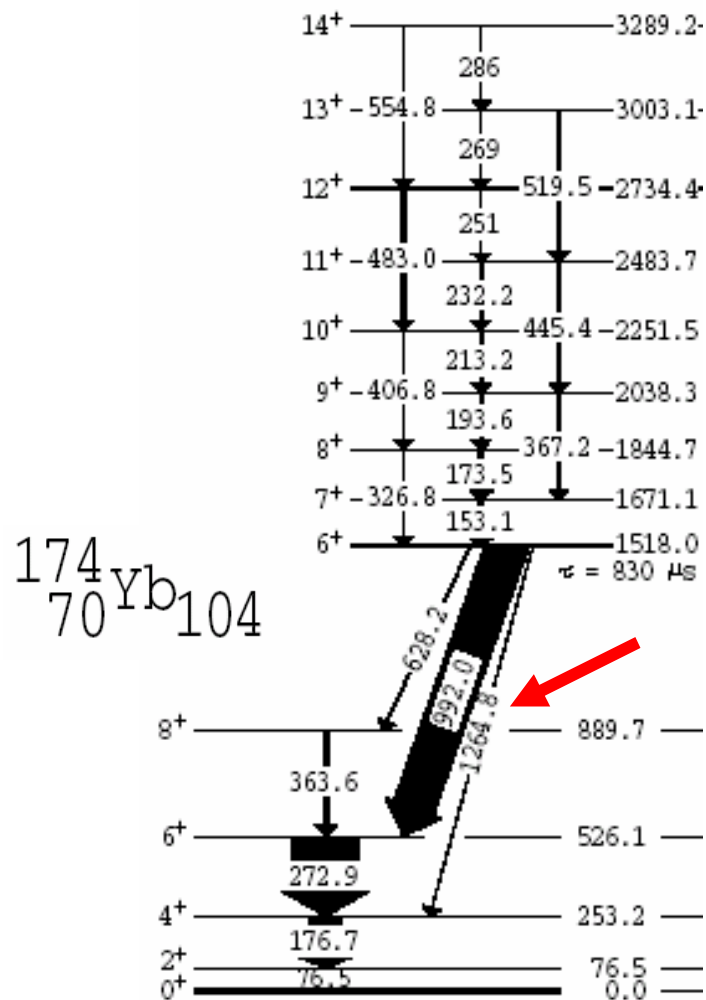


# Löbner systematics



Löbner, *Phys. Lett. B* 26 (1968) 369

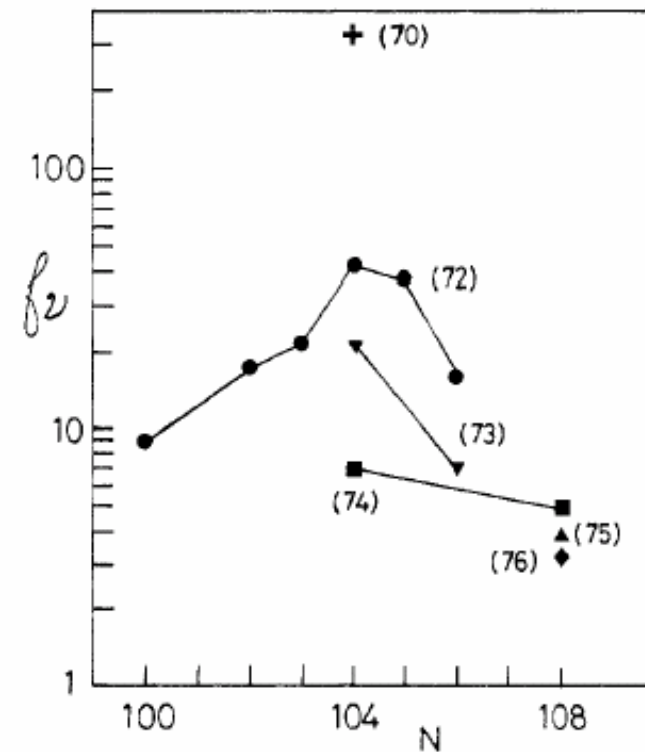
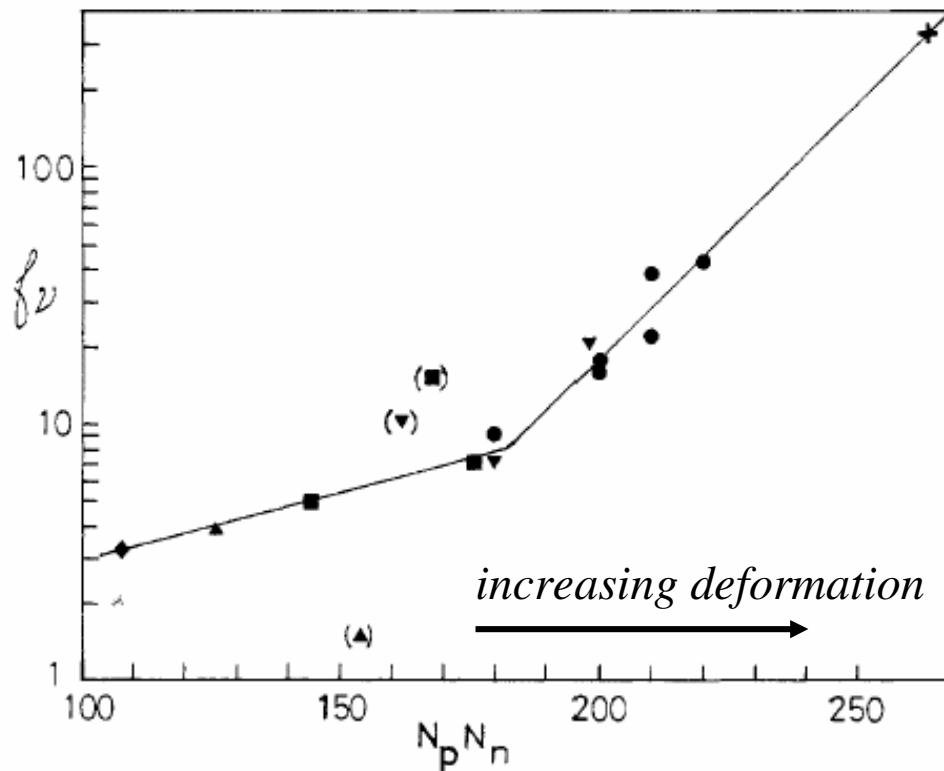
# 2- and 3-qp E2 reduced hindrances



Walker, J. Phys.  
G16 (1990) L233

Dracoulis et al., Phys. Rev. C71 (2005) 044326

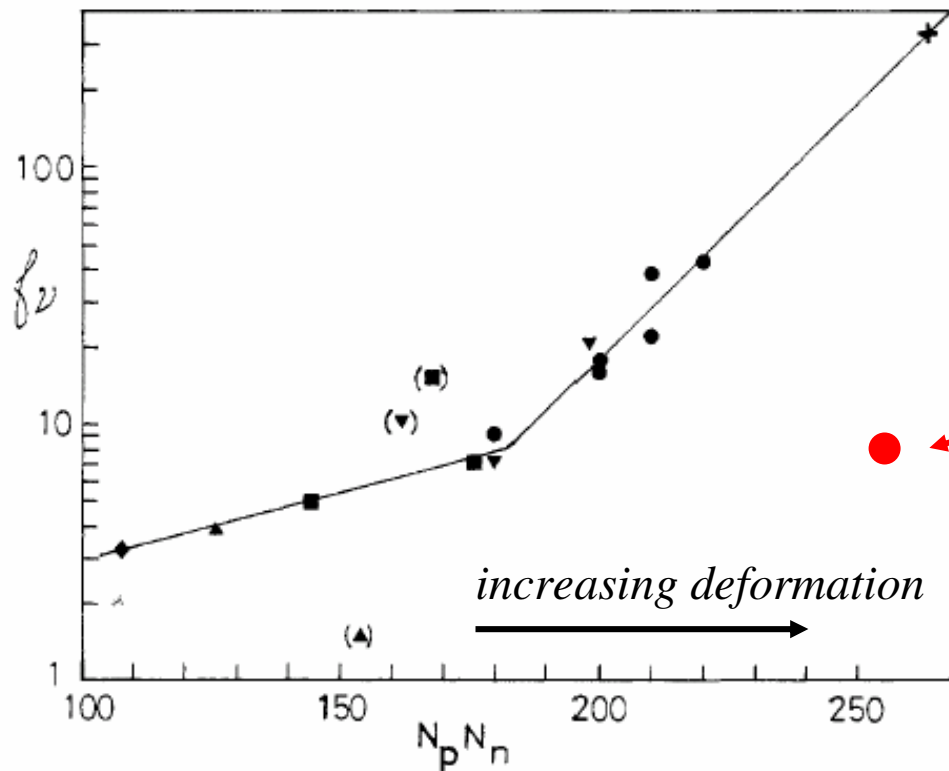
## 2- and 3-qp E2 reduced hindrances



$N_p N_n$ : product of valence  
nucleon numbers, e.g.  $^{174}\text{Yb}$  (+)  
has  $Z=70$ ,  $N_p=12$ ;  $N=104$ ,  $N_n=22$   
 $\Rightarrow N_p N_n=264$

Walker, *J. Phys.*  
*G16* (1990) L233

## 2- and 3-qp E2 reduced hindrances



$^{171}\text{Tm}$

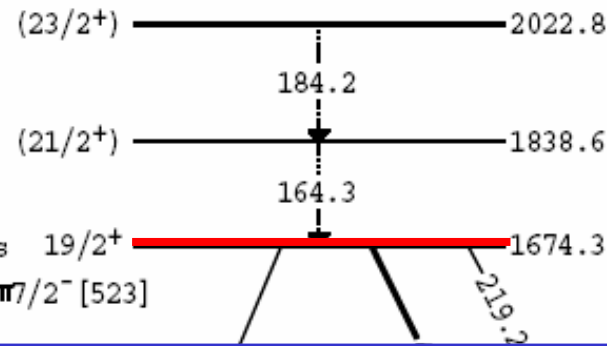
Walker et al.  
Phys. Rev. C79  
(2009) 044321

$N_p N_n$ : product of valence  
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has  $Z=70$ ,  $N_p=12$ ;  $N=104$ ,  $N_n=22$   
 $\Rightarrow N_p N_n=264$

$^{171}\text{Tm}$

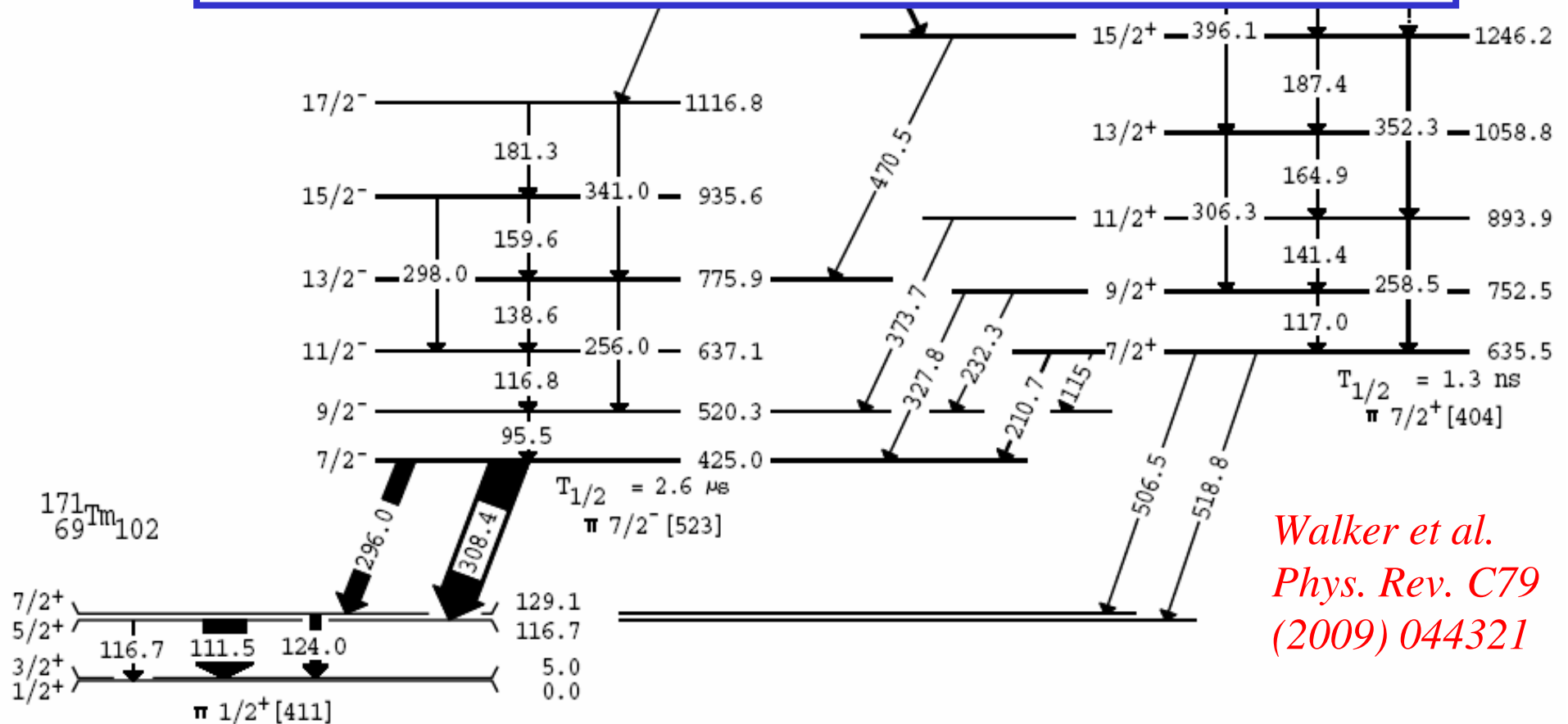
$1.7 \mu\text{s}$

$T_{1/2} = 1.7 \mu\text{s}$   
 $\nu 5/2^- [512], 7/2^+ [633] \otimes \pi 7/2^- [523]$



$\Delta E = 11 \text{ keV (V=12 eV)}$

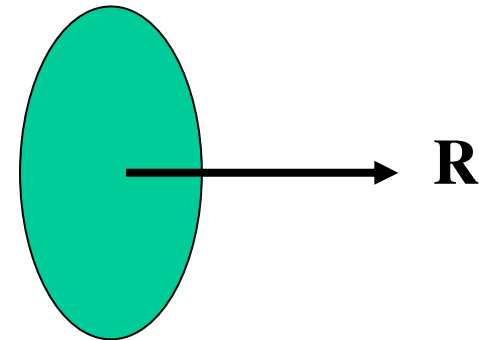
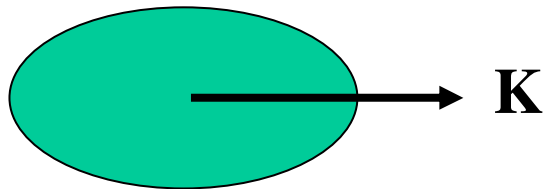
chance near-degeneracy of two  $19/2^+$  levels



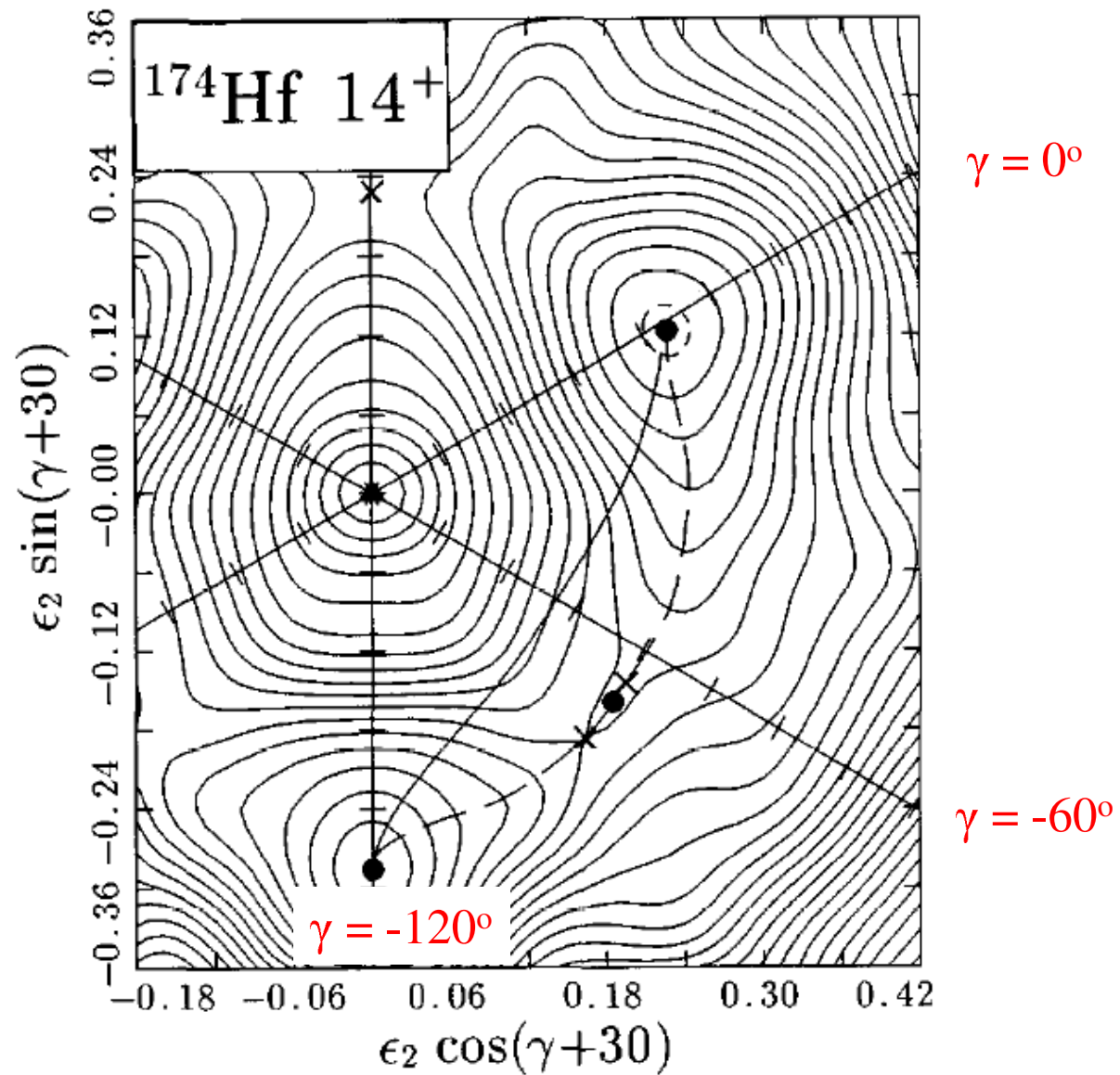
*Walker et al.*  
*Phys. Rev. C79*  
*(2009) 044321*

# K-mixing mechanisms

- chance near-degeneracies – hard to predict!
- Coriolis mixing (rotational – orientation change)  
larger deformation ( $N_p N_n$ )  $\Rightarrow$  less Coriolis mixing
- $\gamma$  tunnelling (vibrational – shape change)
- level density (thermal – statistical)



# $\gamma$ tunnelling

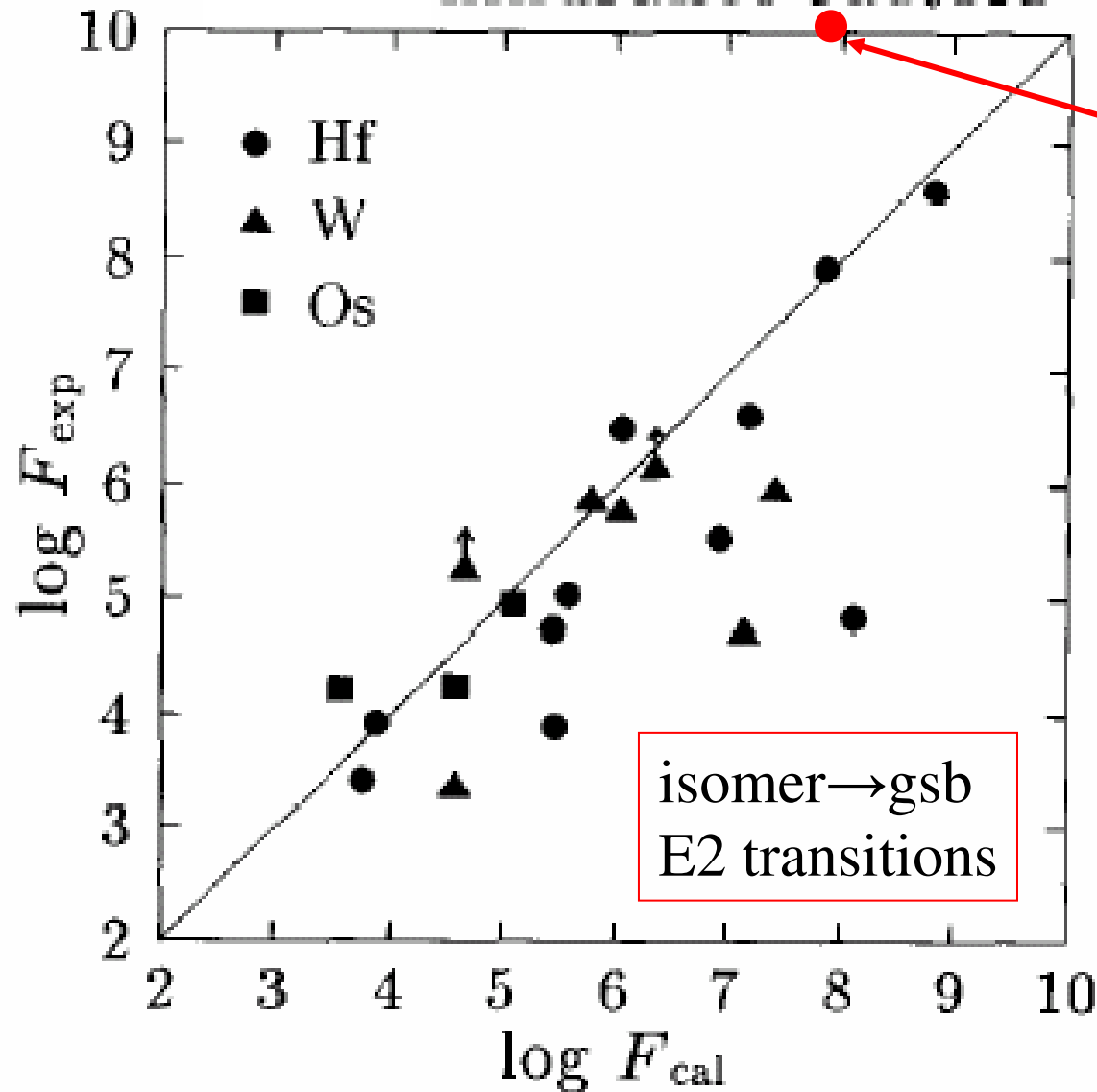


*Narimatsu et al.,  
Nucl. Phys. A601  
(1996) 69*

K. Narimatsu et al./Nuclear Physics A 601 (1996) 69–88

## $\gamma$ -tunnelling description of K-isomer decay

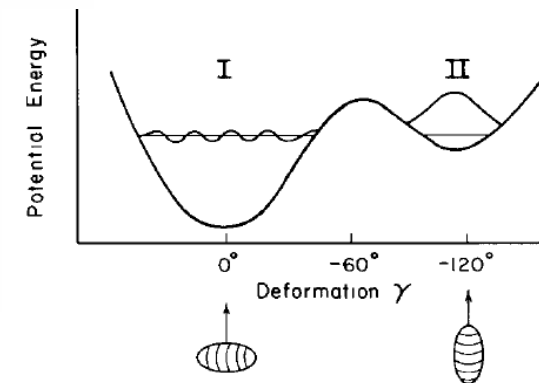
### E2 hindrance factors



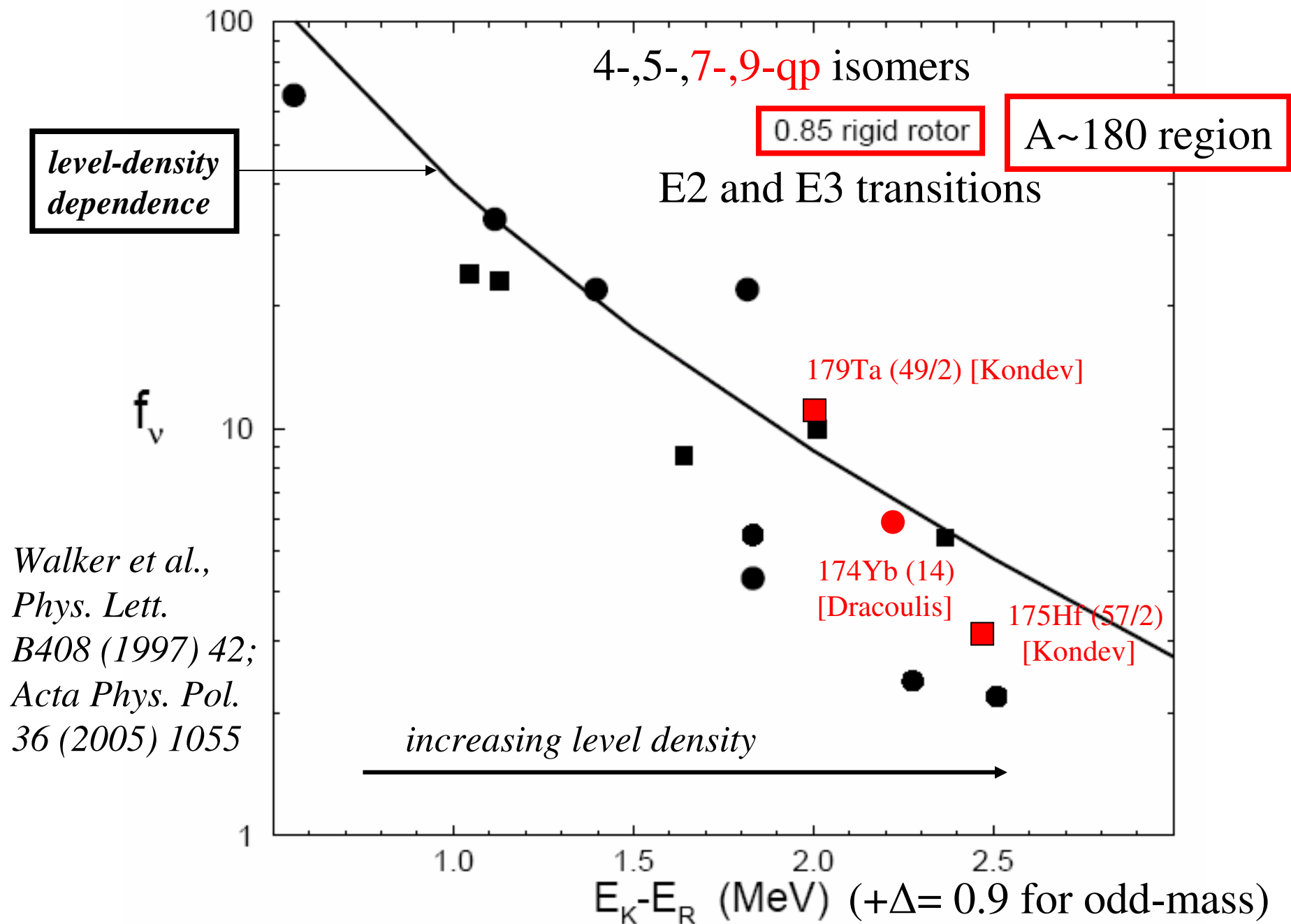
A~180 region

$^{174}\text{Yb}$  (K=6)

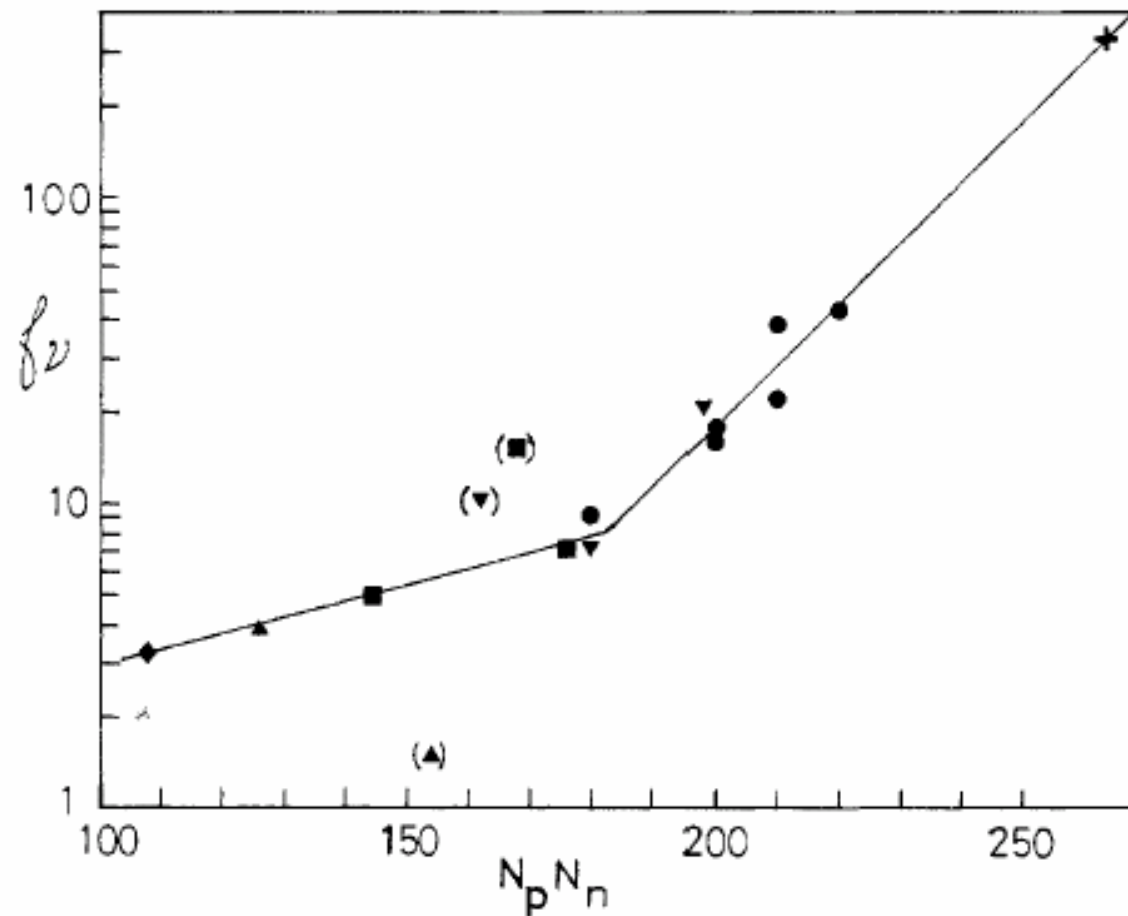
see Dracoulis et al.  
*Phys. Rev. C* 71  
(2005) 044326



Chowdhury et al.,  
*Nucl. Phys. A* 485  
(1988) 136



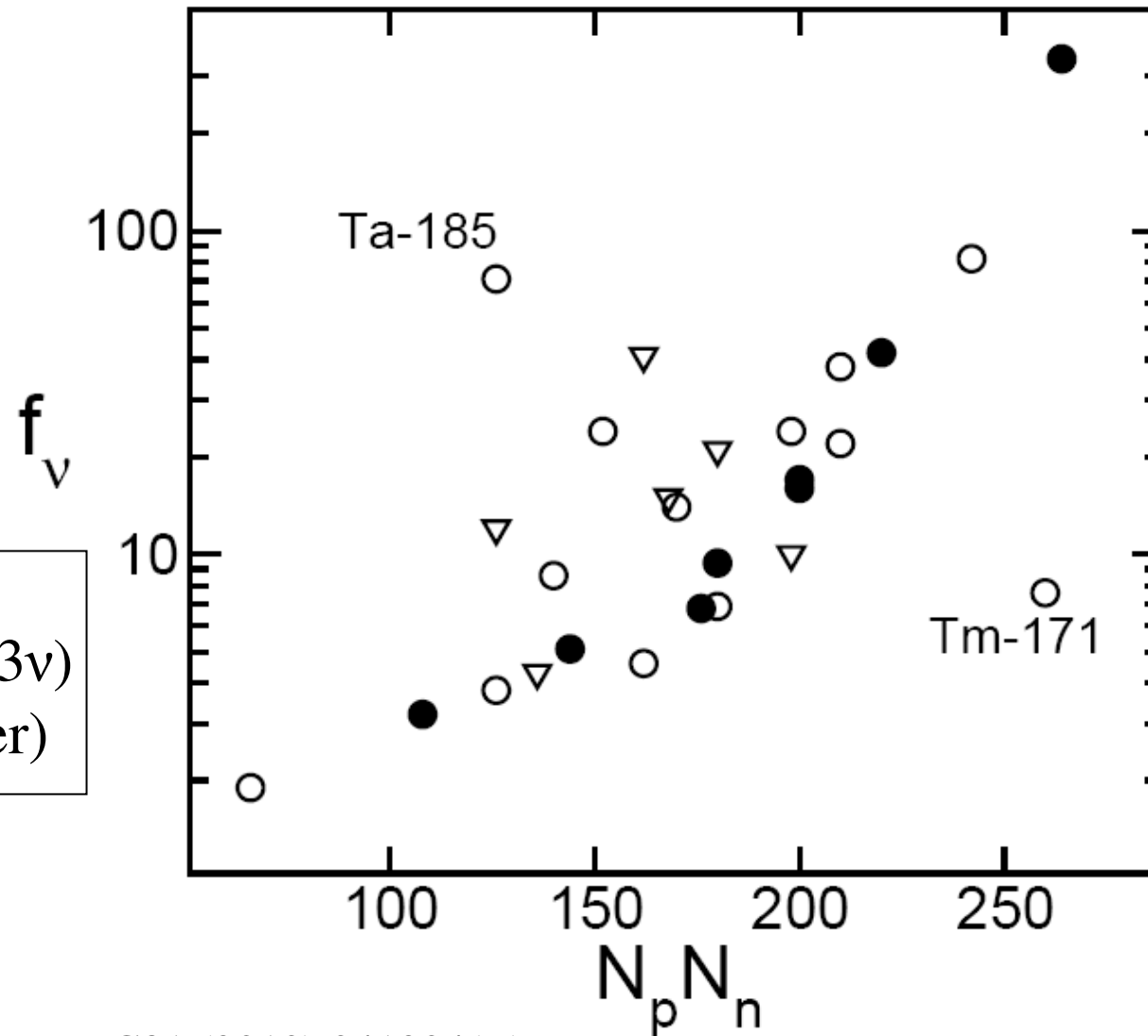
back to 2- and 3-qp isomers



# back to 2- and 3-qp isomers

$^{185}\text{Ta}$ :  
Lane et al.,  
Phys. Rev. C80  
(2009) 024321

● 2-qp  
▽ 3-qp ( $3\pi, 3\nu$ )  
○ 3-qp (other)



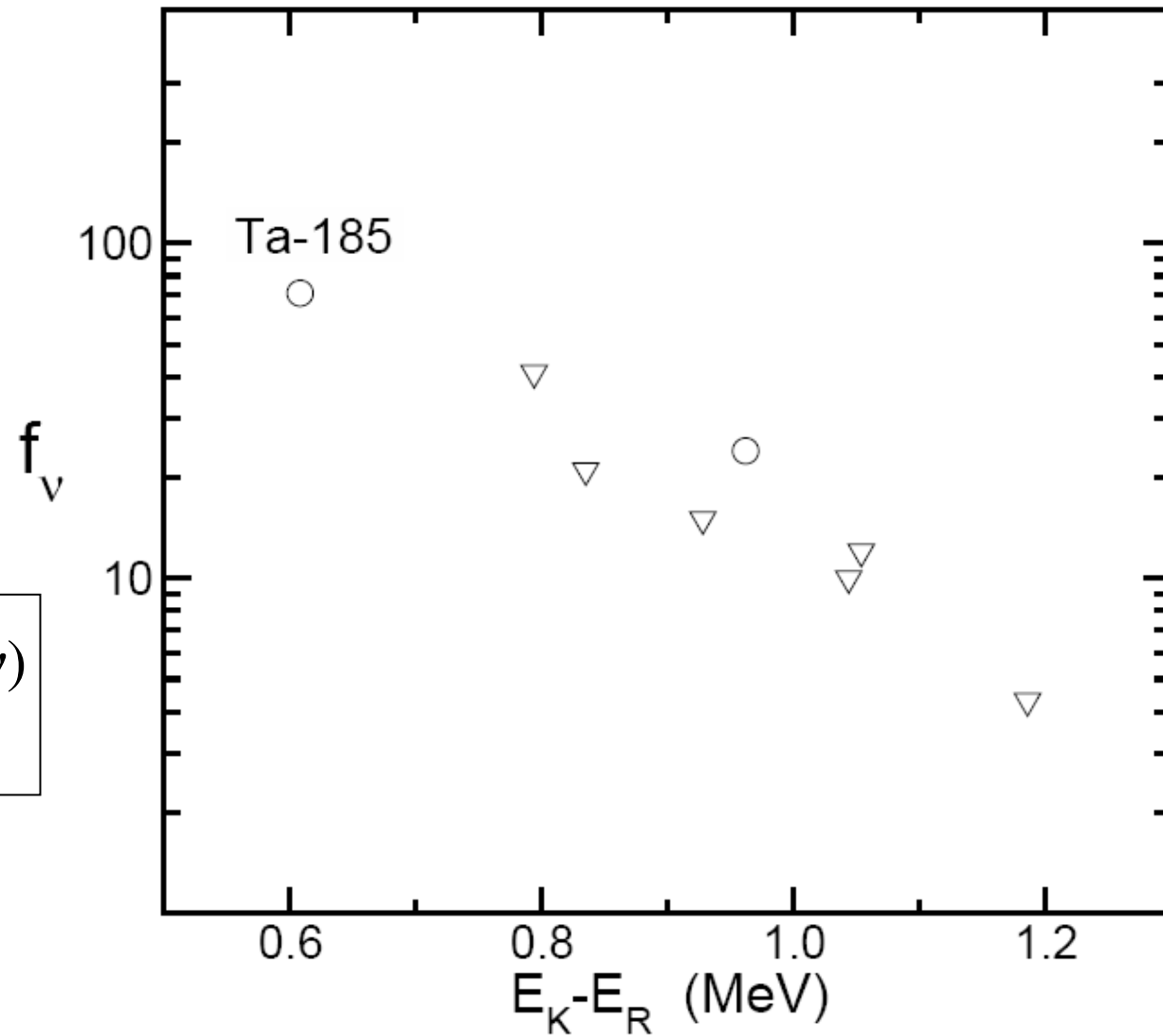
Walker et al., Phys. Rev. C81 (2010) 041304(R)

# back to 2- and 3-qp isomers

$^{185}\text{Ta}$ :

Lane et al.,  
Phys. Rev. C80  
(2009) 024321

$\nabla$  3-qp ( $3\pi, 3\nu$ )  
 $\circ$  3-qp (other)



Walker et al., Phys. Rev. C81 (2010) 041304(R)

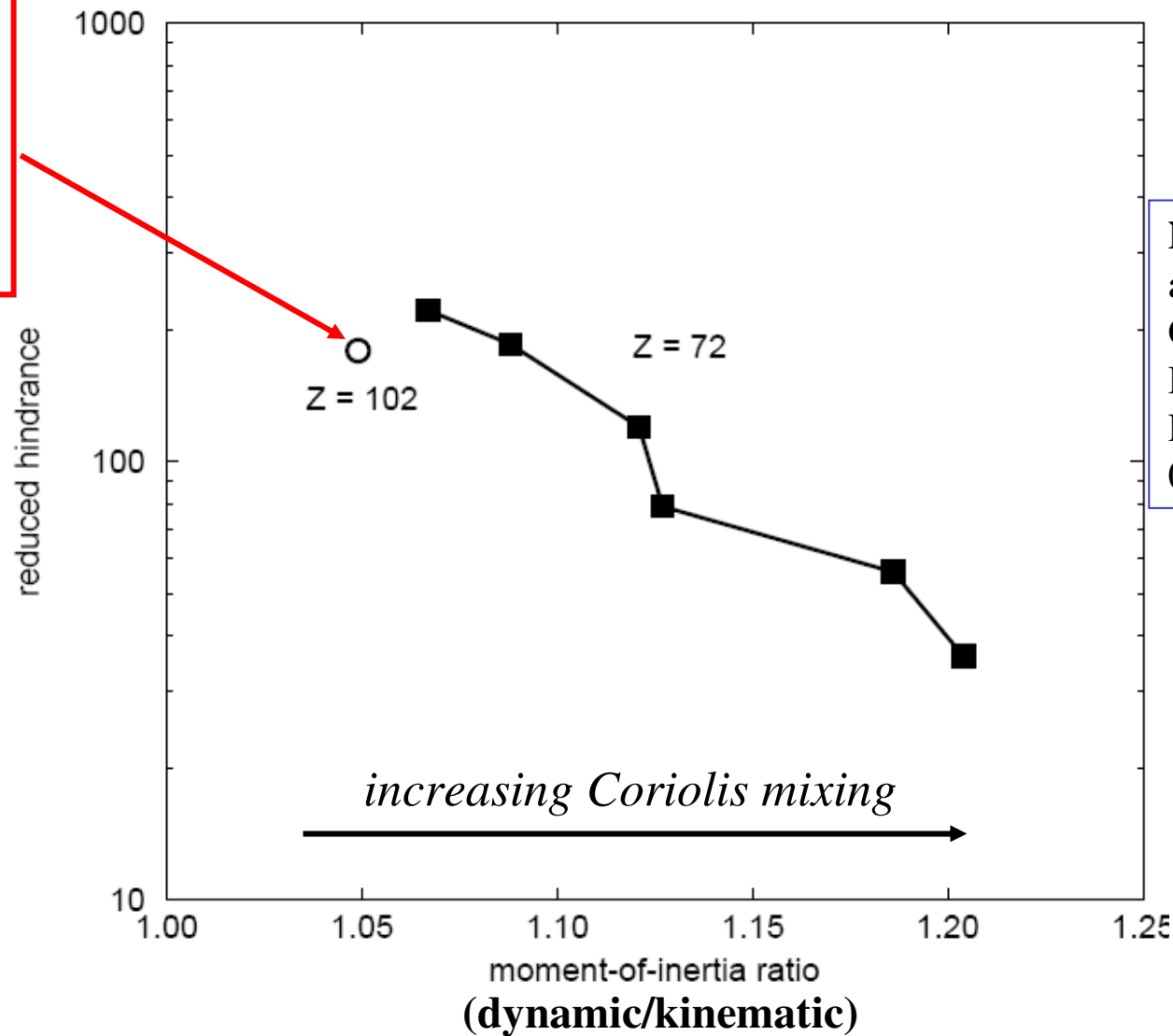
Where next?

# Where next?

- need for quantitative theory
- compare with other mass regions
- make and test predictions for exotic nuclei

# $K^\pi = 8^-$ isomers, E1 decays ( $\nu = 7$ )

$^{252}\text{No}$   
Sulignano  
et al.  
EPJA33  
(2007) 327



**N=106** and  
allowance for  
Coriolis mixing:  
Dracoulis et al.,  
PRC79 (2009)  
061303(R)

*extends analysis of Walker et al., Phys. Rev. C49 (1994) 1718*

# 2-qp E2 reduced hindrances

even-even nuclides,  $K^\pi = 6^+, 10^+$  isomers

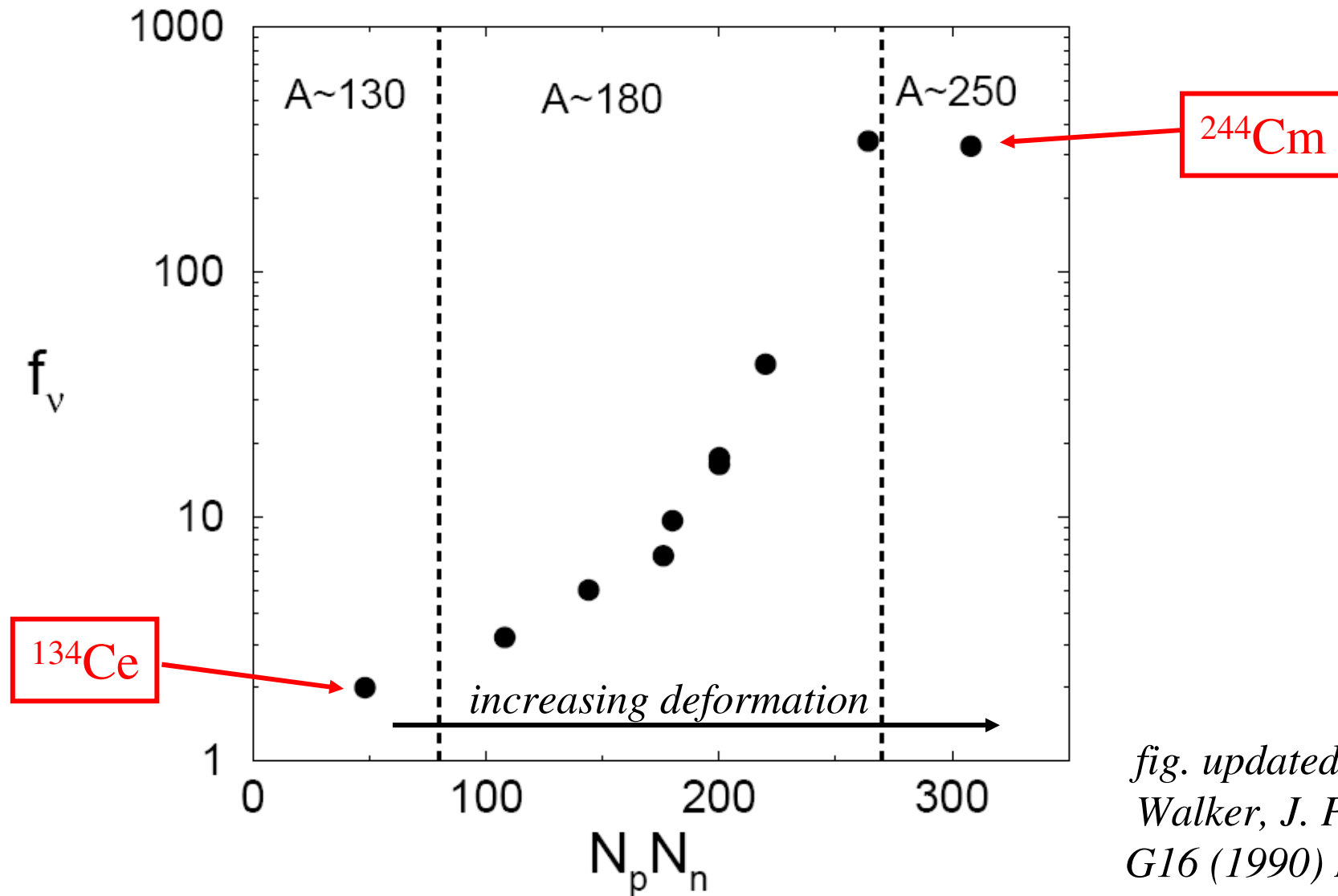
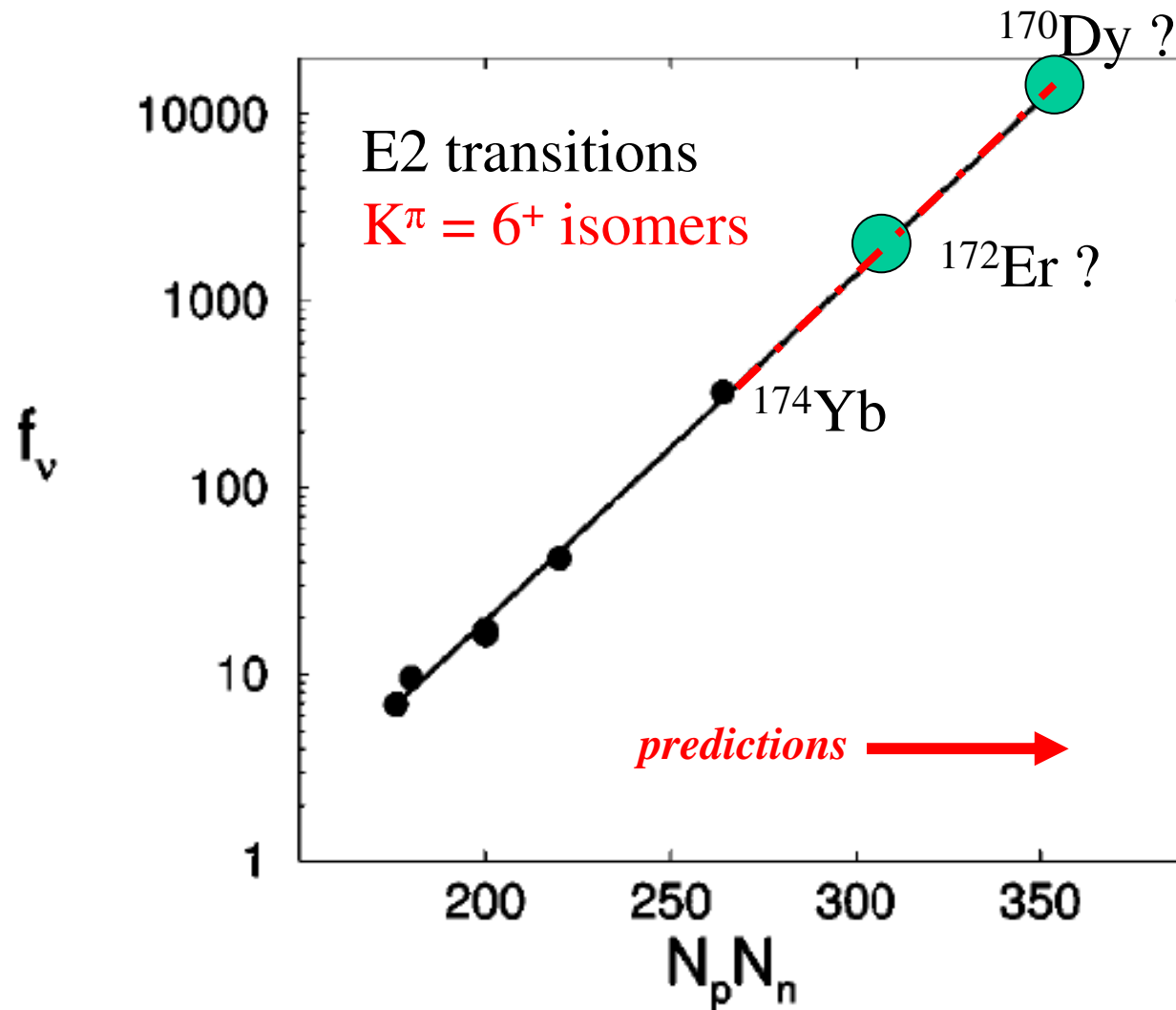


fig. updated from  
Walker, J. Phys.  
G16 (1990) L233

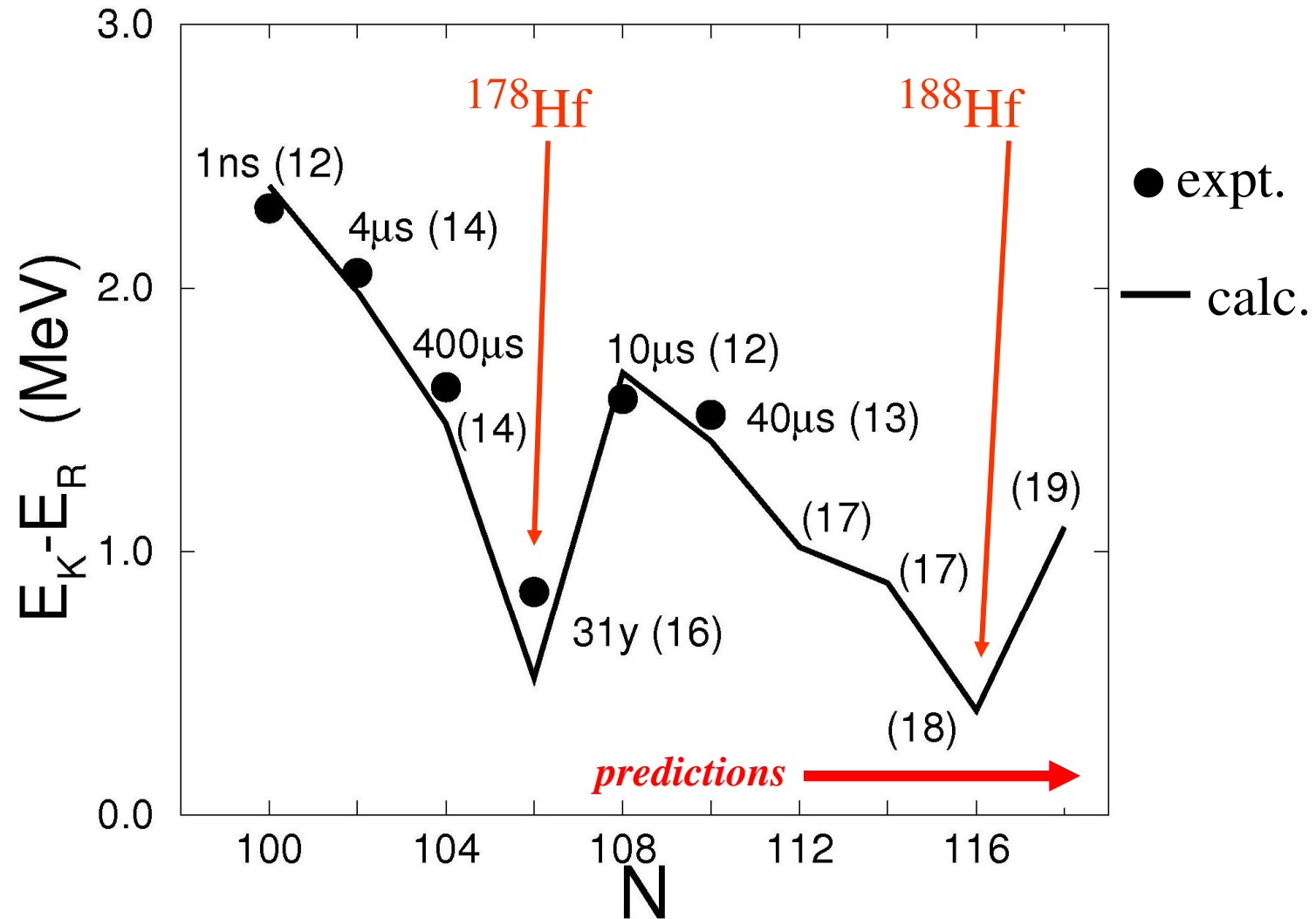
# $^{170}\text{Dy}$ : doubly mid-shell

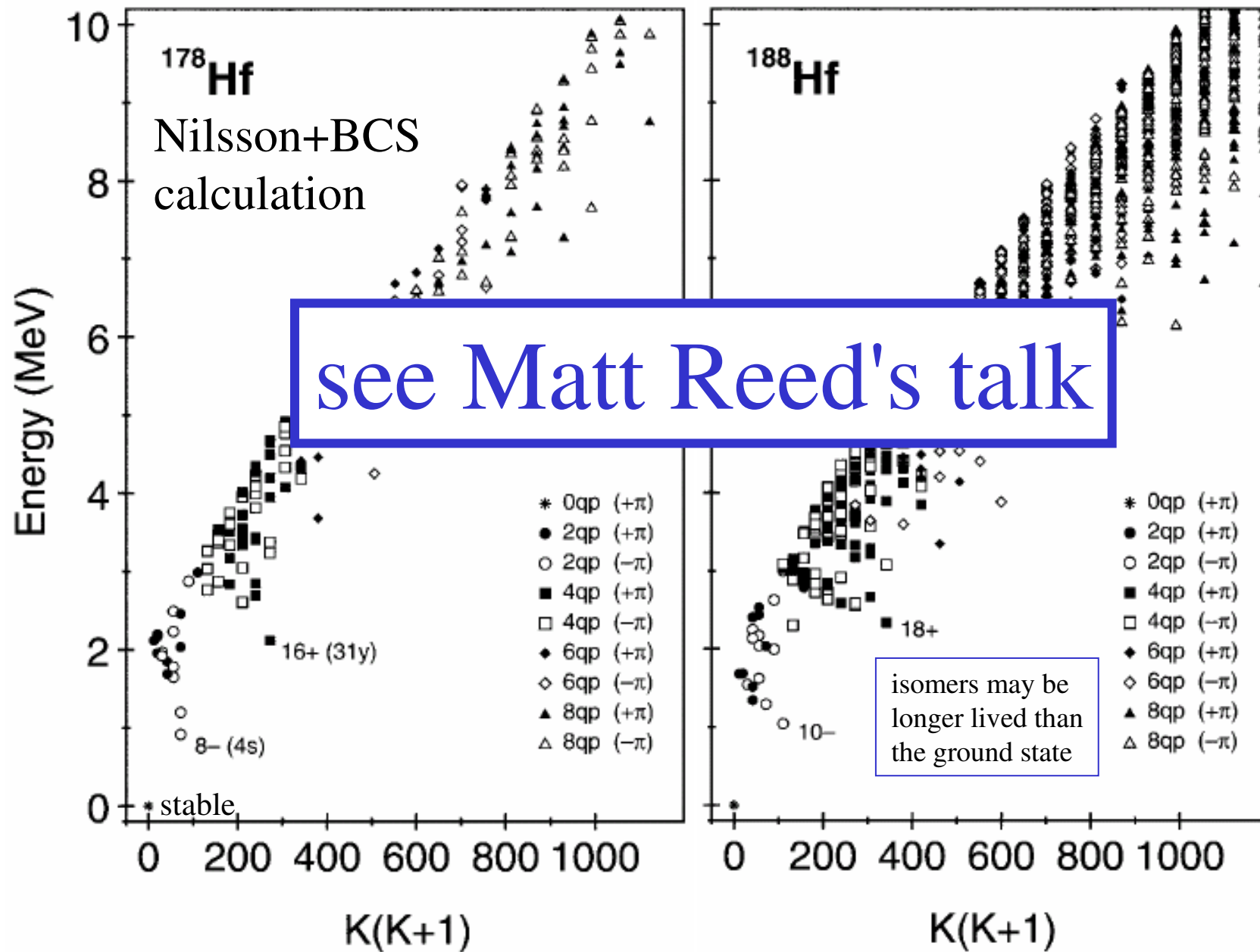


*P.H. Regan et al.,  
Phys. Rev. C65  
(2002) 037302*

*A.K. Rath et al.,  
Phys. Rev. C68  
(2003) 044315*

# hafnium ( $Z=72$ ) 4-qp isomers





[Walker and Dracoulis, *Hyp. Int.* 135 (2001) 83]

## Summary

### K isomers & K mixing

$f_v$  dependence:  $N_p N_n$  (E2 transitions, 2-qp)

Coriolis effects

$\gamma$  tunnelling

level-density (mqp)

chance near-degeneracy

*theory needed, but predictions possible*

n-rich predictions – long-lived isomers