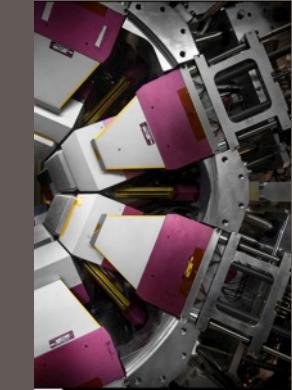


# Lifetime Measurements for the Determination of Electric Monopole Transition Strengths

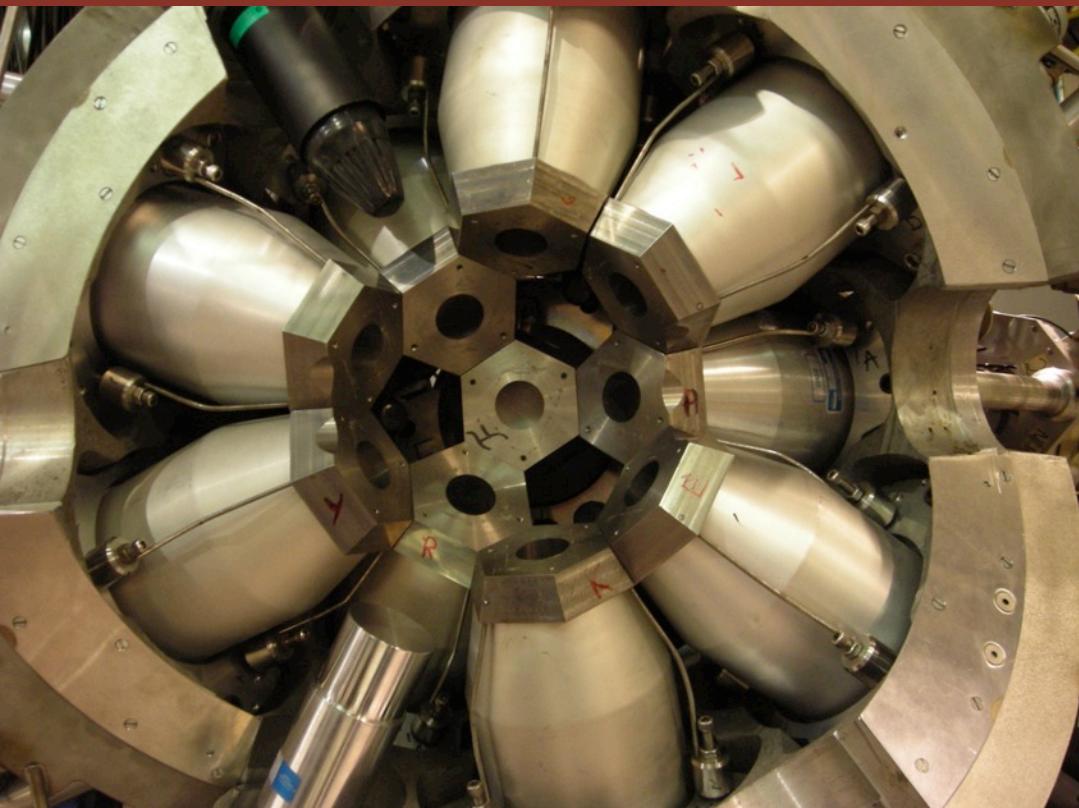


**Adam Garnsworthy | Research Scientist | TRIUMF**

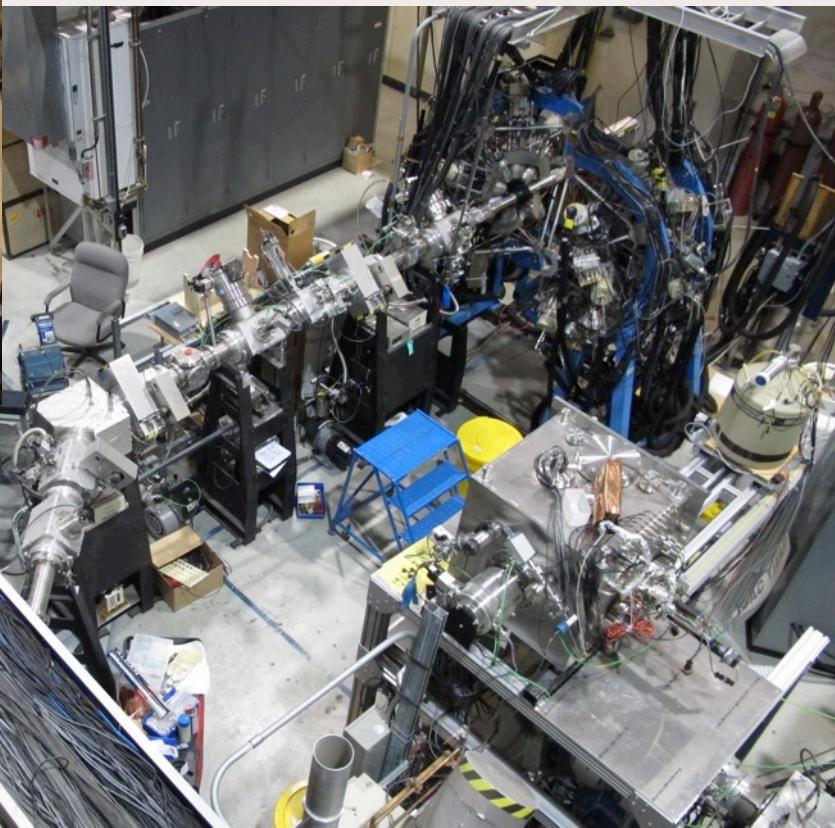
Accelerating Science for Canada  
Un accélérateur de la démarche scientifique canadienne

Owned and operated as a joint venture by a consortium of Canadian universities via a contribution through the National Research Council Canada  
Propriété d'un consortium d'universités canadiennes, géré en co-entreprise à partir d'une contribution administrée par le Conseil national de recherches Canada

# The $8\pi$ Spectrometer at TRIUMF-ISAC



Performed decay spectroscopy at TRIUMF-ISAC-I from Feb 2002 to Dec 2013



Researchers from 24 institutions from 8 countries.

>25 post-docs,  
5PhD, 12MSc, 1MPHys  
12 Grad. Students in progress

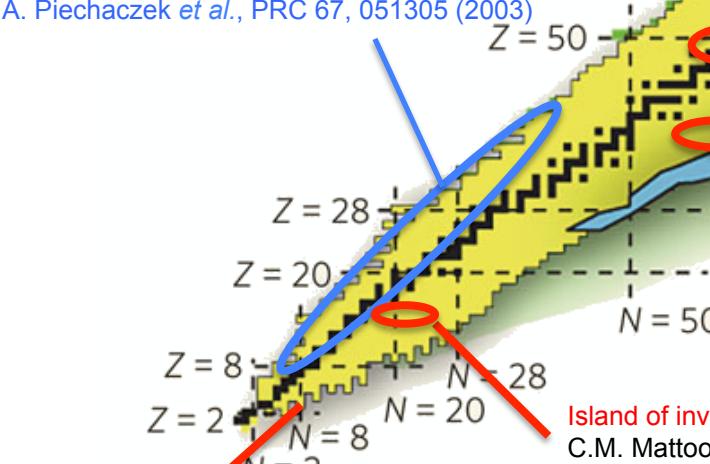


# The $8\pi$ Spectrometer at TRIUMF-ISAC

35 publications including 4 PRLs  
 22 on Nuclear Structure  
 13 on Superallowed beta decay

## Superallowed Beta Decay

- $^{10}\text{C}$ ,  $^{14}\text{O}$ ,  $^{18}\text{Ne}$ ,  $^{19}\text{Ne}$ ,  $^{26m}\text{Al}$ ,  $^{38m}\text{K}$ ,  $^{62}\text{Ga}$ ,  $^{74}\text{Rb}$   
 $\text{R. Dunlop et al., PRC 88, 045501 (2013)}$
- $\text{G.F. Grinyer et al., PRC 87, 045502 (2013)}$
- $\text{A.T. Laffoley et al., PRC 88, 015501 (2013)}$
- $\text{P. Finlay et al., PRC 85, 055501 (2012)}$
- $\text{S. Triambak et al., PRL 109, 042301 (2012)}$
- $\text{P. Finlay et al., PRC 78, 025502 (2008)}$
- $\text{K.G. Leach et al., PRL 100, 192504 (2008)}$
- $\text{G.F. Grinyer et al., PRC 76, 025503 (2007)}$
- $\text{E.F. Zganyar et al., Acta Phys.Pol. B38, 1179 (2007)}$
- $\text{B. Hyland et al., PRL 97, 102501 (2006)}$
- $\text{B. Hyland et al., AIP Conf.Proc. 819, 105 (2006)}$
- $\text{G.F. Grinyer et al., PRC 71, 044309 (2005)}$
- $\text{A. Piechaczek et al., PRC 67, 051305 (2003)}$



## $^{11}\text{Li}$ beta-delayed neutron emission

- $\text{C.M. Mattoon et al., PRC 75, 017302 (2007)}$

## High-statistics studies of Cd, Sn, Xe

- $\text{A.J. Radich et al., Submitted to PRC (2015)}$
- $\text{P.E. Garrett et al., PRC 86, 044304 (2012)}$
- $\text{P.E. Garrett et al., Acta Phys.Pol. B42, 799 (2011)}$
- $\text{P.E. Garrett et al., AIP Conf.Proc. 1377, 211 (2011)}$
- $\text{K.L. Green et al., PRC 80, 032502 (2009)}$

## Half Life of geochronometer, $^{176}\text{Lu}$

- $\text{G.F. Grinyer et al., PRC 67, 014302 (2003)}$

## Structure of $^{219-223}\text{Rn}$ towards a RnEDM search

## Isomer decay in $^{174}\text{Tm}$ , $^{178}\text{Hf}$ , $^{179}\text{Lu}$

- $\text{R.S. Chakraworthy et al., PRC 73, 024306 (2006)}$
- $\text{R.S. Chakraworthy et al., EPJ. A 25, S1, 125 (2005)}$
- $\text{M.B. Smith et al., NPA746, 617c (2004)}$
- $\text{M.B. Smith et al., PRC 68, 031302 (2003)}$

## Large Beta-Delayed neutron branching ratio observed from $^{102}\text{Rb}$

- $\text{Z.M.Wang, A.B. Garnsworthy et al., Submitted to PRC (2015)}$
- $\text{A. Chakraborty et al., PRL 110, 022504 (2013)}$

## Shape coexistence in neutron-rich Sr, Zr

- $\text{A. Chakraborty et al., PRL 110, 022504 (2013)}$

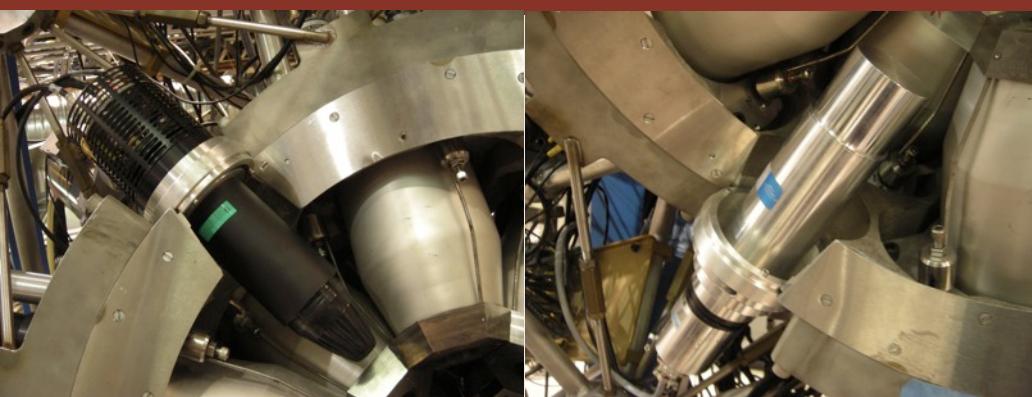
## Island of inversion, $^{32}\text{Mg}$

- $\text{C.M. Mattoon et al., PRC 80, 034318 (2009)}$
- $\text{F. Sarazin et al., PRC 70, 031302 (2004)}$

## Overviews/Technical

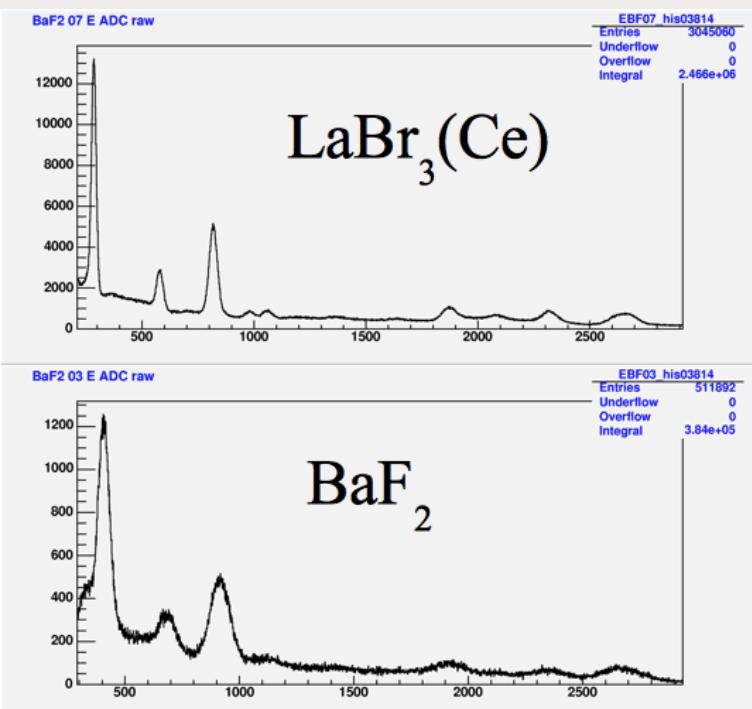
- $\text{A.B.Garnsworthy, Submitted to EPJ Web of Conf.s (2014)}$
- $\text{A.B. Garnsworthy and P.E. Garrett, Hyp. Int. 225, 121 (2014)}$
- $\text{G.C. Ball et al., J.Phys.:Conf.Ser. 387, 012014 (2012)}$
- $\text{D S Cross et al., JINST 6, P08008 (2011)}$
- $\text{P.E. Garrett et al., NIM Phys.Res. B261, 1084 (2007)}$
- $\text{G.C. Ball et al., J.Phys.(London) G31, S1491 (2005)}$
- $\text{S.J. Williams et al., J.Phys.(London) G31, S1979 (2005)}$

# Di-pentagonal Array for Nuclear Timing Experiments



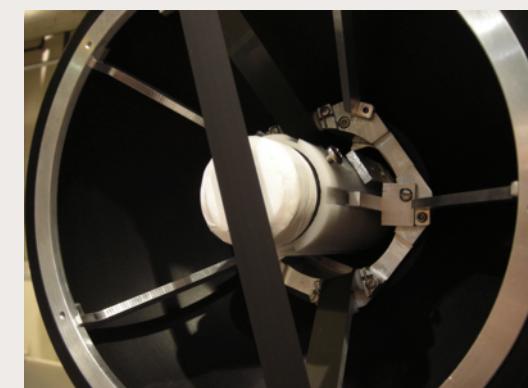
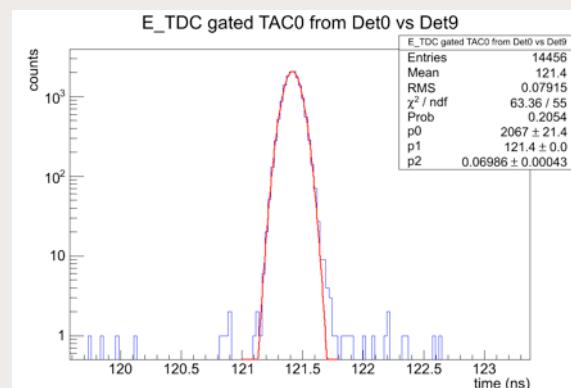
Fast-timing allows the determination of transition rates

- $\text{BaF}_2$ , truncated cone;  
base 4cm, front 2cm, length 3cm
- $\text{LaBr}_3(\text{Ce})$  2" x 2" cylinder

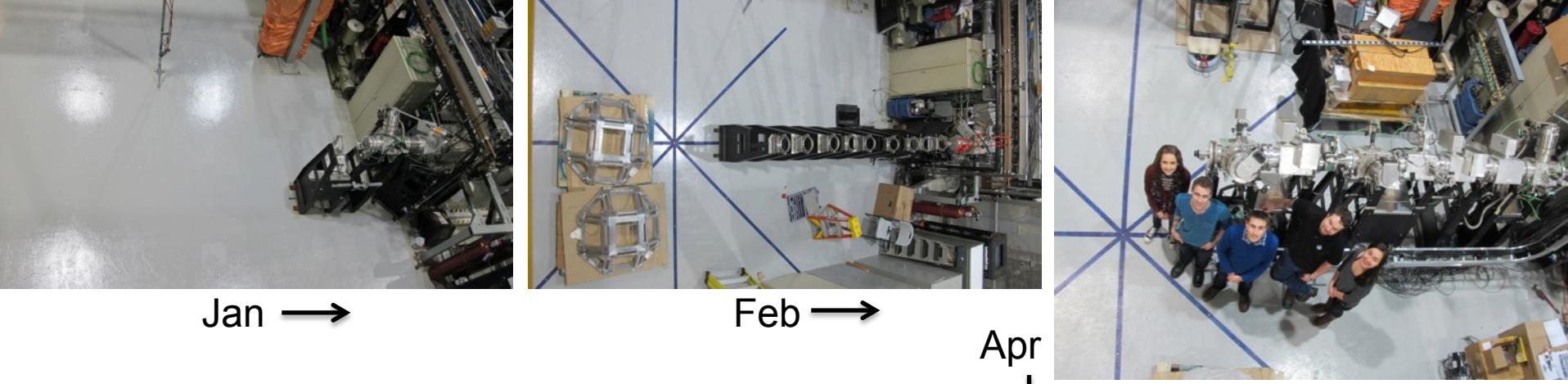


Superior Energy resolution (x3) and efficiency (x2)

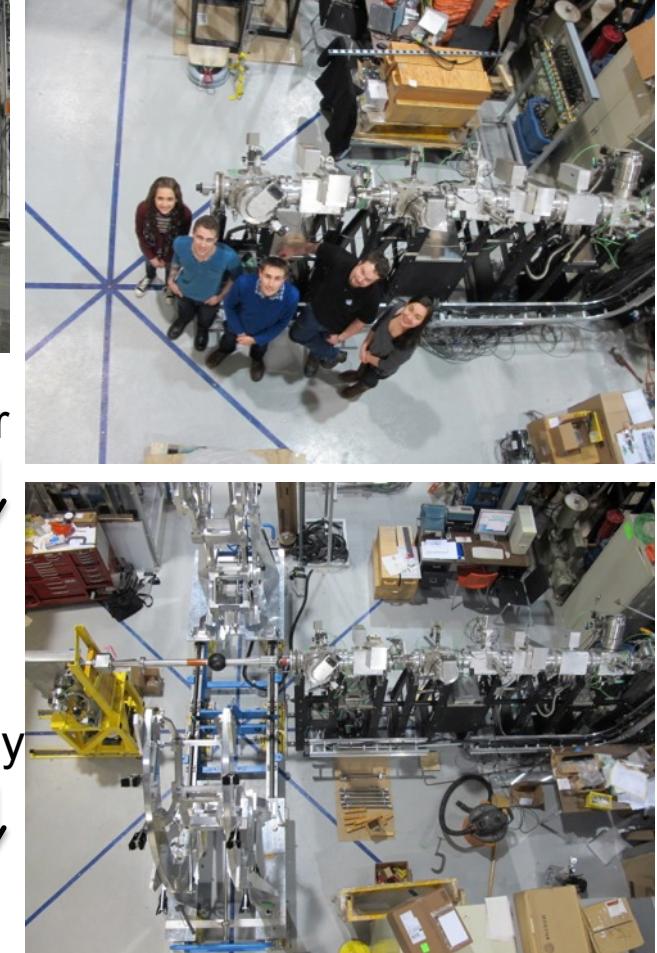
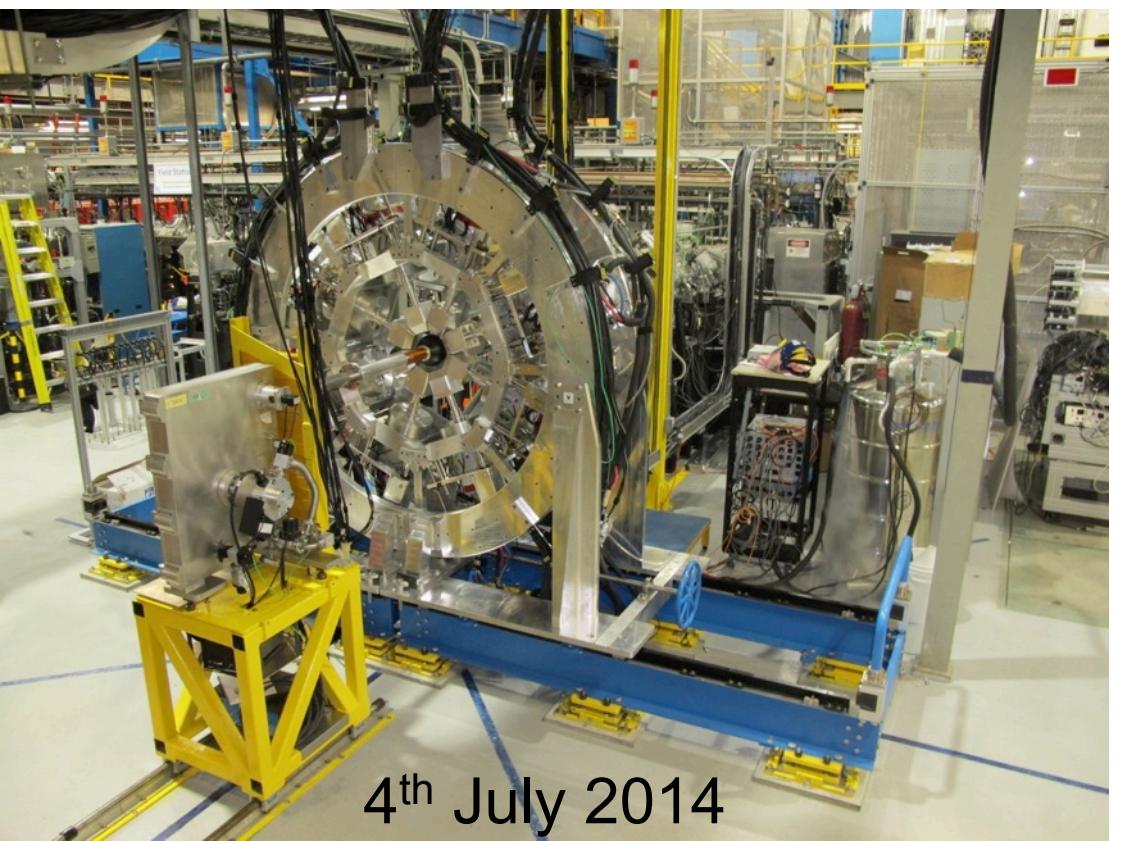
LaBr-LaBr FWHM <200 ps



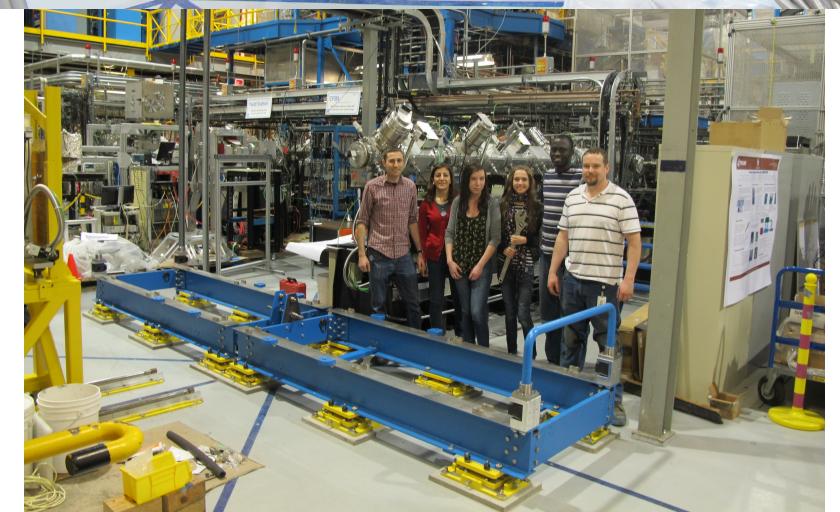
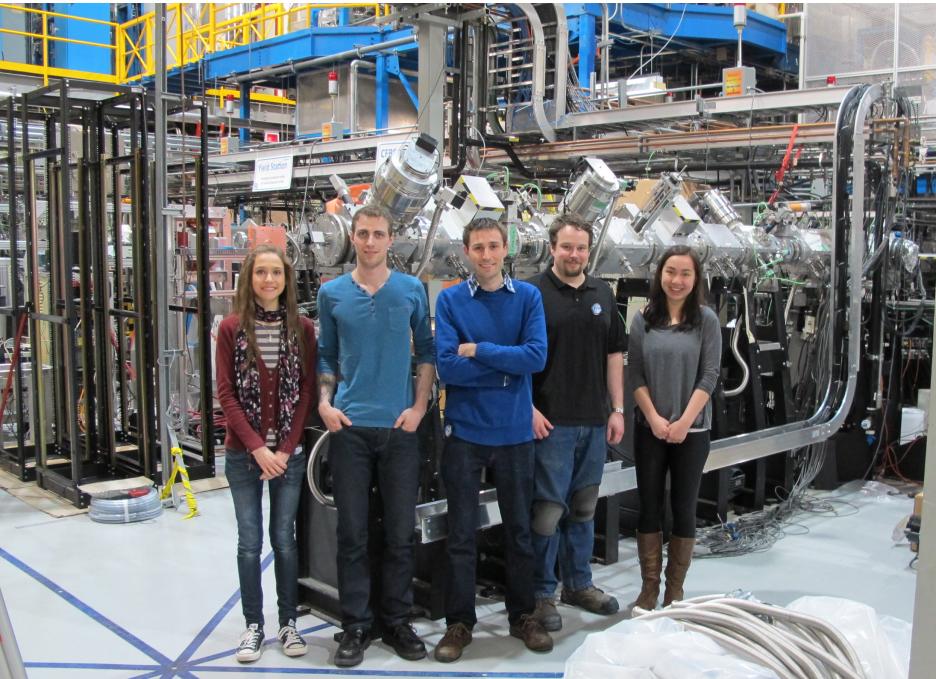
Fast Zero-degree scintillator for  $\beta$ - $\gamma$  timing. BC422Q = 0.7ns



## GRIFFIN Installation in 2014



# Surrey MPhys Student, Lisa Morrison GRIFFIN Installation in 2014





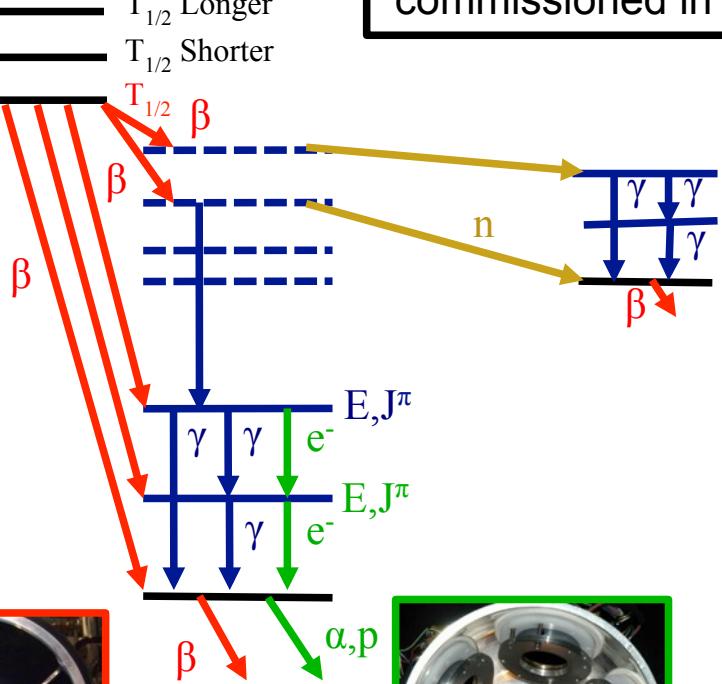
# GRiffin Facility at TRIUMF

## Sensitive Decay Spectroscopy

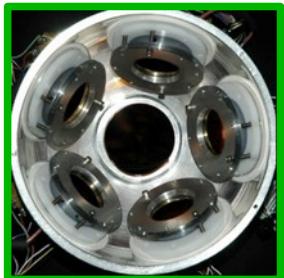
Fast, in-vacuum tape system  
Enhances decay of interest

ISOBAR  
 $J^\pi$  ISOMER  
 $J^\pi_{GS}$

—  $T_{1/2}$  Longer  
—  $T_{1/2}$  Shorter

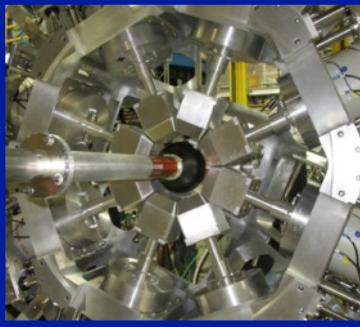


SCEPTAR: 10+10 plastic scintillators  
Detects beta decays and determines branching ratios

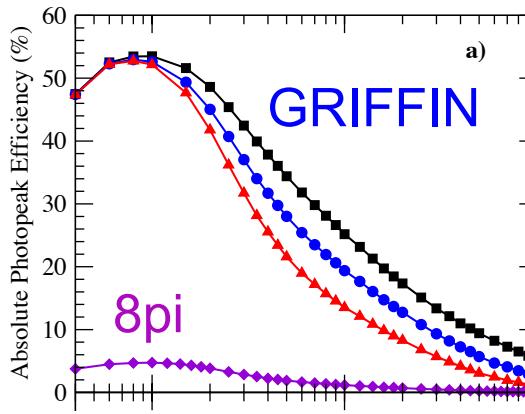


PACES: 5 Cooled Si(Li)s  
Detects Internal Conversion Electrons and alphas/protons

Initial operation in fall 2014. Fully commissioned in 2015

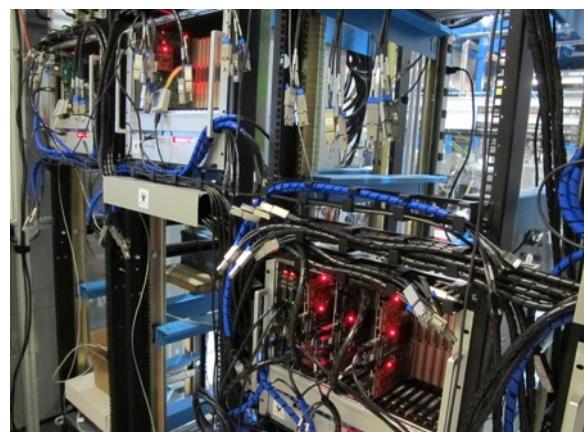


HPGe: 16 Clovers  
Detect gamma rays and determines branching ratios, multipolarities and mixing ratios



Digital DAQ

DESCANT  
Detects neutrons to measure beta-delayed neutron branching ratios



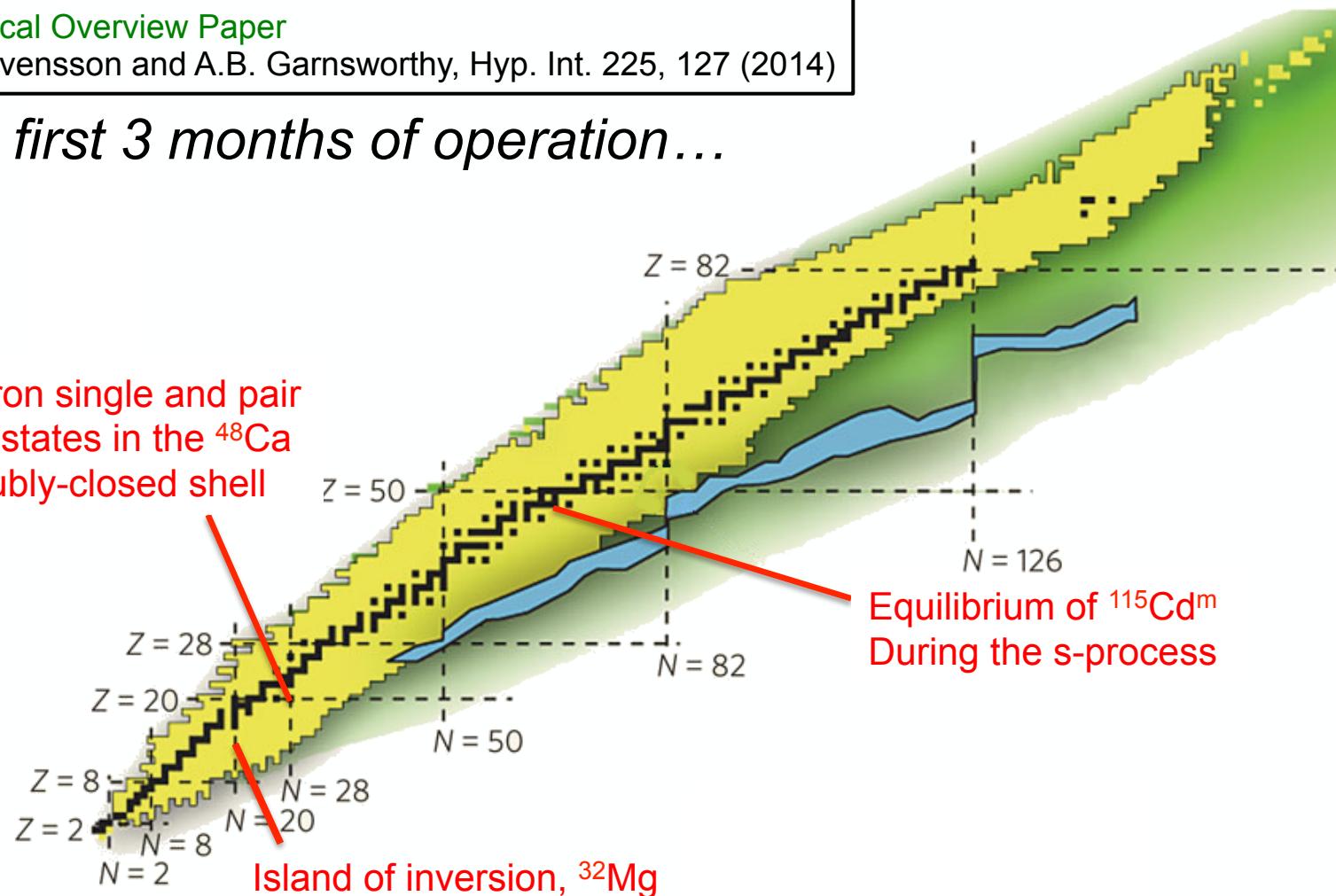
# The GRIFFIN Spectrometer at TRIUMF-ISAC

Technical Overview Paper

C.E. Svensson and A.B. Garnsworthy, Hyp. Int. 225, 127 (2014)

*The first 3 months of operation...*

Neutron single and pair  
hole states in the  $^{48}\text{Ca}$   
doubly-closed shell

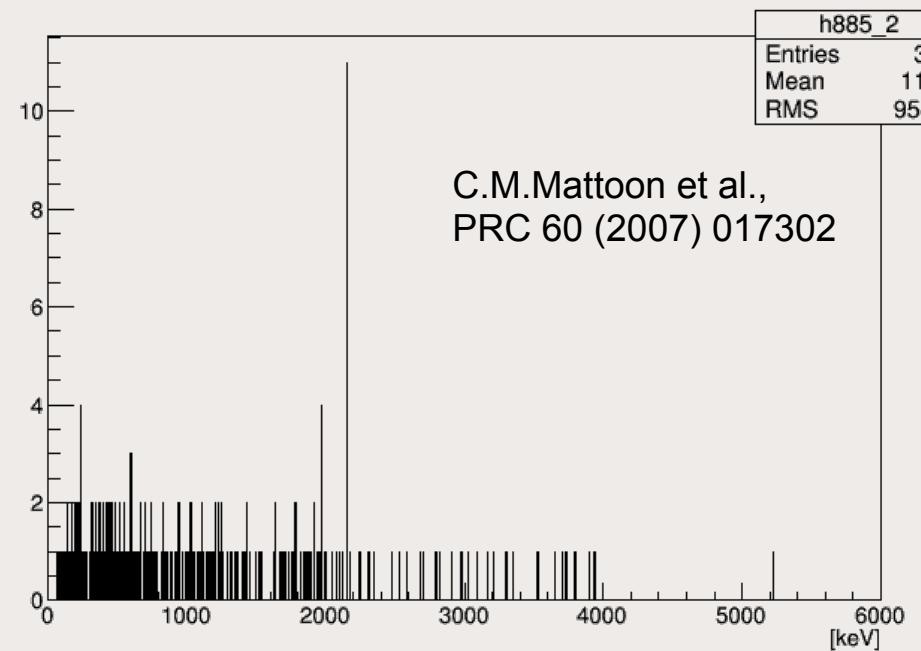
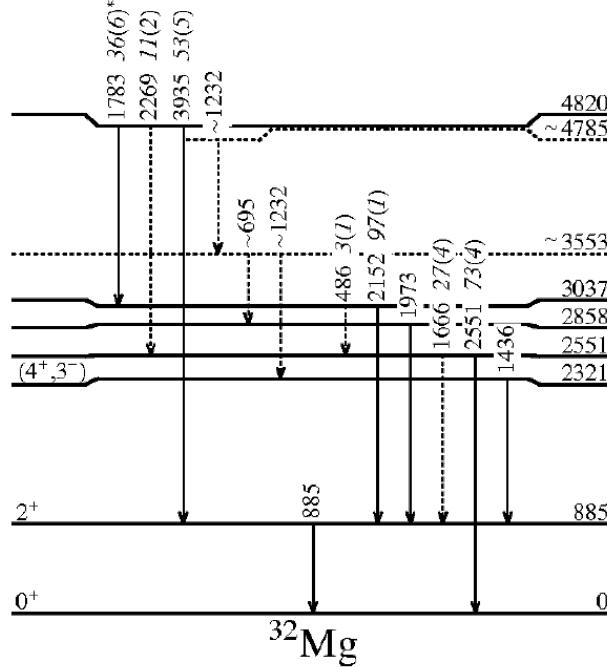


Over 70 scientists from 12 countries have now joined the collaboration

# $^{32}\text{Na}$ decay with 8pi and GRIFFIN

Fred Sarazin, Colorado School of Mines

$\gamma$ - $\gamma$  coincidences with first  
 $2^+-0^+$  transition, [883,887] keV

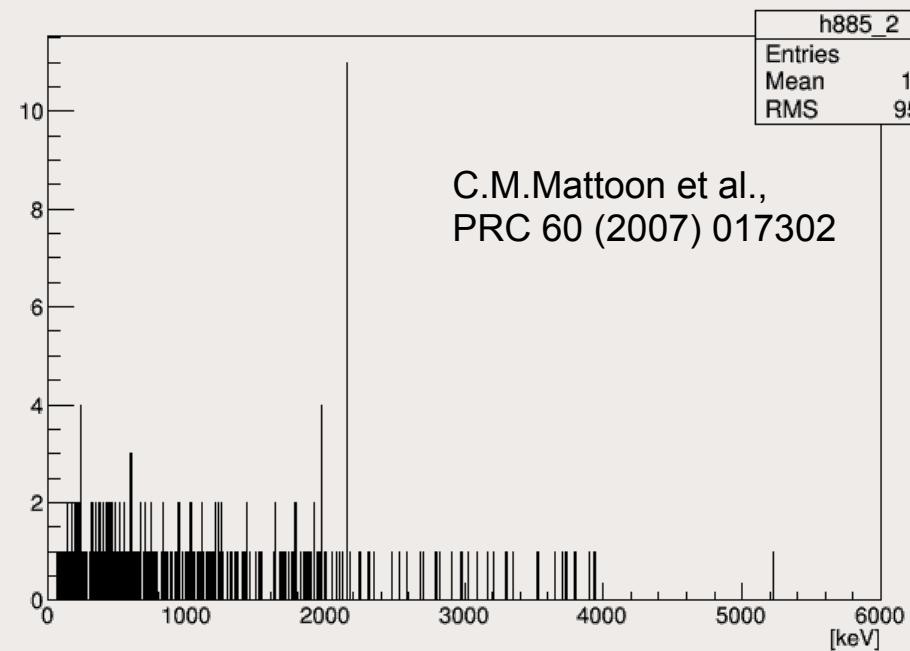
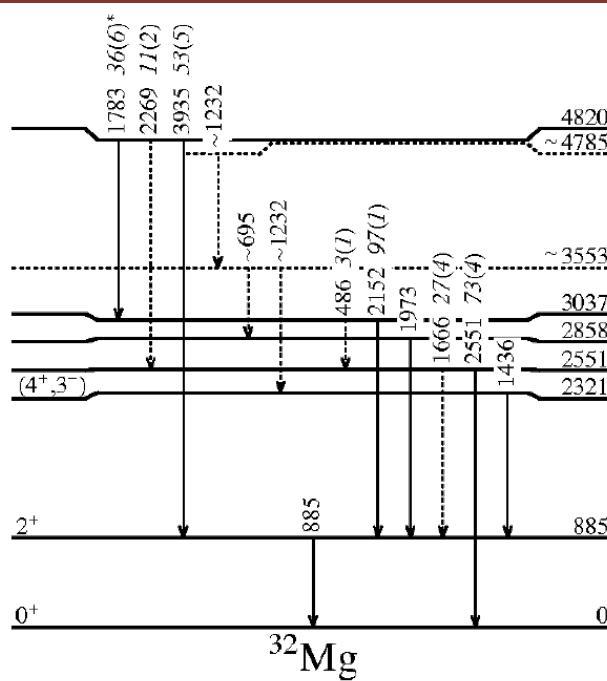


8pi: 2-3 pps, 5 days

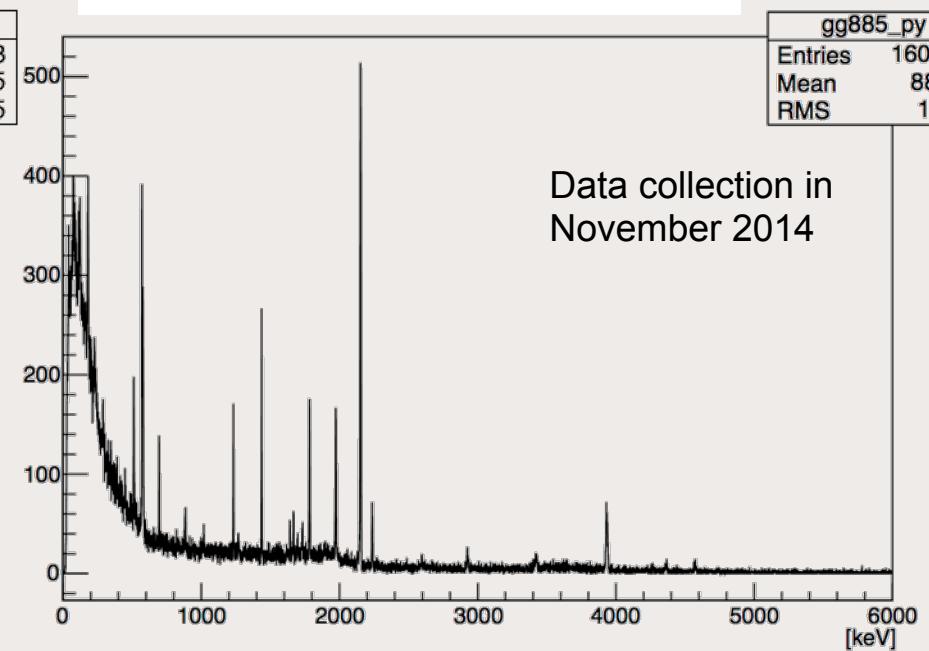
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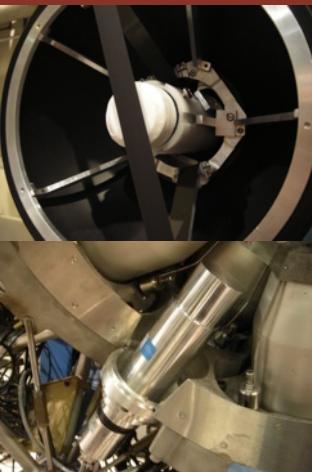


8pi: 2-3 pps, 5 days

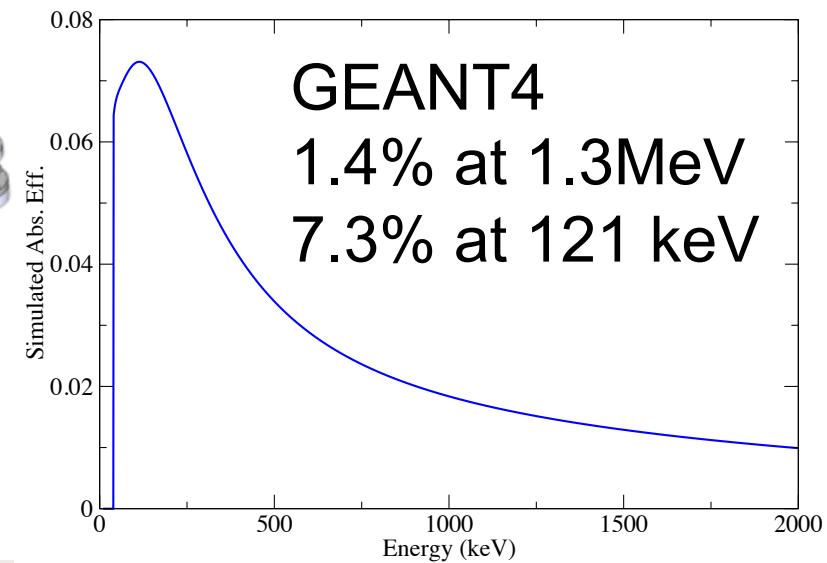
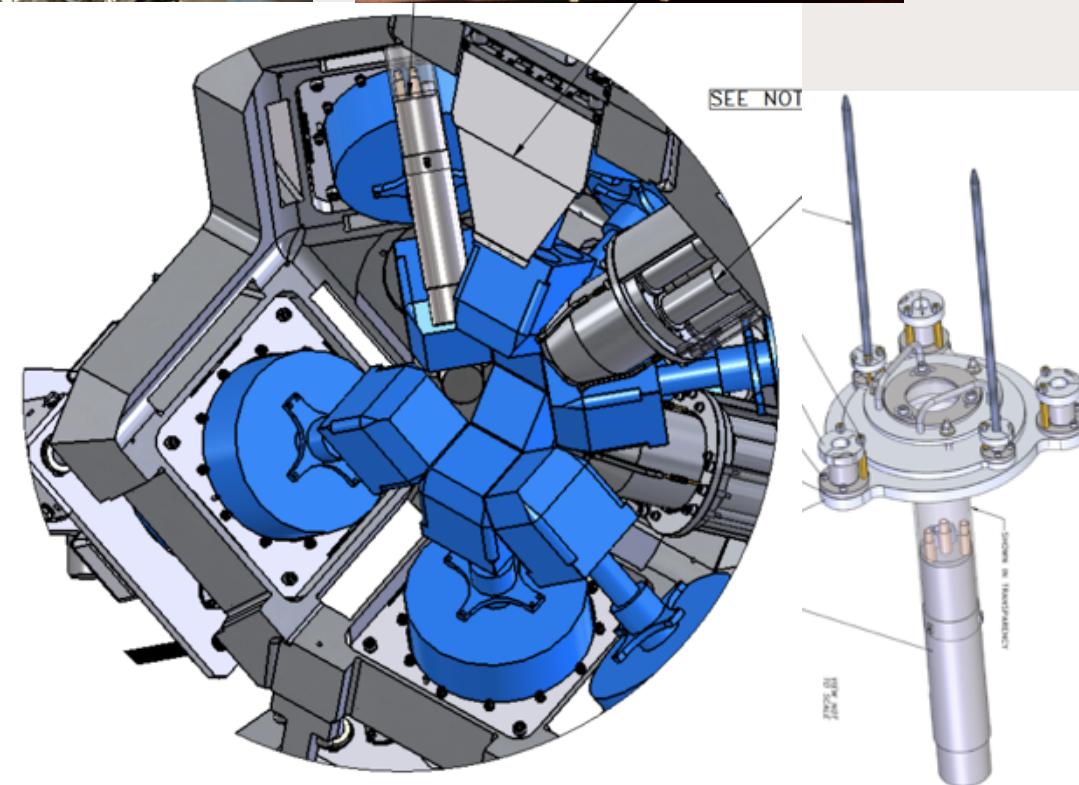


GRIFFIN: ~9 pps, ~2 days

# Fast-Scintillator Array for Excited-State Lifetime Timing

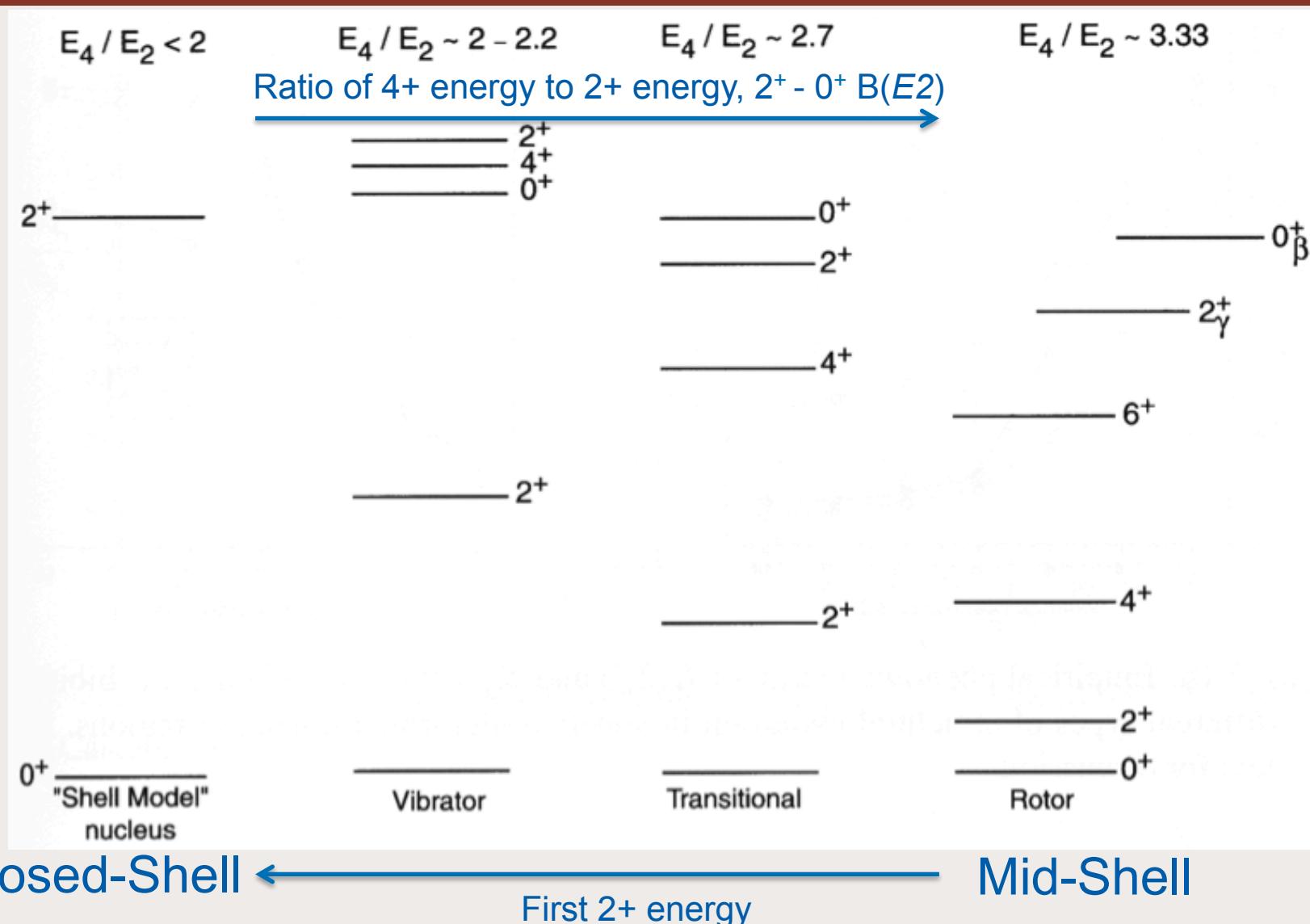


- Eight  $\text{LaBr}_3(\text{Ce})$  2"x2" cylindrical crystal
- Source-detector distance=12.5 cm.
- GEANT4 simulated efficiency 1.4%@1.3MeV
- LaBr-LaBr FWHM <200 ps achieved in 8pi analogue electronics
- Fast Zero-degree scintillator for  $\beta$ - $\gamma$  timing. BC422Q = 0.7ns



# Lifetime Measurements for the Determination of Electric Monopole Transition Strengths

# Excitation Mechanisms of Nuclei



# Evolution of Structure

- Peaks/troughs at magic numbers
- Smooth transition away from magic numbers

What mechanisms drive the transition from spherical, single-particle structures to deformed, collective excitations?

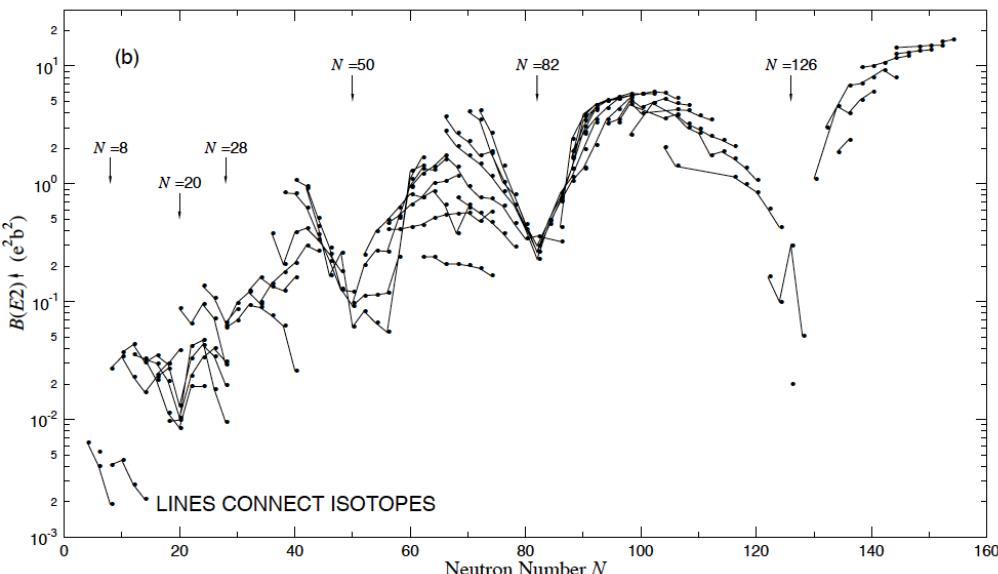
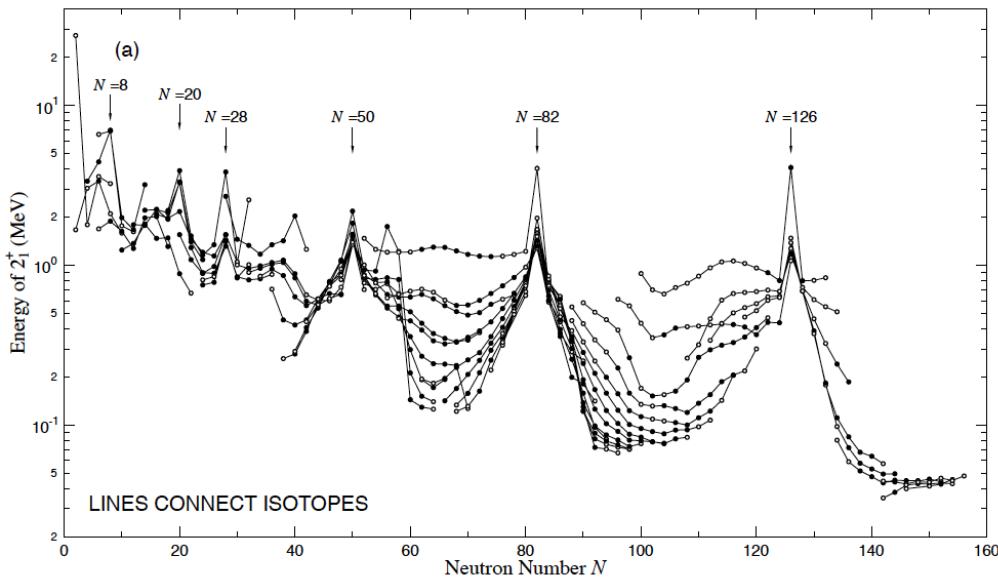


Figure from S. Raman, C.W. Nestor, JR., P. Tikkanen, Atomic Data and Nuclear Data Tables 78, 1 (2001).

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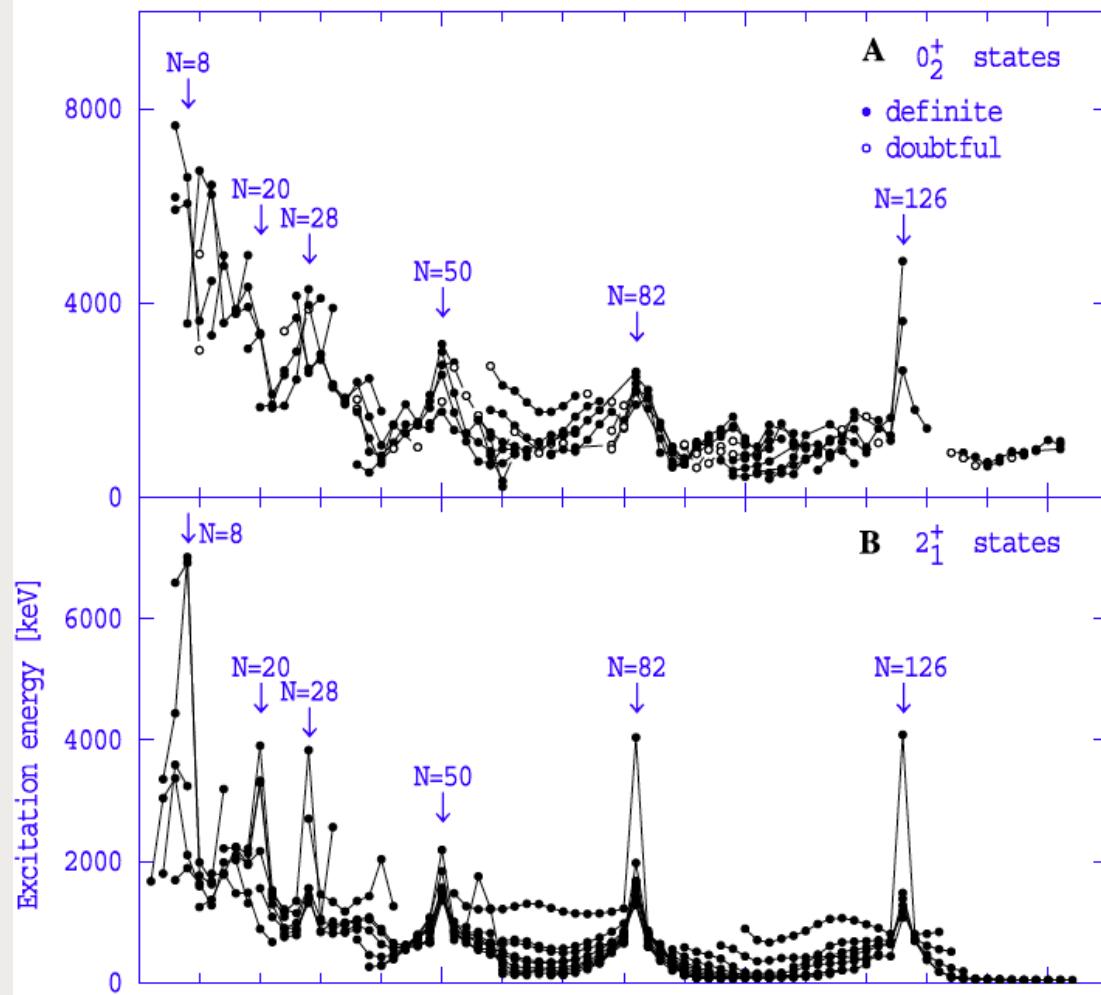
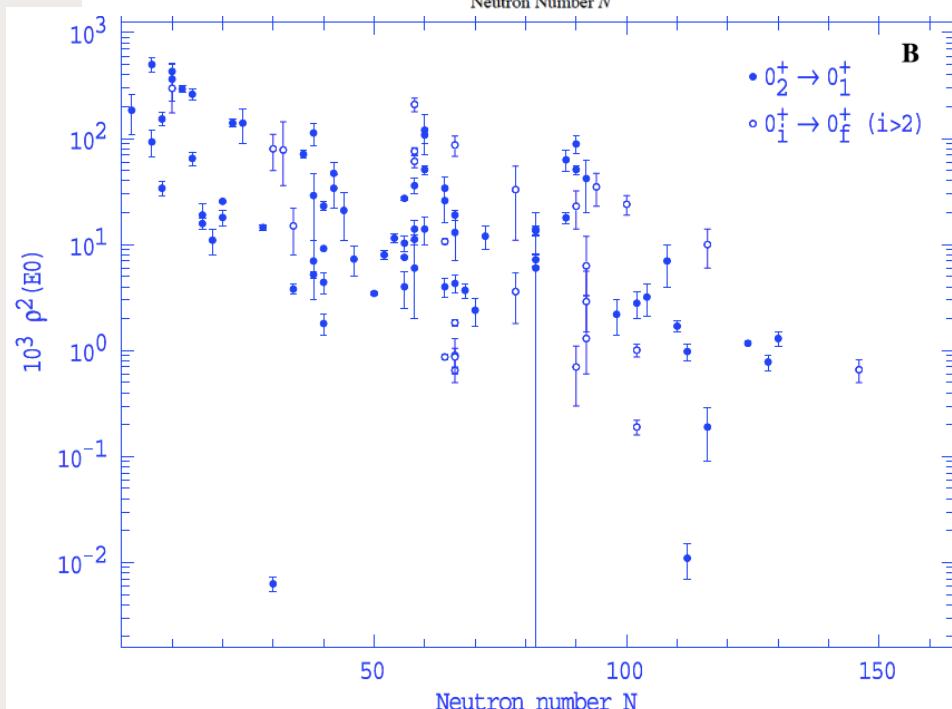
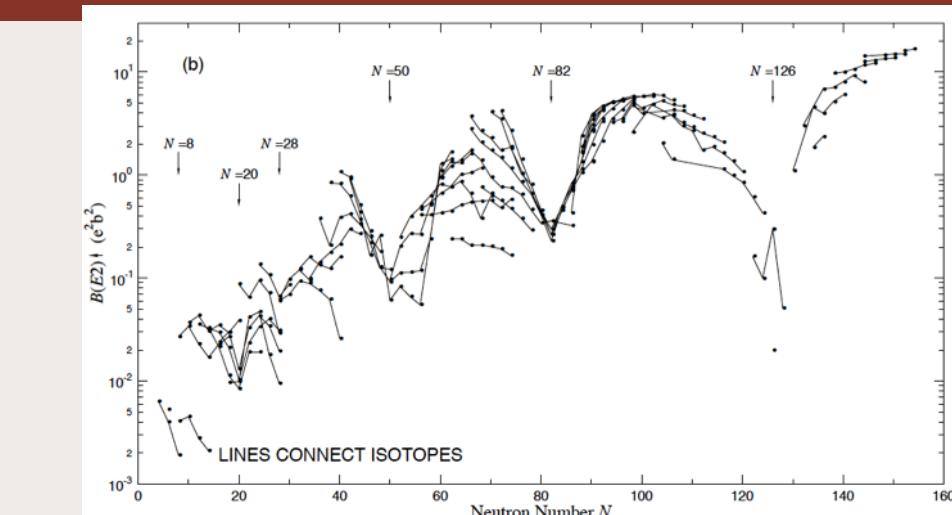


Figure from T. Kibédi and R.H. Spear, Atomic Data and Nuclear Data Tables 89, 77 (2005).

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Figures from S. Raman, C.W. Nestor, JR., P. Tikkanen, Atomic Data and Nuclear Data Tables 78, 1 (2001), and T. Kibédi and R.H. Spear, Atomic Data and Nuclear Data Tables 89, 77 (2005).

# Theoretical Interpretation

- Shell Model

J.L. Wood, Nucl. Phys. A 651, 323 (1999).

$$\rho^2 = 0.5A^{-\frac{2}{3}}$$

- Beta Vibration

P.E. Garrett, J. Phys. G: Nucl. Part. Phys. 27, R1 (2001).

$$\rho^2(E0; n_\beta = 1 \rightarrow n_\beta = 0) = \frac{9}{8\pi^2} Z^2 \beta_0^4 \frac{E(2_1^+)}{E(0_\beta^+)}$$

- IBA

P. Van Isacker, Nuclear Data Sheets 120, 119 (2014).

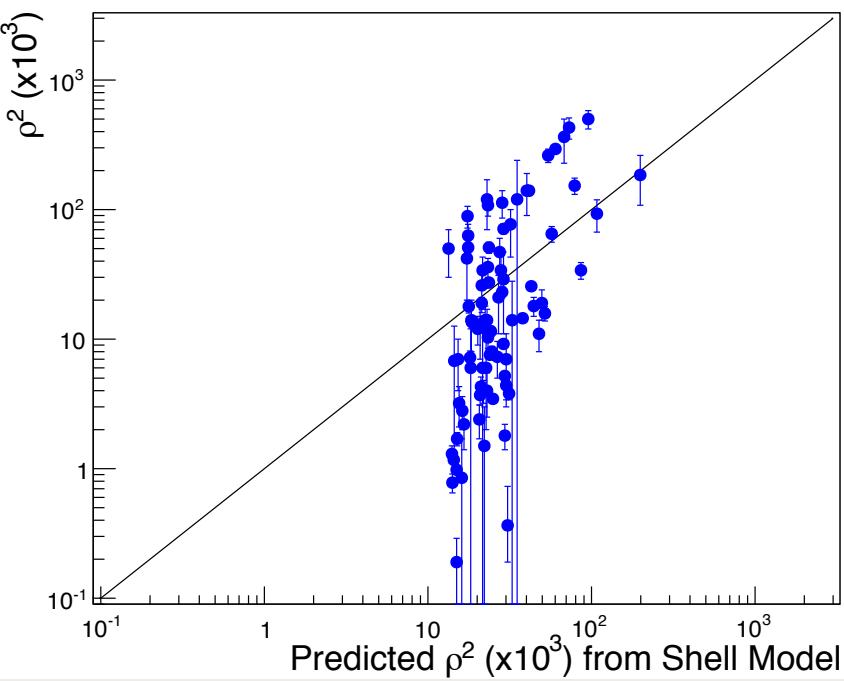
S. Zerguine et al., PRL 101, 022502 (2008).

G. Ilie and R.F. Casten, Phys. Rev. C 84, 064320 (2011).

# Theoretical Interpretation

## Shell Model

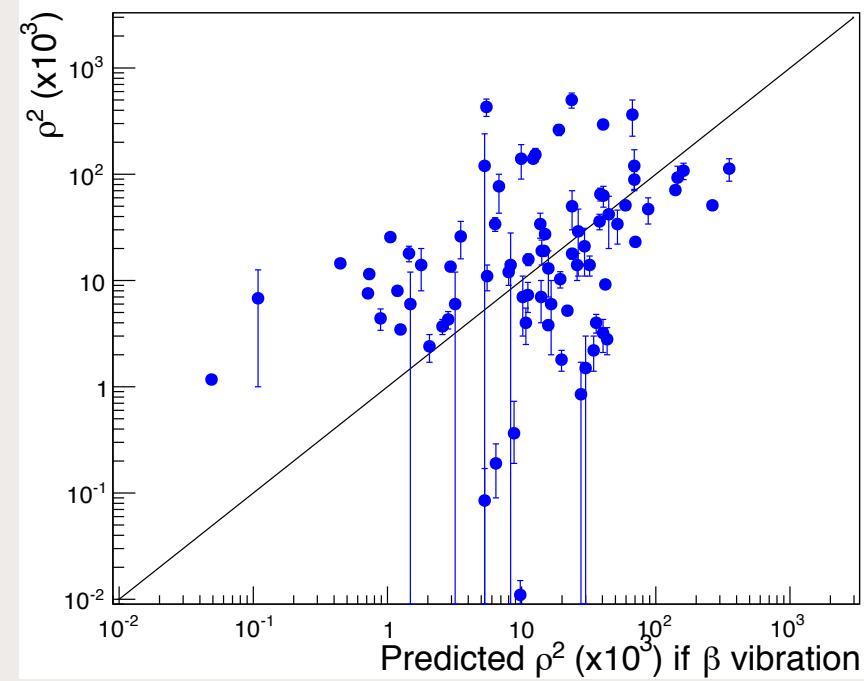
$$\rho^2 = 0.5A^{-\frac{2}{3}}$$



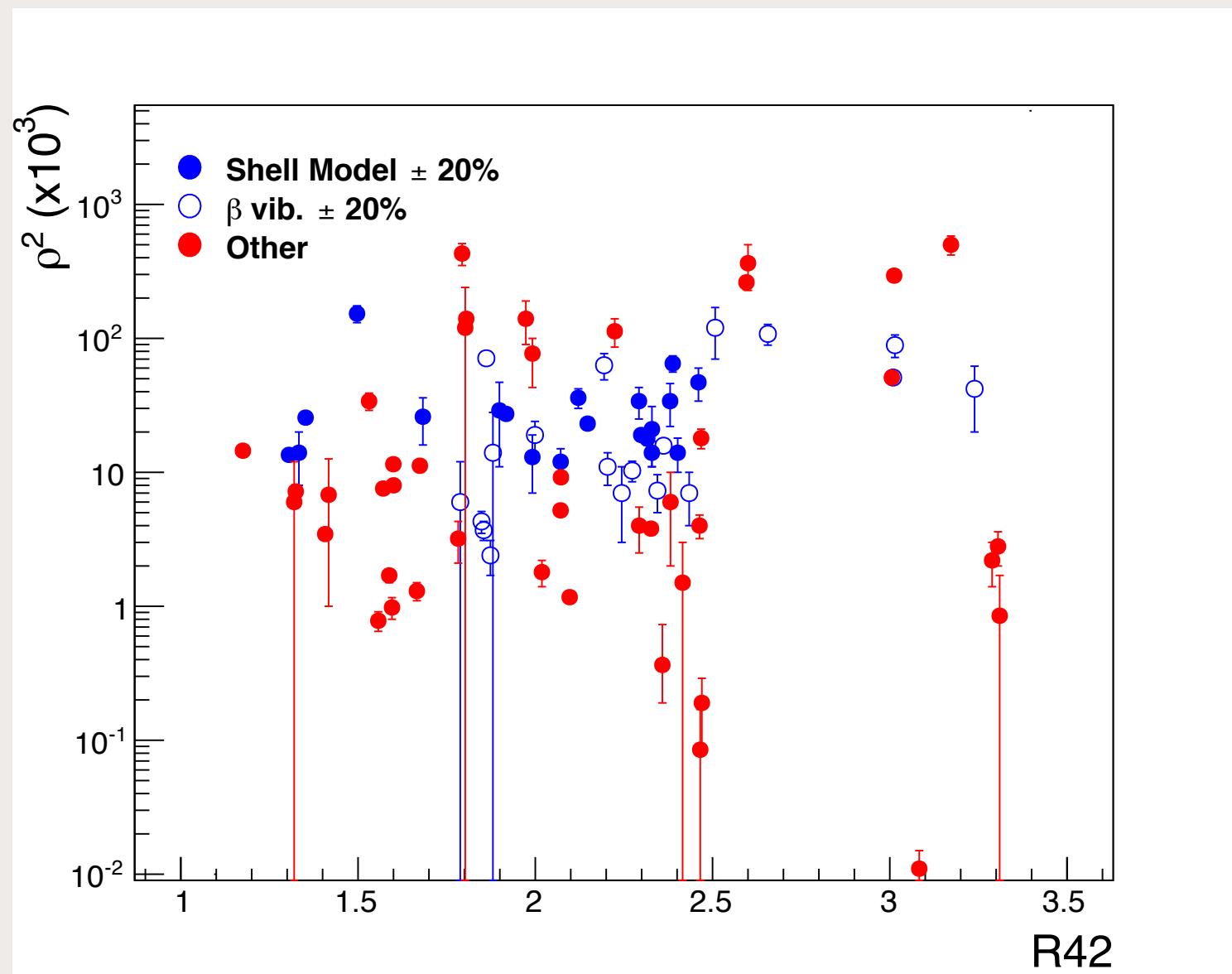
J.L. Wood, Nucl. Phys. A 651, 323 (1999).

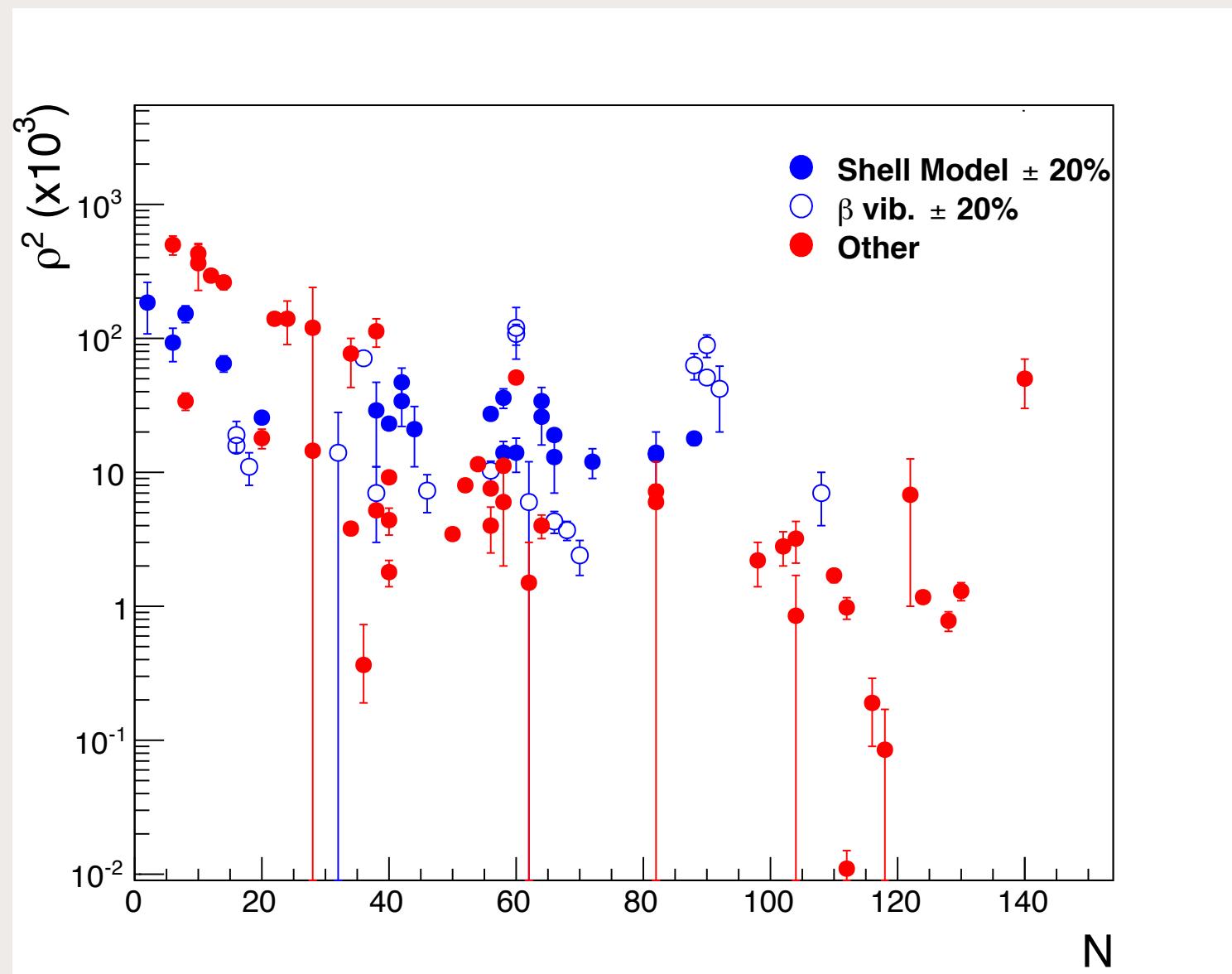
## Beta Vibration

$$\rho^2(E0; n_\beta = 1 \rightarrow n_\beta = 0) = \frac{9}{8\pi^2} Z^2 \beta_0^4 \frac{E(2^+)}{E(0^+)}$$

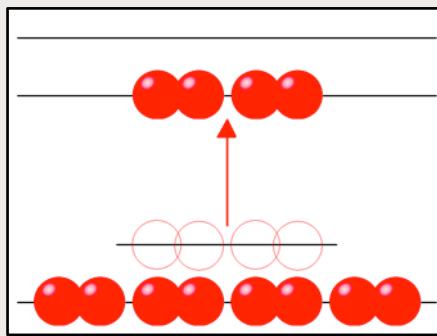


P.E. Garrett, J. Phys. G: Nucl. Part. Phys. 27, R1 (2001).

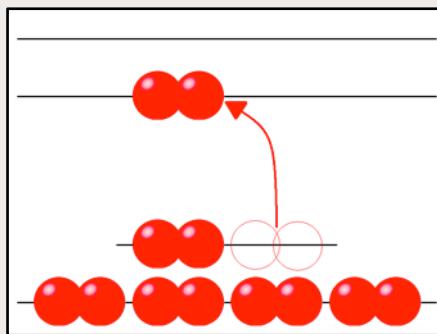




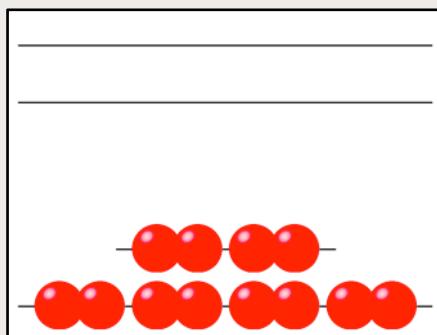
# Particle-Hole Excitations



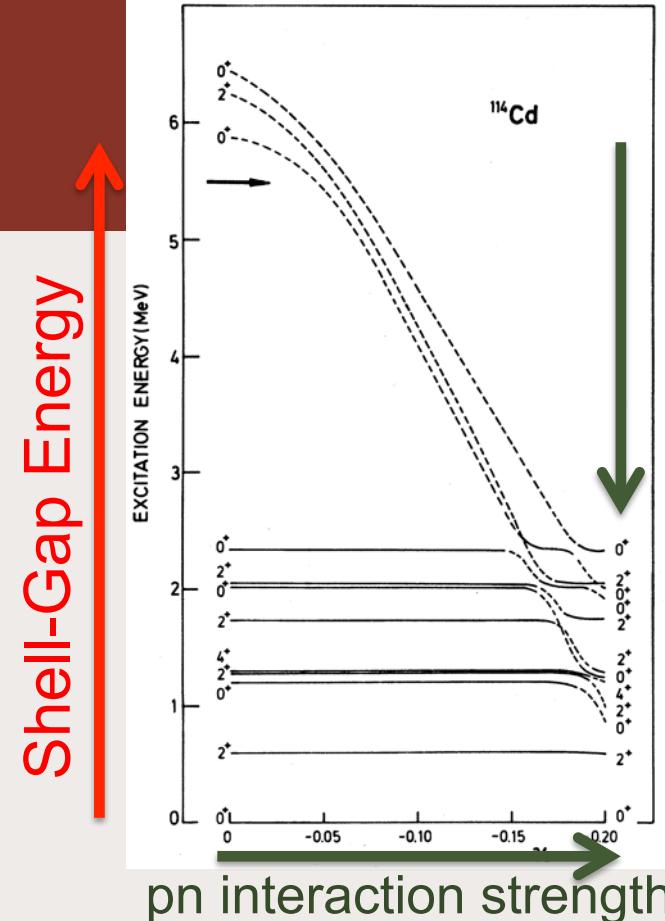
4p - 4h



2p - 2h



Ground State



Effect of attractive proton-neutron residual interaction

State mixing

Unperturbed Wavefunctions  $\rightarrow$  Mixing  $\rightarrow$  Mixed Wavefunctions

$E1, \Psi_1$   
 $E2, \Psi_2$

$$\text{Where: } \alpha^2 + \beta^2 = 1$$

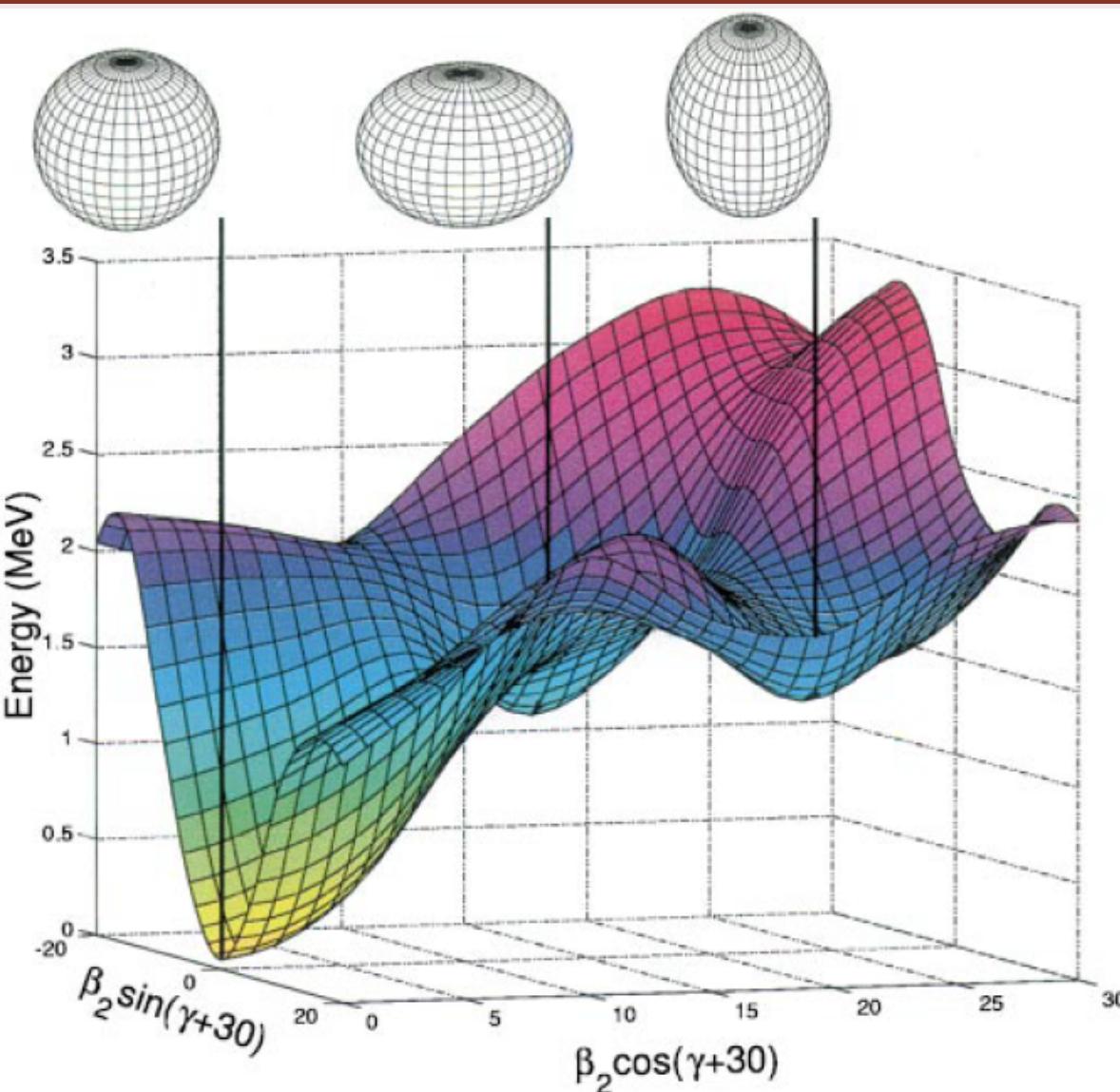
$$\Delta E$$

$E1, \Phi_1$

$E2, \Phi_2$

The amount of mixing depends on the mixing amplitude and the initial separation energy of the states ( $\Delta E$ )

# Co-Existing Nuclear Shapes



Letter to Nature, May 2000  
“A triplet of differently shaped spin-zero states in the atomic nucleus  $^{186}\text{Pb}$ ”

$^{186}\text{Pb}$ :  $Z=82$ ,  $N=104$

Recent review by Heyde and Wood, Reviews of Modern Physics 83, 1467 (2011)

Review notes severe lack of experimental data:  
-particle transfer  
-mean square charge radii  
 $-B(E2), \langle Q^2 \rangle$   
 $-E0$  strengths

# $E0$ Transition Strengths

Recall that:

$$\Phi_1 = \alpha\Psi_1 + \beta\Psi_2$$

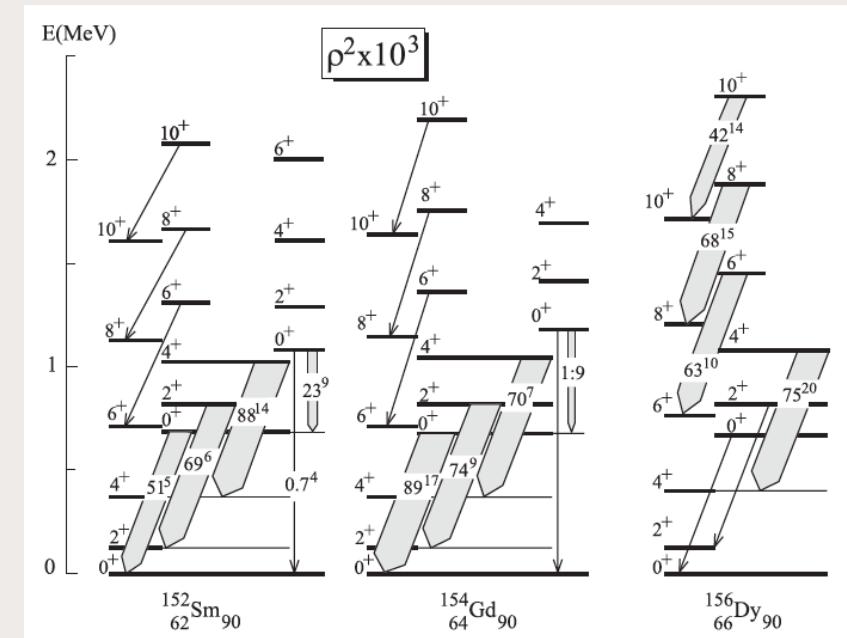
$$\Phi_2 = -\beta\Psi_1 + \alpha\Psi_2$$

where:  $\alpha^2 + \beta^2 = 1$

For a transition between these states  
the  $E0$  strength,  $\rho_{if} = \frac{\langle \Phi_1 | m(E0) | \Phi_2 \rangle}{eR^2}$

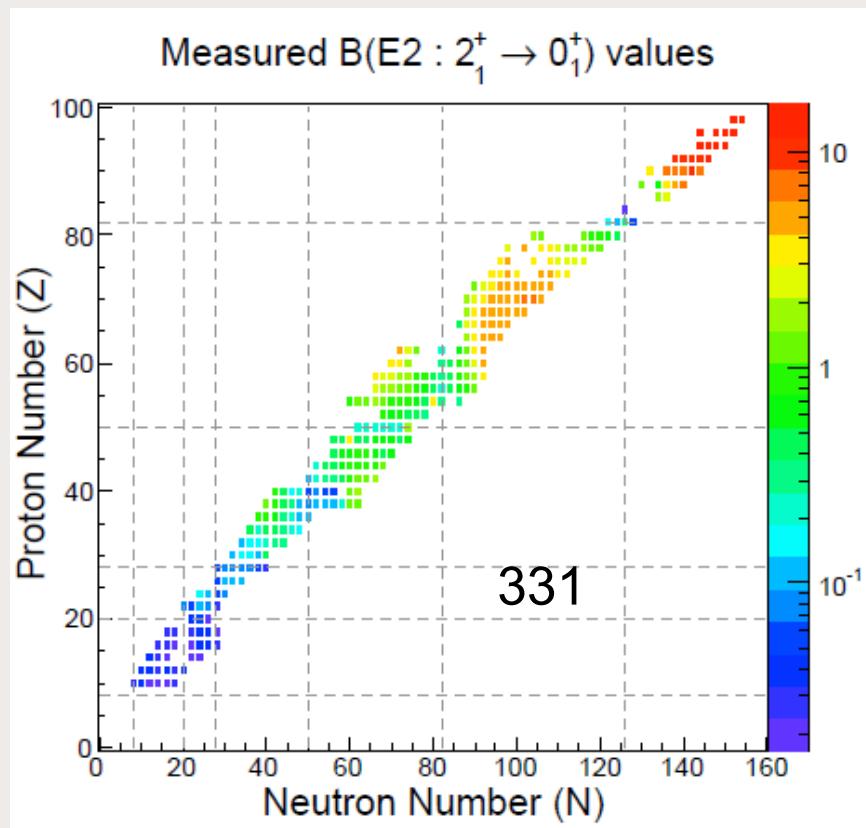
where  $e$  = electric charge  
and  $R = 1.2A^{\frac{1}{3}} fm$  and

$$\langle \Phi_1 | m(E0) | \Phi_2 \rangle \simeq \alpha\beta\Delta\langle r^2 \rangle$$



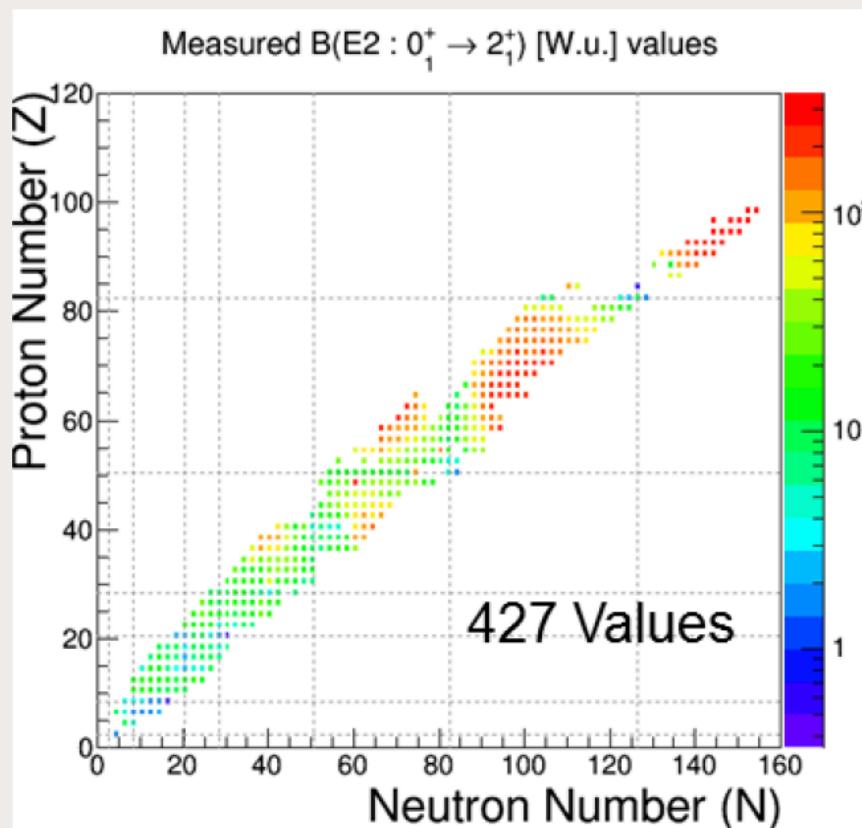
Therefore the  $E0$  strength is  
directly proportional to the  
difference in deformation and  
the amount of mixing

# Measured $B(E2)$ values



Raman et al., Data Nucl. Data  
Tables, 78 (2001)

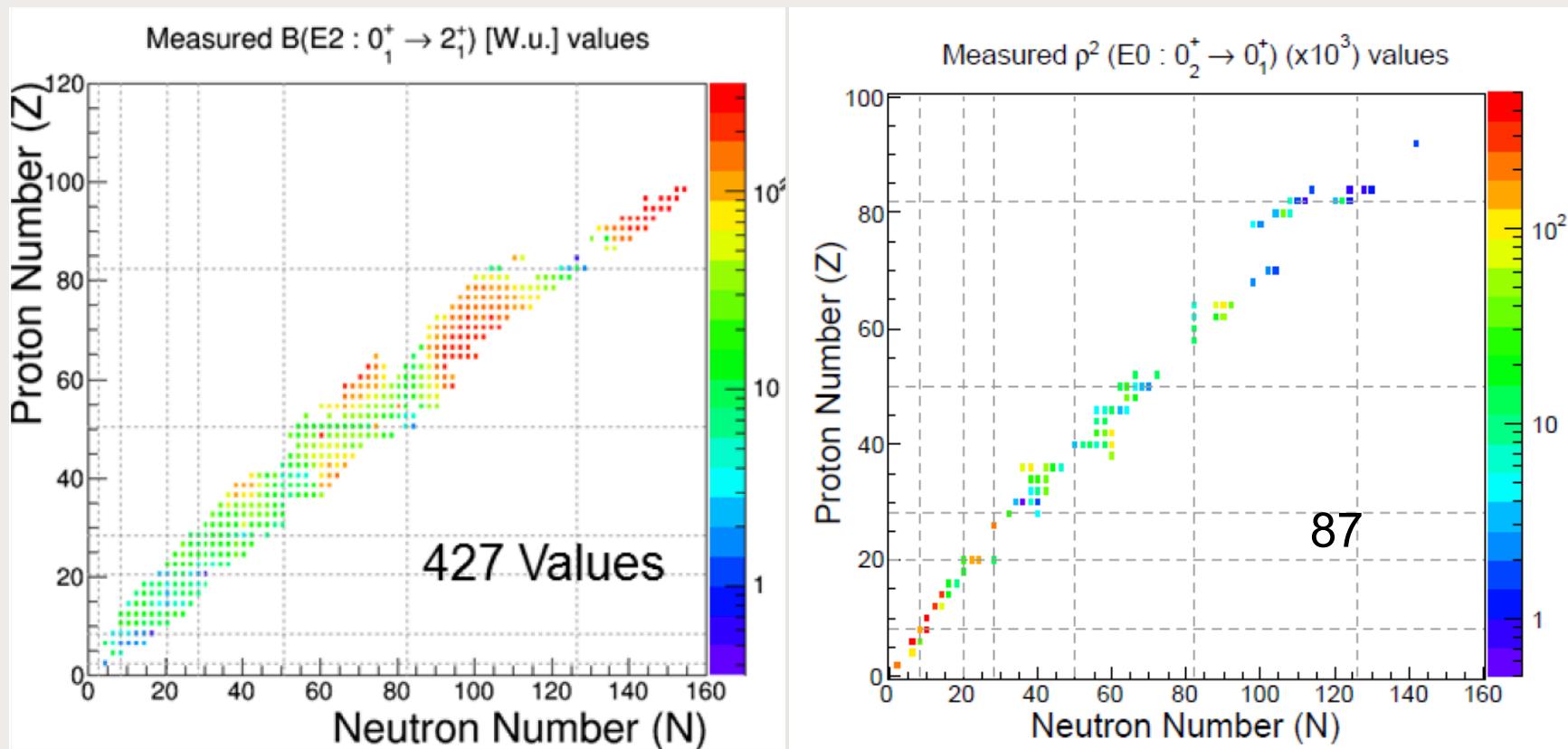
# Measured $B(E2)$ values



Raman et al., Data Nucl. Data  
Tables, 78 (2001)

Pritychenko et al., arXiv:1312.5975 [nucl-th]  
(Dec 2014)

# Measured $\rho^2$ values



Raman et al., Data Nucl. Data Tables, 78 (2001)

Pritychenko et al., arXiv:1312.5975 [nucl-th]  
(Dec 2014)

Kibedi & Spear, Data Nucl. Data Tables, 89, (2005)

# Measuring $\rho^2$ values

$$\rho^2(E0) = q_K^2(E0/E2) \times \frac{\alpha_K(E2)}{\Omega_K(E0)} \times W_\gamma(E2).$$

$\rho^2$  from branching ratio and parent state partial decay constant of  $E2$  gamma ray

$$q_K^2(E0/E2) = \frac{I_K(E0)}{I_K(E2)}$$

$q^2$  found from ICE spectroscopy

$$q_K^2(E0/E2) = \frac{I_\pi(E0)}{I_\pi(E2)} \times \frac{\Omega_K(E0)}{\Omega_\pi(E0)} \times \frac{\alpha_\pi(E2)}{\alpha_K(E2)}$$

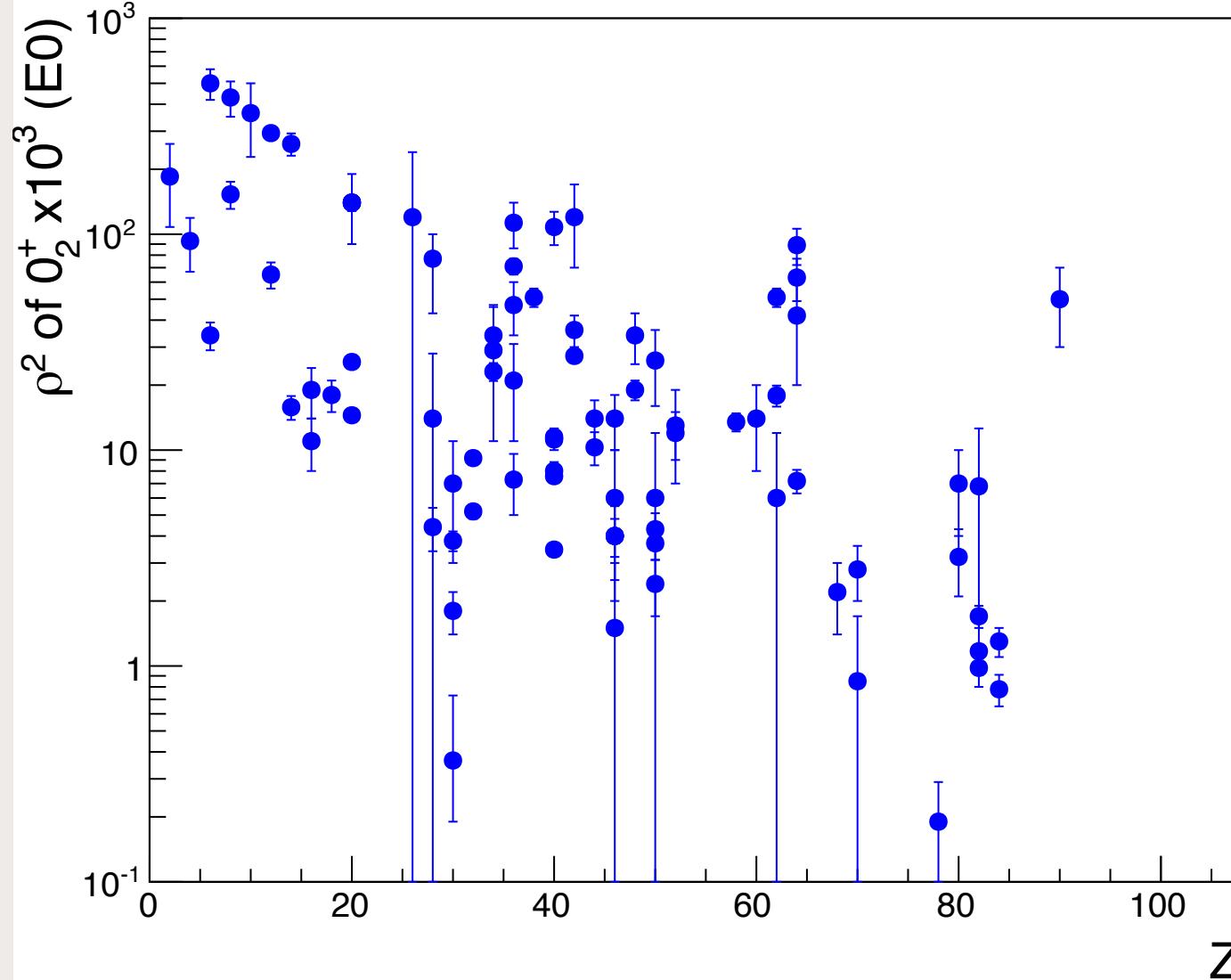
or from IPF spectroscopy

$W_\gamma(E2)$  can be found from Coulex or from **direct lifetime measurement**

# Present Knowledge of $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

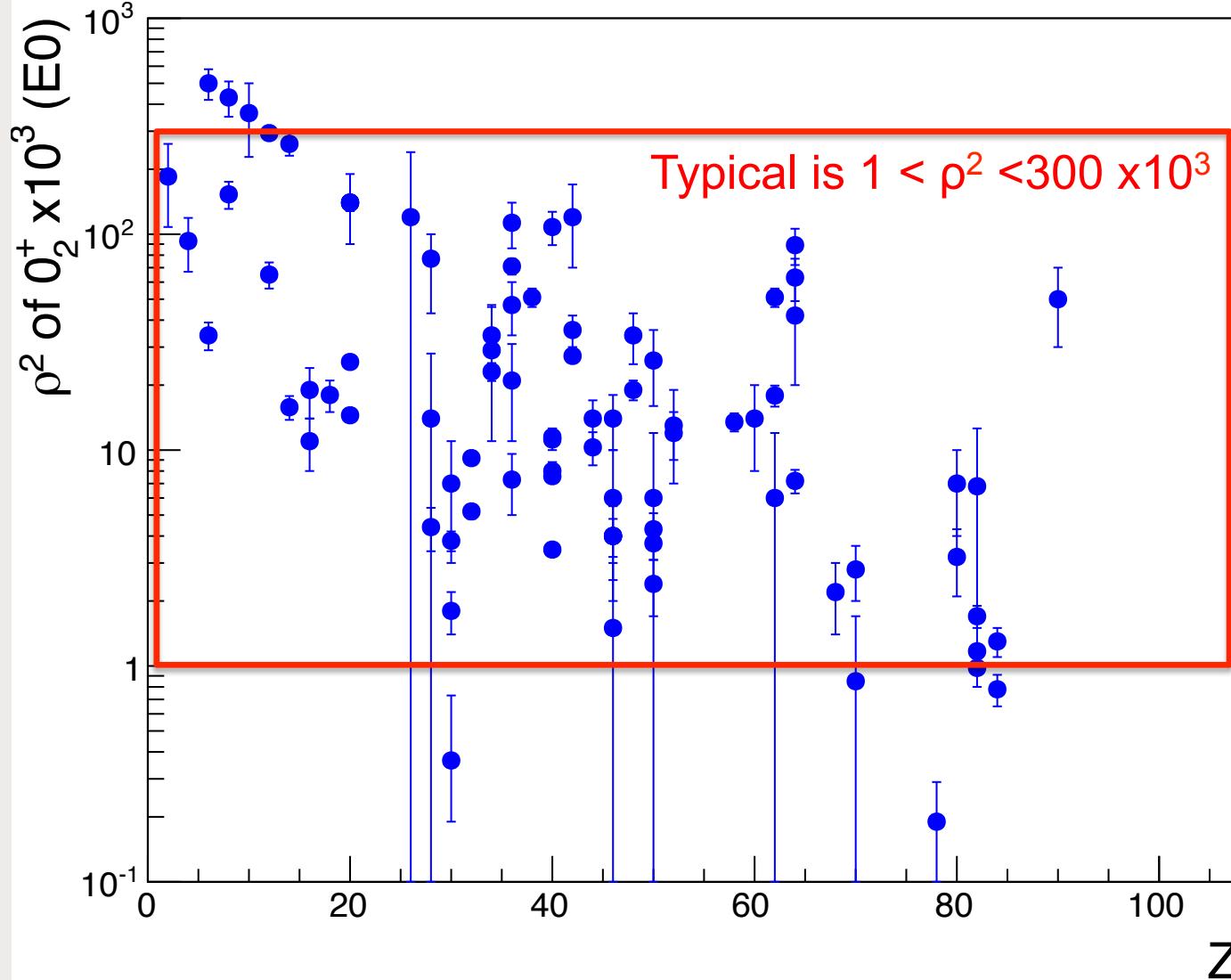
87  $p^2$  values of first excited  $0^+$  to GS  $0^+$  known



# Present Knowledge of $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

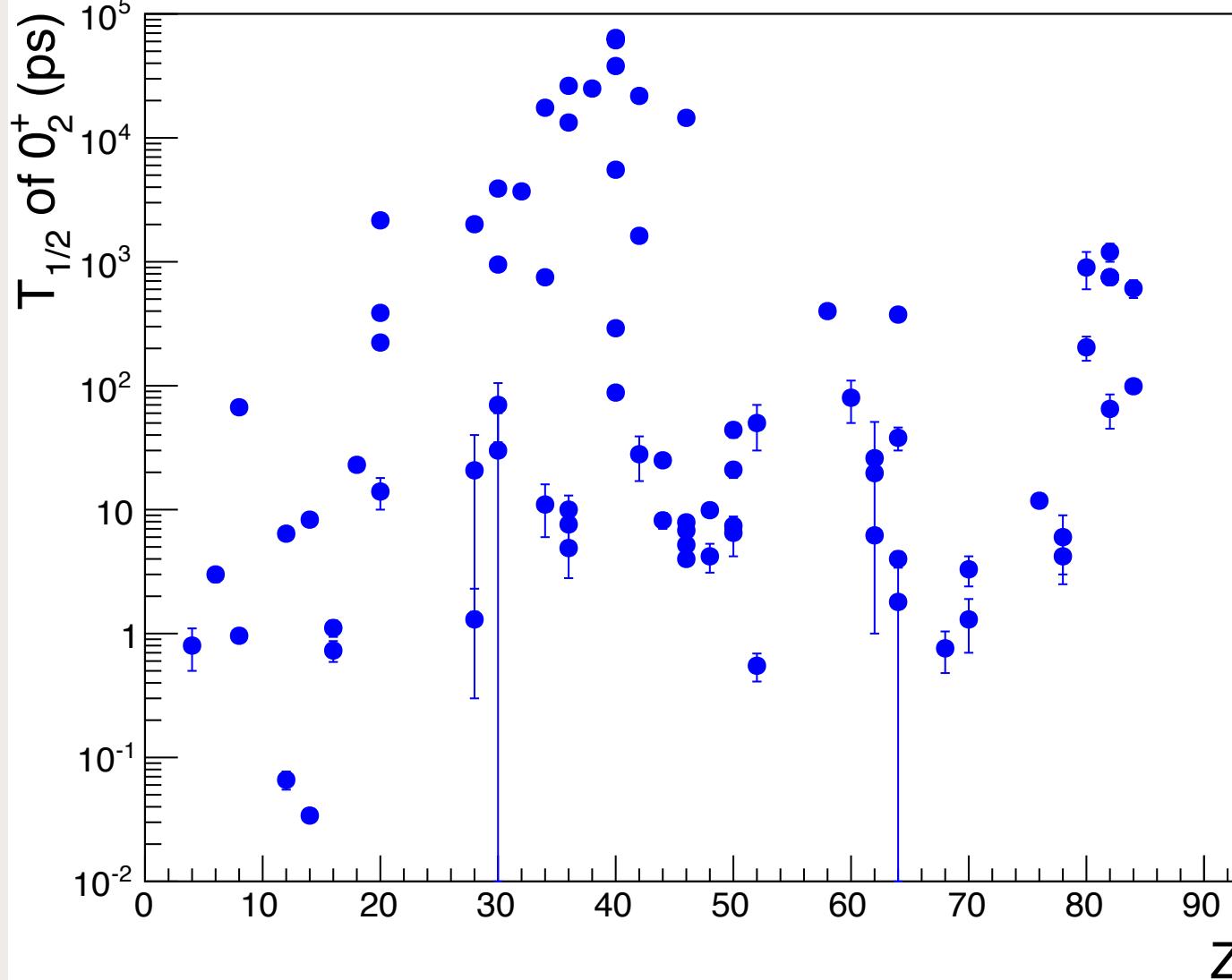
87  $p^2$  values of first excited  $0^+$  to GS  $0^+$  known



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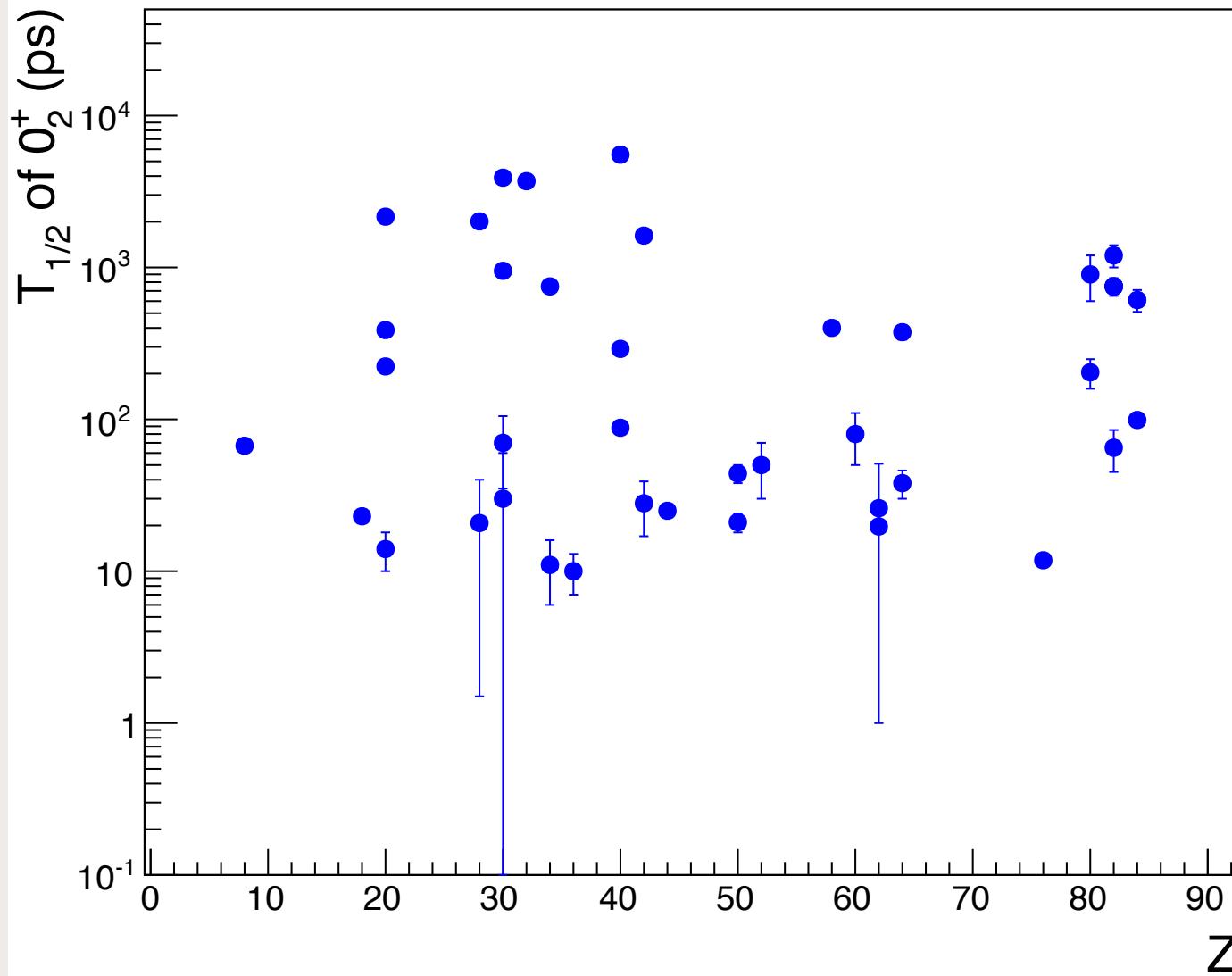
87  $p^2$  values of first excited  $0^+$  to GS  $0^+$  known



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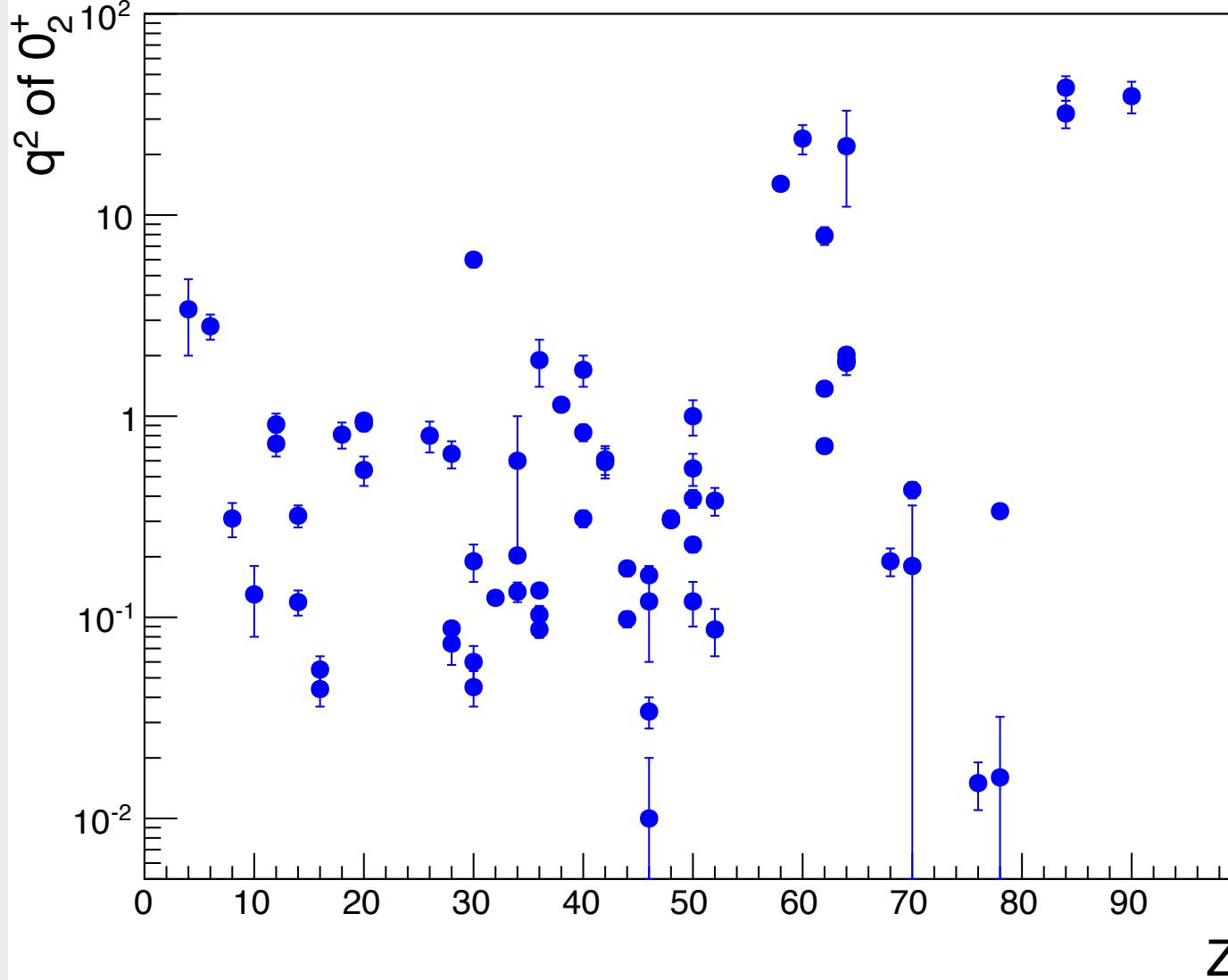
40  $p^2$  values of first excited  $0^+$  to GS  $0^+$  known with  $10\text{ps} < T_{1/2} < 10\text{ns}$



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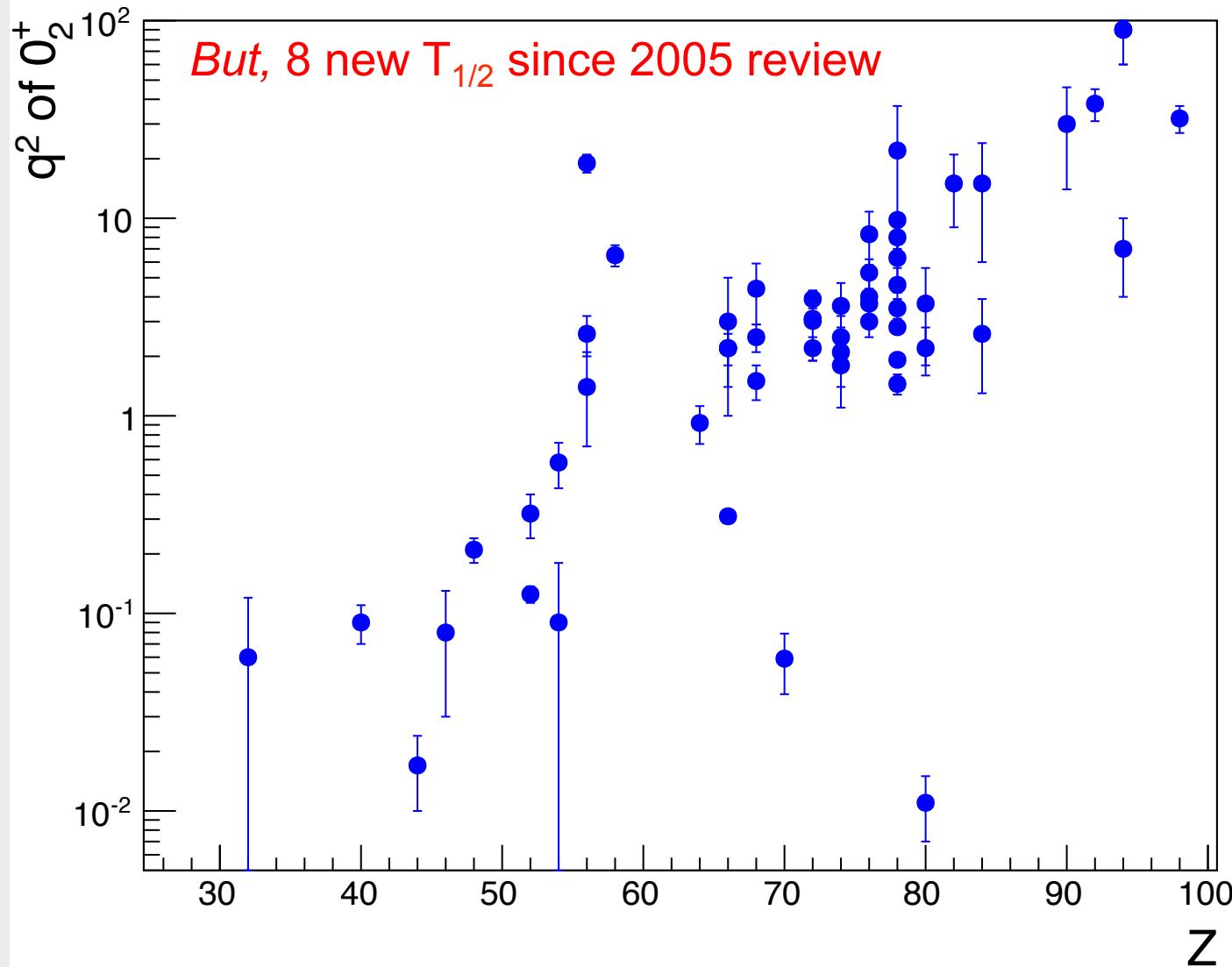
87  $p^2$  values of first excited  $0^+$  to GS  $0^+$  known



# Half-life required to determine $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

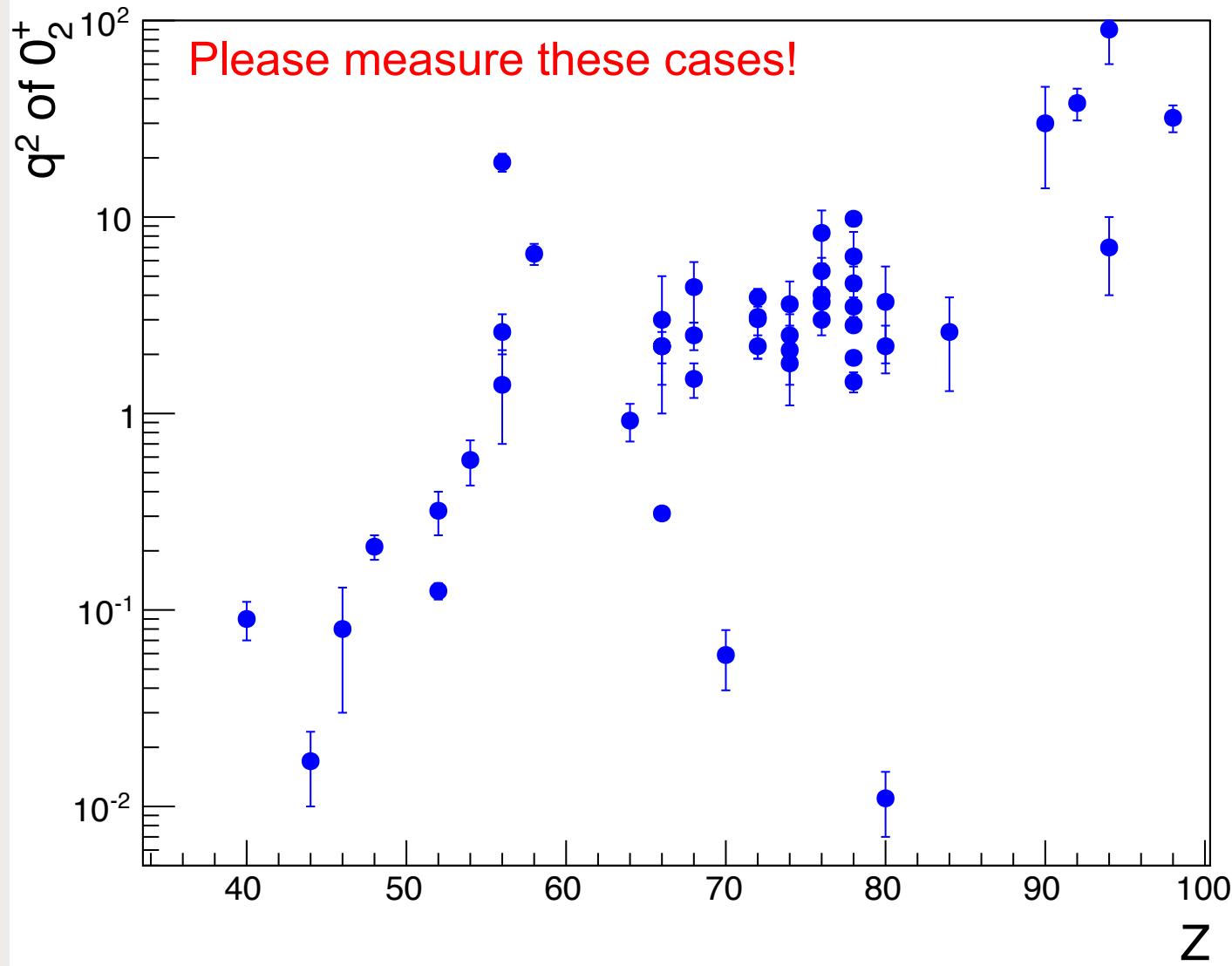
59  $q^2$  values known but no  $T_{1/2}$  of first excited  $0^+$  to GS  $0^+$  known



# Half-life required to determine $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

51  $q^2$  values known but no  $T_{1/2}$  of first excited  $0^+$  to GS  $0^+$  known



# Half-life required to determine $E0$ strengths

Kibédi and Spear,  
Atomic. Data and Nucl. Data Tables 89, 77 (2005).

51  $q^2$  values known but no  $T_{1/2}$  of first excited  $0^+$  to GS  $0^+$  known

Please measure these half lives!

Table 1: Medium-mass and Rare-earth region.

Nucleus	Energy $0_2^+$ (keV)	Energy $0_2^+ \rightarrow 2_1^+$ (keV)	$q^2$
$^{88}_{40}\text{Zr}_{48}$	1521.4	464.37	0.09 (0.02)
$^{106}_{44}\text{Ru}_{62}$	990.62	720.55	0.017 (0.007)
$^{112}_{46}\text{Pd}_{66}$	890.4	541.61	0.08 (0.05)
$^{110}_{48}\text{Cd}_{62}$	1473.07	815.308	0.21 (0.03)
$^{120}_{52}\text{Te}_{68}$	1103.1	542.662	0.32 (0.08)
$^{122}_{52}\text{Te}_{70}$	1357.4	793.307	0.125 (0.012)
$^{118}_{54}\text{Xe}_{64}$	830.36	493.04	0.58 (0.15)
$^{124}_{56}\text{Ba}_{68}$	898	668.09	1.4 (0.7)
$^{134}_{56}\text{Ba}_{78}$	1760.56	1155.83	19 (2)
$^{136}_{56}\text{Ba}_{80}$	1578.99	760.493	2.6 (0.6)
$^{138}_{58}\text{Ce}_{80}$	1476.93	688.186	6.5 (0.8)
$^{150}_{64}\text{Gd}_{86}$	1207.1	569	0.92 (0.2)
$^{154}_{66}\text{Dy}_{88}$	660.55	326.21	2.2 (0.4)
$^{156}_{66}\text{Dy}_{90}$	675.6	537.83	3 (2)
$^{160}_{66}\text{Dy}_{94}$	1279.94	1193.15	2.2 (0.8)
$^{162}_{66}\text{Dy}_{96}$	1400.26	1319.6	0.31 (0.02)
$^{158}_{68}\text{Er}_{90}$	806.38	614.23	1.5 (0.3)
$^{162}_{68}\text{Er}_{94}$	1087.16	985.12	4.4 (1.5)
$^{164}_{68}\text{Er}_{96}$	1246.04	1154.66	2.5 (0.4)
$^{170}_{70}\text{Yb}_{100}$	1069.35	985.095	0.059 (0.02)

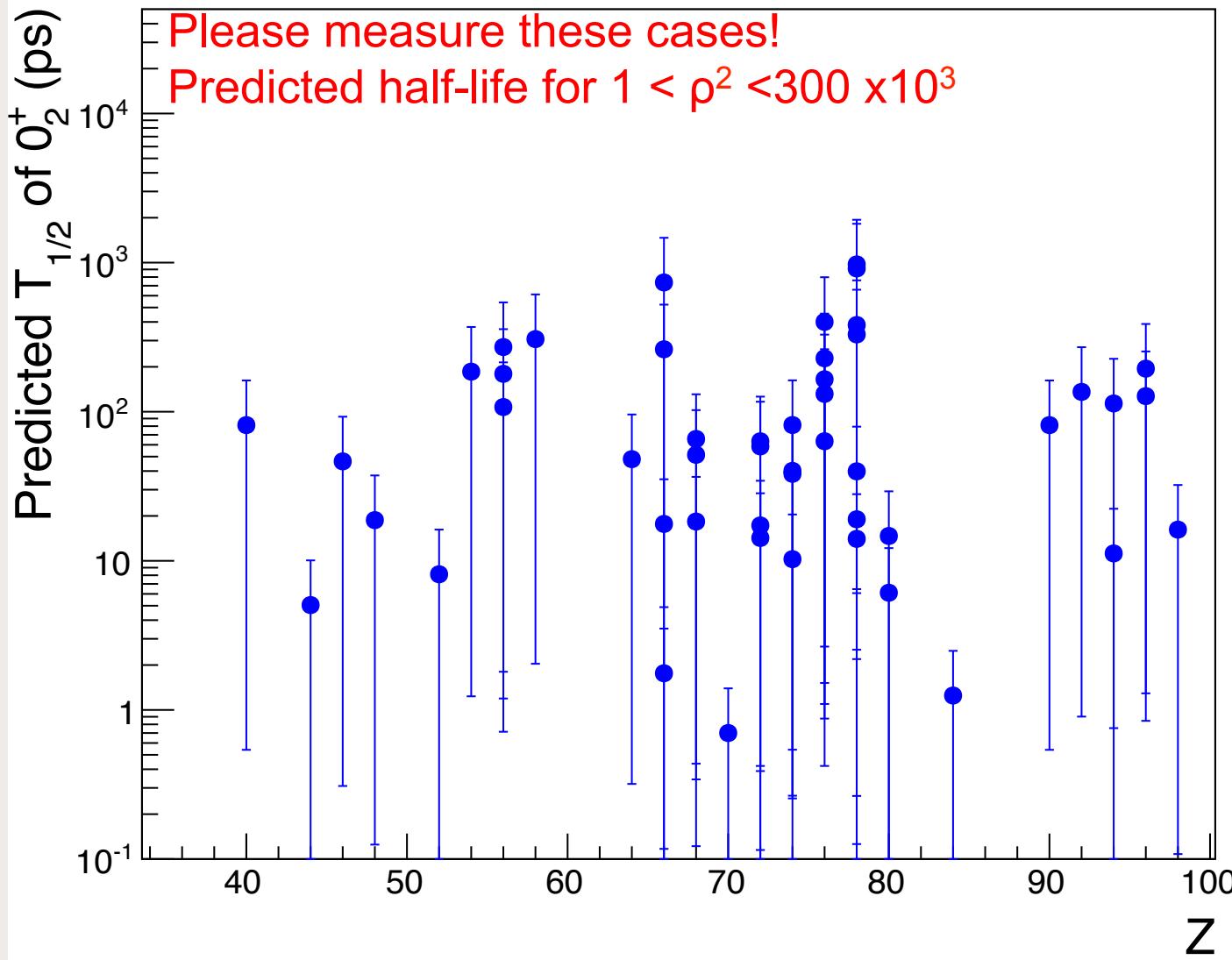
Table 2: Transitional metals to Actinides.

Nucleus	Energy $0_2^+$ (keV)	Energy $0_2^+ \rightarrow 2_1^+$ (keV)	$q^2$
$^{172}_{72}\text{Hf}_{100}$	871.3	776.08	3.9 (0.4)
$^{174}_{72}\text{Hf}_{102}$	828.13	737.145	3.1 (1.2)
$^{176}_{72}\text{Hf}_{104}$	1149.94	1061.59	2.2 (0.3)
$^{178}_{72}\text{Hf}_{106}$	1199.38	1106.2	3.02 (0.13)
$^{172}_{74}\text{W}_{98}$	761.6	638.4	3.6 (1.1)
$^{174}_{74}\text{W}_{100}$	792.2	679.2	2.1 (0.7)
$^{176}_{74}\text{W}_{102}$	843.3	735	2.5 (0.7)
$^{182}_{74}\text{W}_{108}$	1135.82	1035.71	1.8 (0.7)
$^{172}_{76}\text{Os}_{96}$	758.27	530.5	8.3 (2.5)
$^{174}_{76}\text{Os}_{98}$	545.3	386.7	5.3 (0.9)
$^{176}_{76}\text{Os}_{100}$	601.2	466.1	3.7 (0.5)
$^{178}_{76}\text{Os}_{102}$	650.4	518	4 (1)
$^{180}_{76}\text{Os}_{104}$	736.3	604.19	3 (0.5)
$^{180}_{78}\text{Pt}_{102}$	478.13	324.92	9.8 (0.8)
$^{182}_{78}\text{Pt}_{104}$	499.5	344.9	4.6 (1)
$^{184}_{78}\text{Pt}_{106}$	491.78	328.8	3.5 (0.4)
$^{186}_{78}\text{Pt}_{108}$	471.51	279.98	6.3 (2.1)
$^{188}_{78}\text{Pt}_{110}$	798.76	533.13	1.92 (0.06)
$^{190}_{78}\text{Pt}_{112}$	920.86	625.06	1.45 (0.17)
$^{192}_{78}\text{Pt}_{114}$	1195.17	878.663	2.81 (0.2)
$^{190}_{80}\text{Hg}_{110}$	1278.6	862.28	3.7 (1.9)
$^{198}_{80}\text{Hg}_{118}$	1401.52	989.717	2.2 (0.6)
$^{200}_{80}\text{Hg}_{120}$	1029.34	661.401	0.011 (0.004)
$^{210}_{84}\text{Po}_{126}$	2608.58	1427.18	2.6 (1.3)
$^{228}_{90}\text{Th}_{138}$	831.8	774.041	30 (16)
$^{232}_{92}\text{U}_{140}$	691.2	643.628	38 (7)
$^{238}_{94}\text{Pu}_{144}$	941.5	897.42	90 (30)
$^{240}_{94}\text{Pu}_{146}$	860.7	817.876	7 (3)
$^{244}_{96}\text{Cm}_{148}$	984.9	941.935	210 (70)
$^{246}_{96}\text{Cm}_{150}$	1174.7	1131.85	220 (30)
$^{250}_{98}\text{Cf}_{152}$	1154.3	1111.58	32 (5)

# Half-life required to determine $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

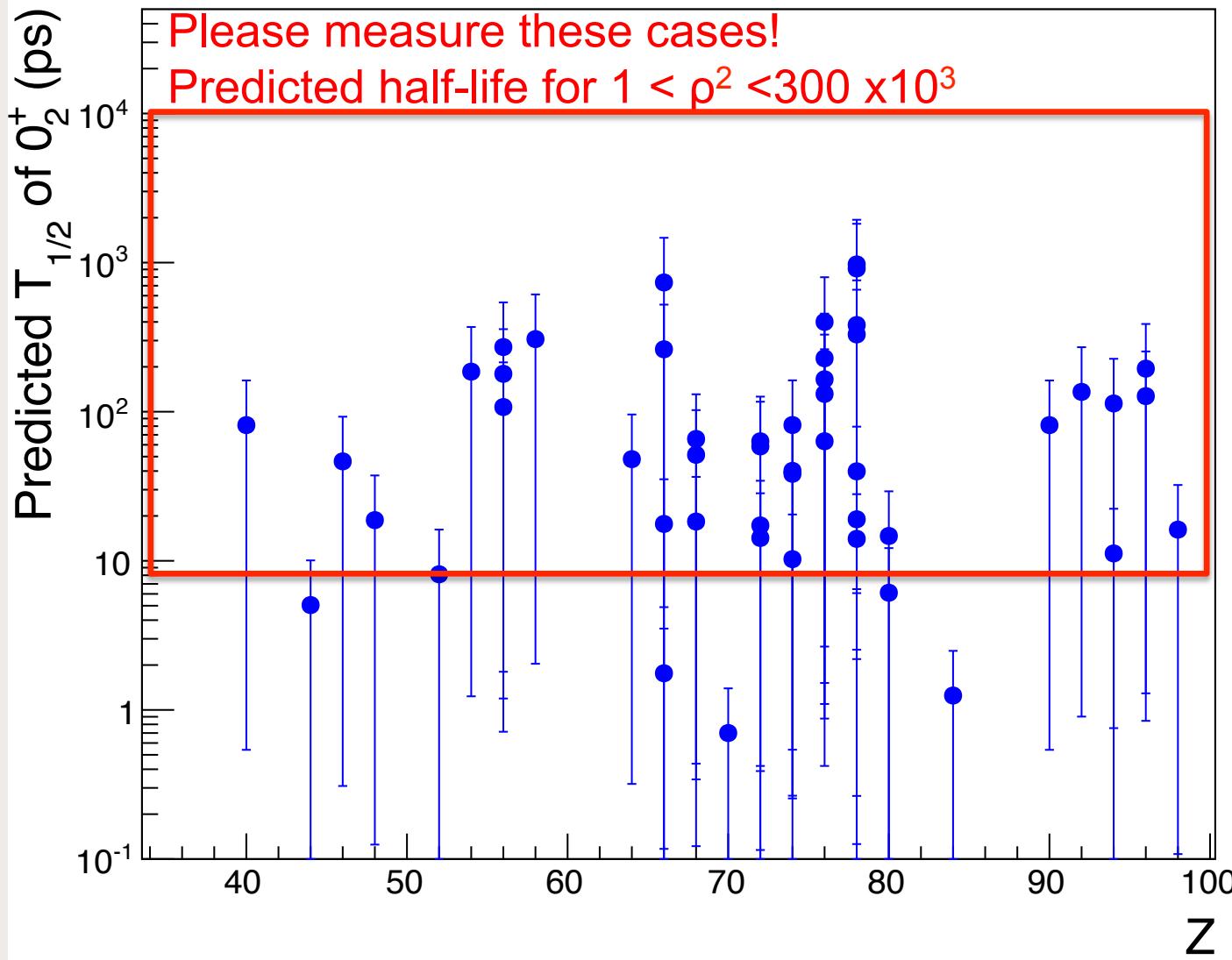
51  $q^2$  values known but no  $T_{1/2}$  of first excited  $0^+$  to GS  $0^+$  known



# Half-life required to determine $E0$ strengths

Kibédi and Spear, Atomic. Data and Nucl. Data Tables 89, 77 (2005).

51  $q^2$  values known but no  $T_{1/2}$  of first excited  $0^+$  to GS  $0^+$  known



# Summary

- We do not have a universal and consistent description of  $0^+$  states in nuclei.
- $E0$  transition strengths are a sensitive probe of nuclear structure. More data is required to properly map the systematic behavior.
- Half life measurements are an essential ingredient for determining  $\rho^2$ .
- 51 cases with electron work already completed.

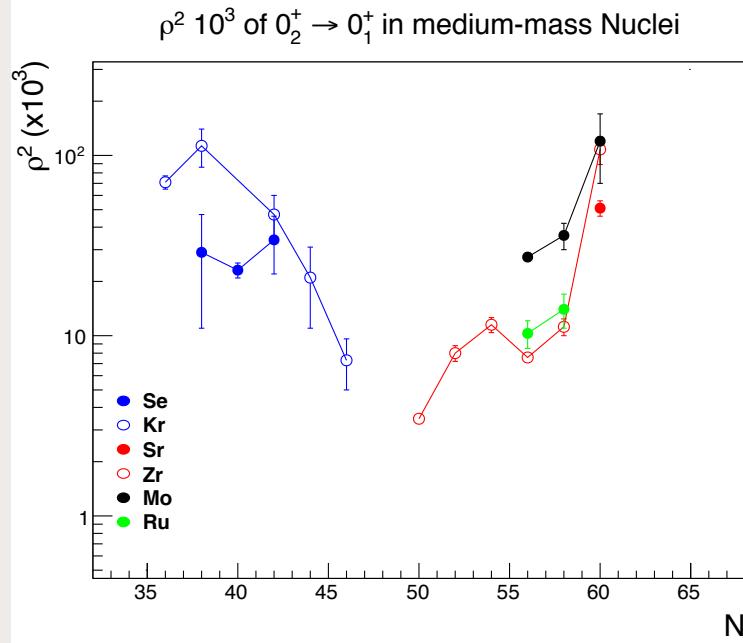
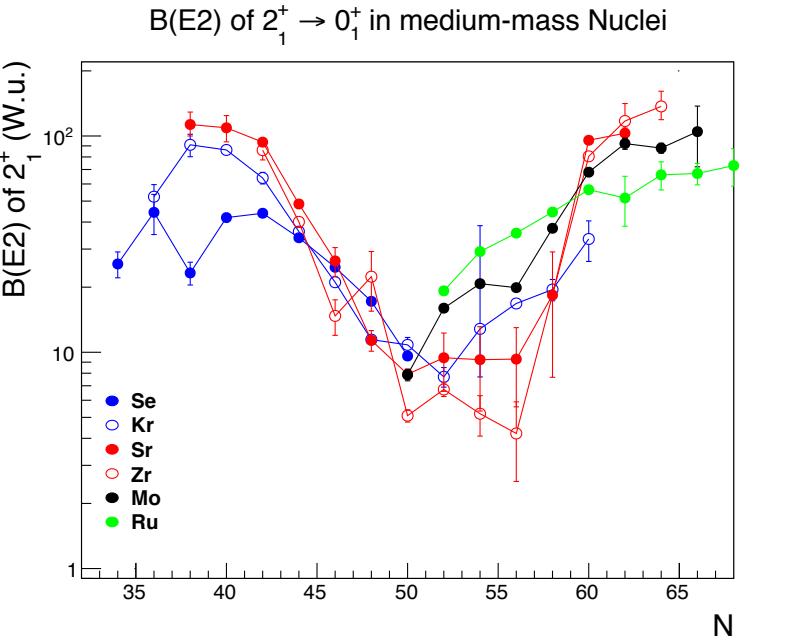
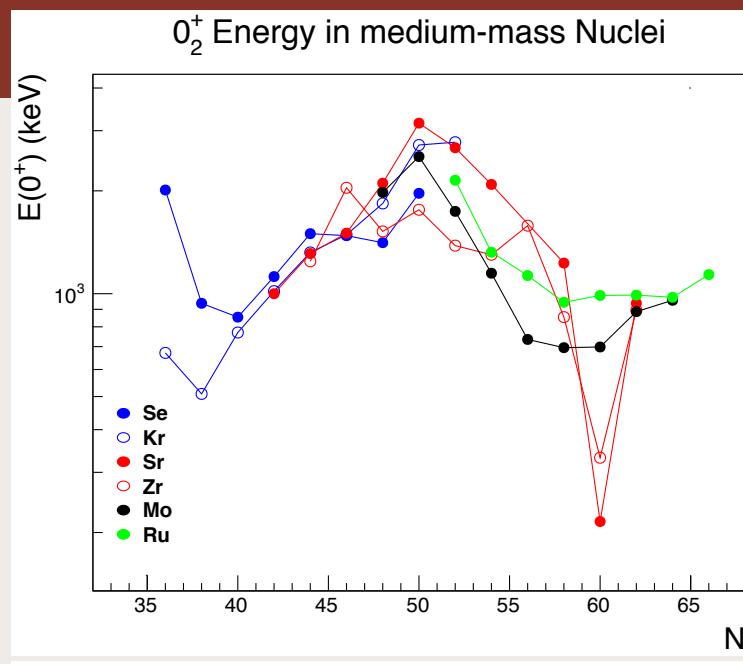
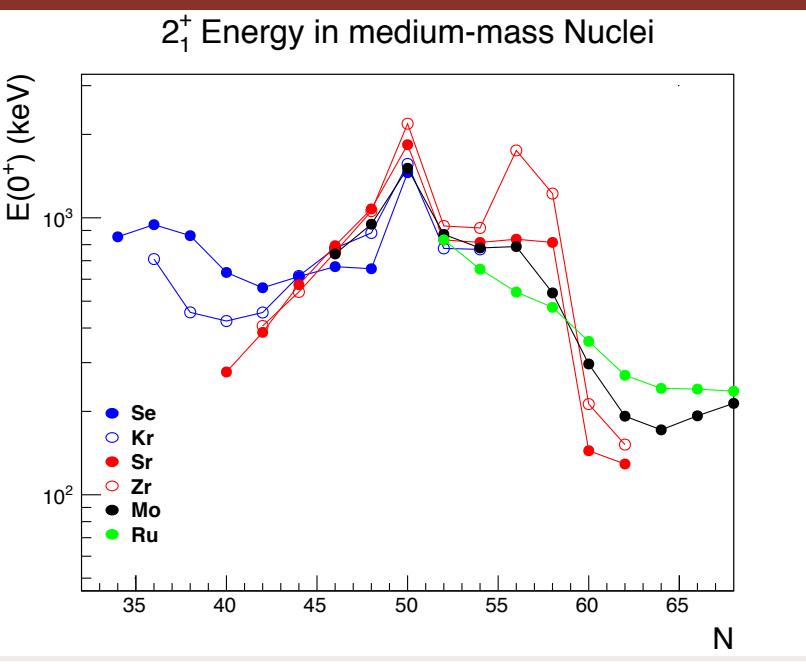
# Thank you! Merci

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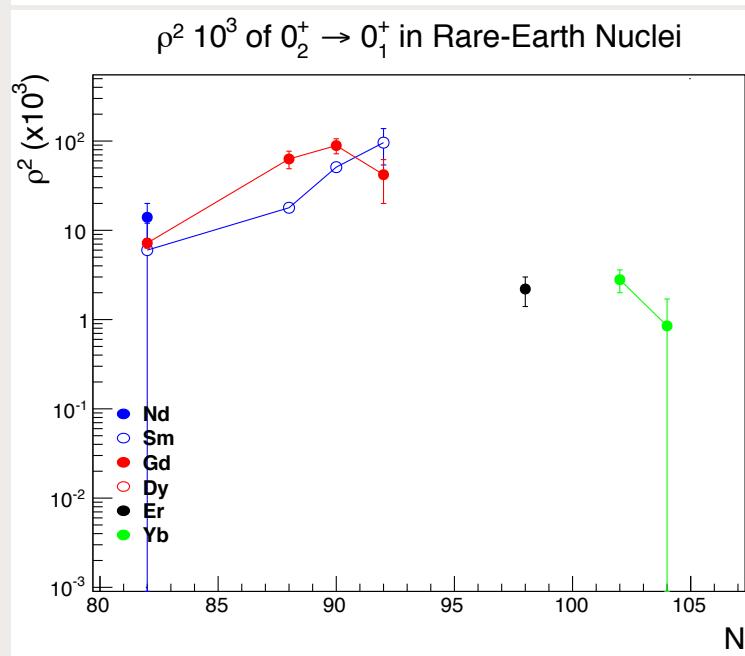
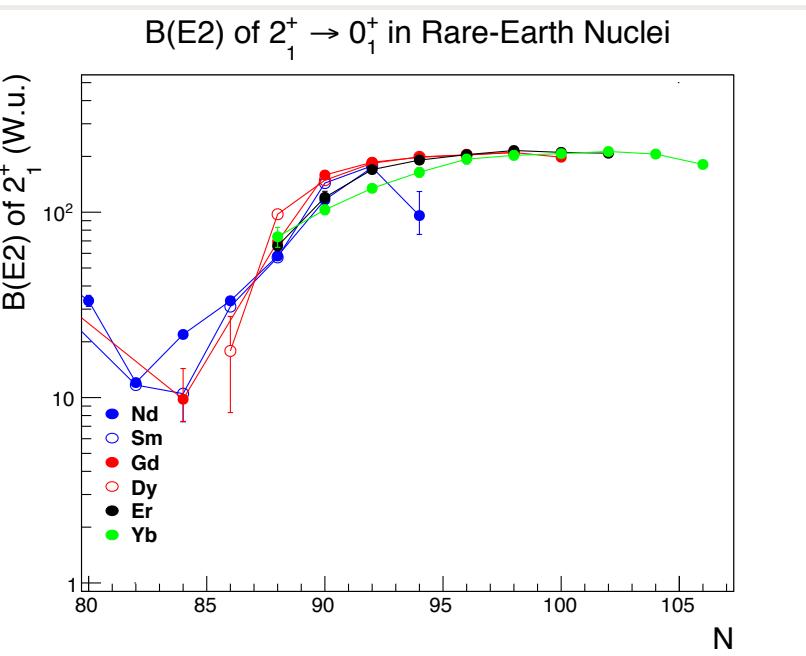
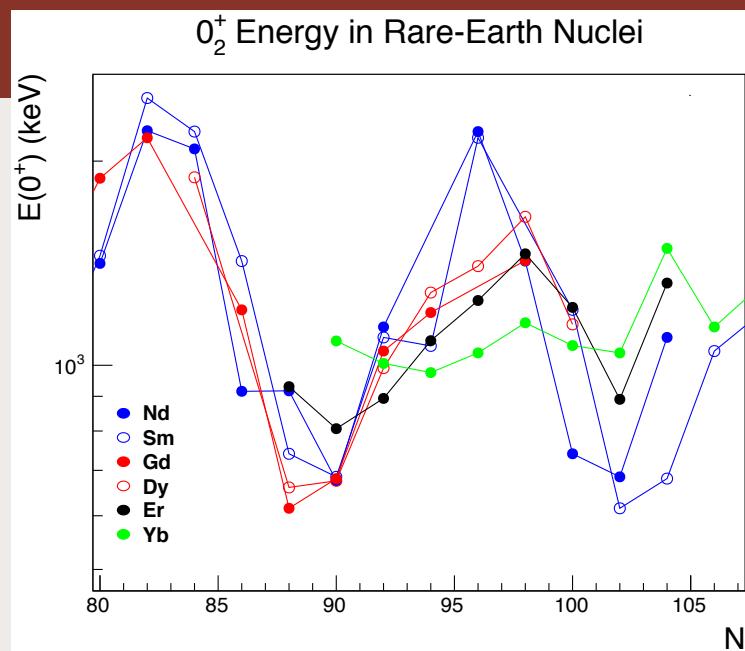
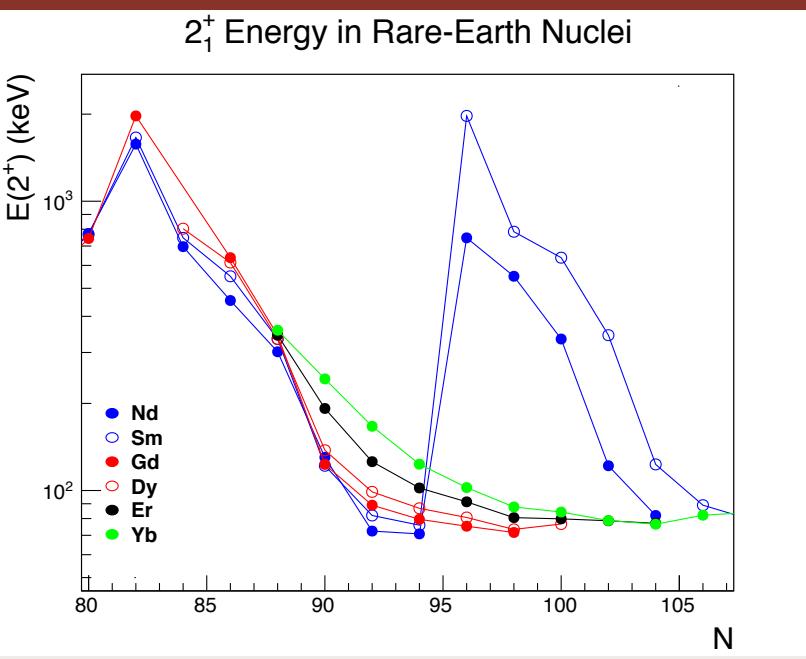
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Victoria | Western | Winnipeg | York



# Medium-Mass Systematics



# Rare-Earth Systematics



# Rare-Earth Systematics

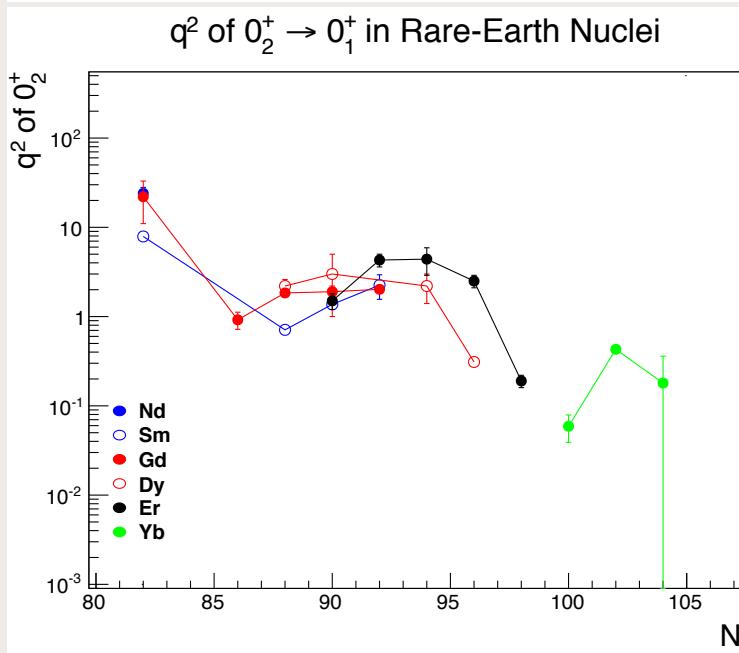
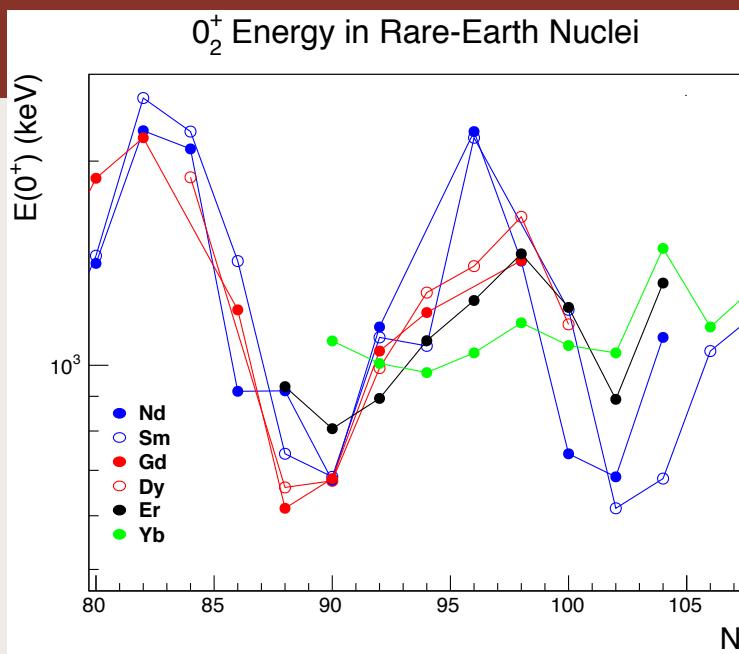
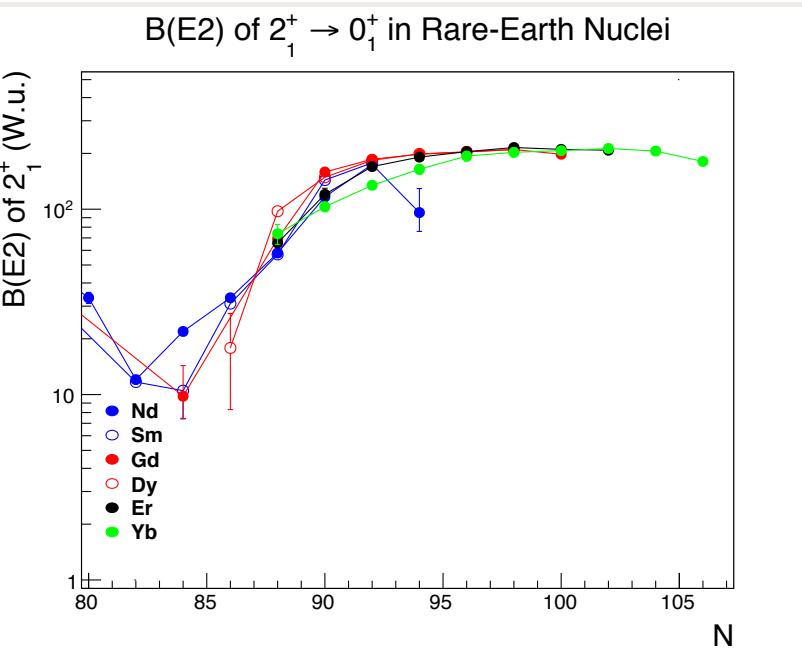
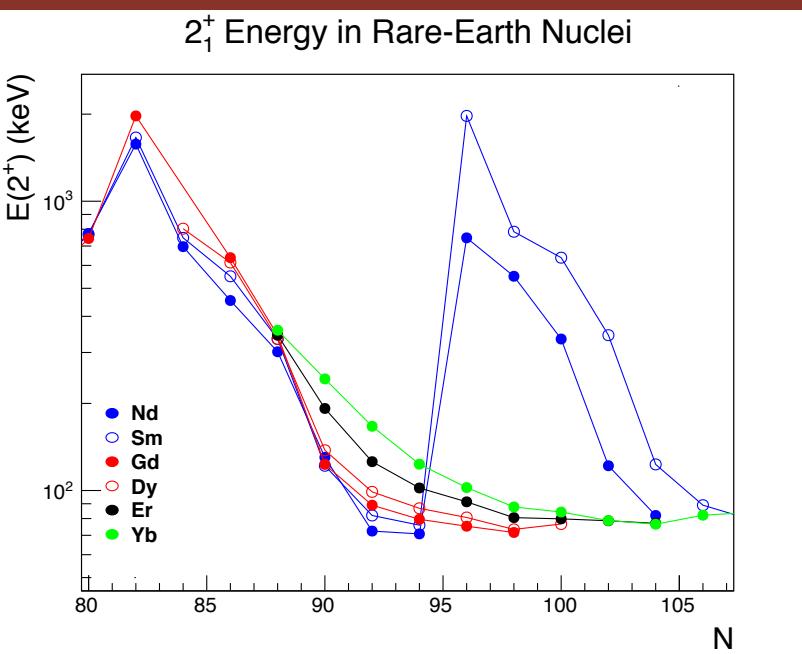
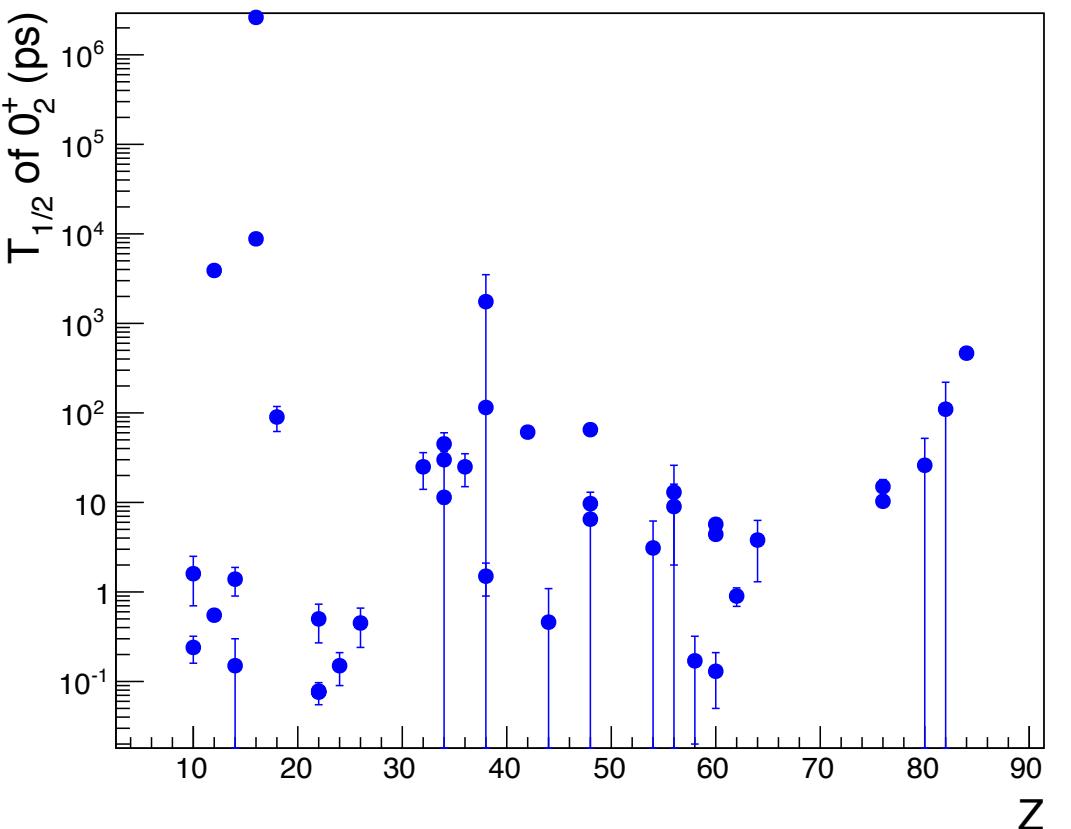


Table 1:  $T_{1/2}$  of  $0_2^+$  state is known. A  $q^2$  measurement will yield a  $\rho^2$  value.

Kibédi and Spear,  
Atomic. Data and Nucl. Data Tables 89, 77 (2005).

41  $T_{1/2}$  values known but no  $q^2$  of first excited  $0^+$  to GS  $0^+$  known

Electron spectroscopy can measure these cases.



Nucleus	Energy $0_2^+$ (keV)	Energy $2_1^+$ (keV)	$T_{1/2}$ (ps)
$^{22}_{10}\text{Ne}_{12}$	6234.3	1274.58	0.24 (0.08)
$^{24}_{10}\text{Ne}_{14}$	4766.5	1981.6	1.6 (0.9)
$^{28}_{12}\text{Mg}_{16}$	3862.15	1473.54	0.55 (0.07)
$^{30}_{12}\text{Mg}_{18}$	1788.2	1482.8	3900 (400)
$^{26}_{14}\text{Si}_{12}$	3336.4	1797.3	1.39 (0.49)
$^{32}_{14}\text{Si}_{18}$	4983.9	1941.4	0.15 (0.15)
$^{36}_{16}\text{S}_{20}$	3346	3290.9	8800 (200)
$^{44}_{16}\text{S}_{28}$	1365	1315	2.619e+06 (26000)
$^{40}_{18}\text{Ar}_{22}$	2120.8	1460.85	90 (28)
$^{46}_{22}\text{Ti}_{24}$	2611	889.286	0.076 (0.021)
$^{48}_{22}\text{Ti}_{26}$	2997.22	983.539	0.078 (0.009)
$^{50}_{22}\text{Ti}_{28}$	3862.79	1553.78	0.5 (0.23)
$^{54}_{24}\text{Cr}_{30}$	2829.62	834.855	0.15 (0.06)
$^{56}_{26}\text{Fe}_{30}$	2941.5	846.778	0.45 (0.21)
$^{78}_{32}\text{Ge}_{46}$	1546.6	619.36	25 (11)
$^{34}_{34}\text{Se}_{44}$	1498.6	613.727	45 (8)
$^{80}_{34}\text{Se}_{46}$	1478.82	666.27	11.4 (1.7)
$^{82}_{34}\text{Se}_{48}$	1410.3	654.75	30 (30)
$^{84}_{36}\text{Kr}_{48}$	1837.3	881.615	25 (10)
$^{82}_{38}\text{Sr}_{44}$	1310.89	573.54	1750 (1750)
$^{88}_{38}\text{Sr}_{50}$	3156.19	1836.09	1.5 (0.6)
$^{96}_{38}\text{Sr}_{58}$	1229.28	814.93	115 (12)
$^{96}_{42}\text{Mo}_{54}$	1148.13	778.237	61 (8)
$^{96}_{44}\text{Ru}_{52}$	2148.78	832.56	0.46 (0.63)
$^{116}_{48}\text{Cd}_{68}$	1282.56	513.49	65 (4)
$^{118}_{48}\text{Cd}_{70}$	1285.61	487.77	9.7 (1.4)
$^{120}_{48}\text{Cd}_{72}$	1388.9	505.94	6.5 (6.5)
$^{120}_{54}\text{Xe}_{66}$	908.7	322.61	3.1 (3.1)
$^{142}_{56}\text{Ba}_{86}$	1535.53	359.596	9 (7)
$^{144}_{56}\text{Ba}_{88}$	1020.03	199.326	13 (13)
$^{142}_{58}\text{Ce}_{84}$	2031.01	641.282	0.17 (0.15)
$^{144}_{60}\text{Nd}_{84}$	2084.68	696.561	0.13 (0.08)
$^{148}_{60}\text{Nd}_{88}$	916.93	301.705	4.4 (0.3)
$^{150}_{60}\text{Nd}_{90}$	675.9	130.21	5.7 (0.3)
$^{154}_{62}\text{Sm}_{92}$	1099.26	81.981	0.9 (0.21)
$^{158}_{64}\text{Gd}_{94}$	1196.16	79.5128	3.8 (2.5)
$^{190}_{76}\text{Os}_{114}$	911.78	186.718	15 (3)
$^{192}_{76}\text{Os}_{116}$	956.54	205.794	10.3 (1.1)
$^{186}_{80}\text{Hg}_{106}$	523	405.33	26 (26)
$^{190}_{82}\text{Pb}_{108}$	658	773.9	110 (110)
$^{208}_{84}\text{Po}_{124}$	1271.6	686.526	465 (20)